Debugging and Slicing

Mohammad Mousavi

Halmstad University, Sweden

http://bit.ly/TAV16

Testing and Verification, March 4, 2016

Slices

An executable subset of the program

- capturing possible (indirect) dependencies
- among all definitions and uses
- influencing the value of a set of variables.

Also called: cone of influence reduction



Annotated Flow Graphs

Defining nodes

DEF(n, v) holds (for a var. v and a node n), when n defines v. Examples:

- ► input(v), or
- ▶ *v* := *exp*

 $DEF(n) = \{v \mid DEF(n, v)\}$

Annotated Flow Graphs

Using nodes

USE(n, v) holds (for a var. v and a node n), when n uses the values of v. Examples:

- ▶ output(v),
- x := exp(v),
- if cond(v) then, or
- while cond(v) do, ...

```
USE(n) = \{v \mid USE(n, v)\}
```

```
Also REF(n, v) in the literature
```

Definitions and Uses: An Example





- 1: Input(x)
- 2: Input(y)
- 3: total := 0
- 4: sum := 0
- 5: if $x \le 1$ then
- 6: sum := y
- 7: **else**
- 8: Input(z)
- 9: total := x * y
- 10: end if
- 11: Write(total, sum)
- Slice on $\{\textit{total}\}$ at 11?

- 1: Input(x)
- 2: Input(y)
- 3: total := 0
- 4: sum := 0
- 5: if $x \le 1$ then
- 6: sum := y
- 7: **else**
- 8: Input(z)
- 9: total := x * y
- 10: **endif**
- 11: Write(total, sum)
- Slice on $\{\textit{total}\}$ at 11?

Slice on $\{total\}$ at 11: 1: Input(x) 2: Input(y) 3: total := 0 4: if $x \le 1$ then 5: 6: else 7: total = x * y

8: end if

1: Input(b) 2: c := 13: d := 34: a := d5: d := b + d6: b := b + 17: a := b + c8: Write(a) Slice on $\{d, c\}$ at 6?

Slice on {*d*, *c*} at 6: 1: Input(b) 2: c := 1 3: d := 3 4: d := b + d

 $(6, \{d, c\})$ (in general (n, V)): the slicing criterion

Outline of the algorithm

Slice criterion (n, V)

- Statements in the slice: those define the relevant variables.
- At $n, v \in V$: relevant.
- A relevant $v \in DEF(m)$: v is no more relevant above m,
- ▶ but then all variables in USE(m) become relevant above m.

Relevant Variables

Given a slicing criterion
$$(n, V)$$
, $Relevant_0(m) =$

$$\begin{cases}
1 \quad V & \text{if } m = n + 1 \\
2a)\{v \mid \exists_{m \to m'}(v \in relevant(m') \setminus DEF(m) \lor & \text{otherwise} \\
2b) & (DEF(m) \cap relevant(m') \neq \emptyset \land v \in USE(m)))\}
\end{cases}$$

- 1) base case: all variables in V are initially relevant
- 2a) v remains relevant: has been relevant below and not defined at m
- 2b) v becomes relevant: defines relevant variables

```
Slicing criterion: (6, \{d, c\})?
Relevant_0(m) =
  1) V
                                                                                          if m = n + 1
\begin{cases} 2a) \{ v \mid \exists_{m \to m'} (v \in relevant(m') \setminus DEF(m) \lor \\ 2b) & (DEF(m) \cap relevant(m') \neq \emptyset \land v \in USE(m))) \} \end{cases}
                                                                                              otherwise
                        Relevant<sub>0</sub>(m)
  m
 1 Input(b) \emptyset
 2 c := 1  {b}
 3 d := 3 \{c, b\}
 4 a := d \{c, b, d\}
 5 d := b + d \{ c, b, d \}
 6 b := b + 1 \{ d, c \}
                          \{\mathbf{d}, \mathbf{c}\}
```

Slicing Sequential Programs

 $m \in Slice_0(n, V)$ when

1.
$$n = m$$
 and $DEF(m) \cap V \neq \emptyset$, or

2. $m \to \ldots \to n$ and there exists an m' such that $m \to m'$ and $DEF(m) \cap Relevant_0(m') \neq \emptyset$

Slicing Sequential Programs

 $m \in Slice_0(n, V)$ when

1.
$$n=m$$
 and $DEF(m)\cap V
eq \emptyset$, or

2. $m \rightarrow \ldots \rightarrow n$ and

there exists an m' such that $m \to m'$ and

 $DEF(m) \cap Relevant_0(m') \neq \emptyset$

Relevant₀(m) DEF(m) \in Slice₀(6, {d, c}) m 1 Input(b) \emptyset *{b}* 2 c := 1 {*b*} {*c*} $3 d := 3 \{c, b\}$ $\{d\}$ 4 a := d $\{c, b, d\}$ {a} X $5 d := b + d \{c, b, d\}$ $\{d\}$ $\sqrt{}$ $6 b := b + 1 \{d, c\}$ *{b}* × $\{d, c\}$

lnput(x)
 lnput(z)
 if x < 10 then
 z := z + 2;
 else
 z := z - 1;
 end if
 Write(z)
 Slice wrt. the criterion (3, {x})?



Slice wrt. the criterion $(3, \{x\})$?

m	$Relevant_0(m)$	DEF(m)	\in Slice ₀ (3, {x})
1 Input(x)	Ø	$\{x\}$	\checkmark
2 Input(z)	$\{x\}$	$\{z\}$	×
3,5 if $x < 10$ then / else	$\{x\}$	Ø	×
	$\{x\}$		

lnput(x)
 lnput(z)
 if x < 10 then
 z := z + 2;
 else
 z := z - 1;
 end if
 Write(z)
 Slice wrt. the criterion (8, {z})?



m	$Relevant_0(m)$	DEF(m)	\in Slice ₀ (8, {z})
1 Input(x)	Ø	$\{x\}$	×
2 Input(z)	Ø	$\{z\}$	
3,5 if $x < 10$ then / else	$\{z\}$	Ø	×
4 z := z + 2	{ <i>z</i> }	$\{z\}$	\checkmark
6 z := z - 1	{ <i>z</i> }	$\{z\}$	\checkmark
7 end if	{ <i>z</i> }	Ø	×
8 Write(z)	{ <i>z</i> }	Ø	×
	$\{z\}$		

Slicing Structured Programs: Informal Idea

- 1. Start with sequential slicing algorithm: $Slice_0(n, v)$
- Find all conditionals Cond_{k+1}(n, V) influencing m ∈ Slice_k(n, v)
- Add the following node to Slice_k(n, V), the result: Slice_{k+1}(n, V)
 - 3.1 the conditional in $c \in Cond_k n, V$ and
 - 3.2 those statement influencing the conditions of c
- 4. repeat 2 until a fixed-point

(Inverse) Denominators

 $m \in IDen(n)$ (*m* inversely denominates *n*) when *m* appears in all paths $n \to \ldots \to n_t$.

m = NIDen(n) (the nearest inverse denominator of n) when $m \in IDen(n)$ and for all $m' \in IDen(n)$ either m = m' or there is a simple path $m \rightarrow \ldots \rightarrow m'$.

 $m \in Infl(n)(m \text{ is influenced by } n)$ when m appears in a path from n to NIDen(n) $(m \neq n, m \neq NIDen(n), NIDen(n)$ may not appear in the path).

1: Input(x) 2: lnput(z)3: if x < 10 then 4: z = z + 2: 5: else 6: z = z - 1: 7: end if 8: Write(z) NIDen(1)? 2. Infl(1)? \emptyset . NIDen(2)? 3. Infl(2)? ∅. Observation, for sequential nodes $Infl(n) = \emptyset$. NIDen(3)? 7. Infl(3)? {4,6}.



Slicing Structured Programs

Given a slicing criterion (n, V): $m \in Cond_{k+1}(n, V)$ (conditions influencing $Slice_k(n, V)$) when there exists $m' \in Slice_k(n, V)$ and $m' \in Infl(m)$.

$v \in Relevant_{k+1}(m)$ when $v \in Relevant_k(m)$ or there exists an $m' \in Cond_{k+1}(n, V)$ and $v \in Relevant_0(m)$ w.r.t. the slicing criterion (m', USE(m')).

 $m \in Slice_{k+1}(n, V)$ when $m \in Cond_{k+1}(n, V)$ or there exists an m' such that $m \to m'$ and $DEF(m) \cap Relevant_{k+1}(m') \neq \emptyset$.

- Slice wrt. $(8, \{z\})$
 - 1: Input(x)
 - 2: Input(z)
 - 3: if x < 10 then
 - 4: z = z + 2;
 - 5: **else**
 - 6: z = z 1;
 - 7: end if
 - 8: Write(z)

```
Slice_0(8, \{z\}) = \{2, 4, 6\}.
```

 $m \in Cond_{k+1}(n, V)$ (conditions influencing $Slice_k(n, V)$) when there exists $m' \in Slice_k(n, V)$ and $m' \in Infl(m)$.

```
Slice wrt. (8, \{z\})
```

- 1: Input(x)
- 2: Input(z)
- 3: if x < 10 then

4:
$$z = z + 2;$$

- 5: **else**
- 6: z = z 1;
- 7: end if
- 8: Write(z)

```
Slice_0(8, \{z\}) = \{2, 4, 6\}.
Cond_1(8, \{z\}) = \{3\}
Slice_1(8, \{z\})?
```

m	$Relevant_1(m)$	DEF(m)	\in Slice ₁ (8, {z})
1 Input(x)	Ø	$\{x\}$	
2 Input(z)	{ x }	$\{z\}$	
3,5 if $x < 10$ then / else	$\{z, \mathbf{x}\}$	Ø	×
4 z := z + 2	{ <i>z</i> }	$\{z\}$	\checkmark
6 z := z - 1	{ <i>z</i> }	$\{z\}$	\checkmark
7 end if	{ <i>z</i> }	Ø	×
8 Write(z)	{ <i>z</i> }	Ø	×
	$\{z\}$		

Another Example

Slice wrt. $(11, \{sum\})$?

1: lnput(x)2: Input(y)3: sum := 04: if x < 1 then 5: y := 16: end if 7: while $y \ge 1$ do 8. sum := sum + x9: y := y - 110: end while 11: Write(sum)



m	DEF(m)	Relevant ₀ (m)	Slice ₀	Cond ₁	Rel ₁	Slice ₁
1	{ <i>x</i> }	Ø	,	×	Ø	\checkmark
2	{ <i>y</i> }	{ <i>x</i> }	×	×	{ <i>x</i> }	\checkmark
3	{sum}	{ <i>x</i> }	\checkmark	×	$\{x, y\}$	\checkmark
4	Ø	$\{sum, x\}$	×	×	$\{sum, x, y\}$	×
5	{ <i>y</i> }	$\{sum, x\}$	×	×	$\{sum, x\}$	\checkmark
6	Ø	$\{sum, x\}$	×	×	$\{sum, x, y\}$	×
7	Ø	$\{sum, x\}$	×		$\{sum, x, y\}$	\checkmark
8	{sum}	$\{sum, x\}$	\checkmark	×	$\{sum, x, y\}$	\checkmark
9	{ <i>y</i> }	$\{sum, x\}$	×	×	$\{sum, x, y\}$	\checkmark
10	Ø	{sum}	×	×	{sum}	×
11	Ø	{ <i>sum</i> }	×	×	{sum}	×
		{ <i>sum</i> }			{ <i>sum</i> }	

m	DEF(m)	Cond ₂	Rel ₂	Slice ₂	Slice ^(*)
1	{ <i>x</i> }	×	Ø	\checkmark	\checkmark
2	{ <i>y</i> }	×	{ <i>x</i> }		
3	$\{sum\}$	×	$\{x, y\}$		
4	Ø	\checkmark	$\{sum, x, y\}$		
5	{ <i>y</i> }	×	$\{sum, x\}$		
6	Ø	×	$\{sum, x, y\}$	×	
7	Ø	\checkmark	$\{sum, x, y\}$		
8	$\{sum\}$	×	$\{sum, x, y\}$		
9	$\{y\}$	×	$\{sum, x, y\}$		
10	Ø	×	{ <i>sum</i> }	×	
11	Ø	×	{ <i>sum</i> }	×	×

(*) Syntactic check after generating the slice:

if then $(/else) \in Slice \Rightarrow$ (the corresponding) end if $\in Slice$ while ... do $\in Slice \Rightarrow$ (the corresponding) end while $\in Slice$

. . .

The Ideal Slicing Algorithm?

Slice wrt. $(2, \{x\})$?

1: Input(x)2: x := x

Slice wrt. $(5, \{x\})$?

- 1: if true then
- 2: x := 1
- 3: **else**
- 4: x := 2
- 5: end if

No algorithm for the smallest slice exists! Reason: Undecidability of halting/termination.

Slicing: Applications

- 1. Test adequacy: for each output variable, all du-paths in its slice must be covered
- Robustness testing: Add pseudo-variables that check dangerous situations, generate the slice and test
- 3. Regression testing: testing if a change influences a particular component

(i.e., if the slice of the component interface contains the change)

4. Debugging:

code review

comparing a correct running program with a new faulty version

(Automated) Debugging: A Sorting Program

```
1: int main(int argc, char * argv[])
 2: {
3: int *a:
 4: int i:
 5: a = (int *) malloc((argc - 1) * sizeof(int));
 6: for (i = 0; i < argc - 1; i + +)
 7: a[i] = atoi(argv[i + 1]);
 8: shell_sort(a, argc);
 9: printf("Output: ");
10: for (i = 0; i < argc - 1; i++)
   printf("%d ", a[i]);
11:
12: free(a);
13: return 0:
14: \}
```

Mousavi: Debugging and Slicing

(Automated) Debugging: A Sorting Program

Once upon a time, a tester found the following bug:

\$./simple 5 4 3 2 1 666666 Output: 0 1 2 3 4 5

How do we find the fault?

Find and Focus

Scientific method:

- 1. assume,
- 2. organize an experiment,
- 3. if refuted, refine your assumption and repeat.

possible formalization: invariants and assertions

Observing: logging the value of infected variables

e.g., print command in gdb

- Watching: keeping an eye on infected variables e.g., break and watch commands in gdb
- Slicing: find the slice responsible for infection see the lecture on slicing



Getting Our Hands Dirty...

We use gdb (any other debugger will do)

Reproduce the test:

run 5 4 3 2 1 666666 Damn, the tester was right! (Not always that easy, try 55 4.)

- Simplify the test-case run 5 4 3 2
- Find the possible the origins, focus on a problem area, e.g., a[0] and shell_sort (See slicing next...)
- Isolate the causes what makes a[0] wrong? compare it with the sane situation, what is different?
- Correct the problem

TRAFFIC

- 1. Track the problem
- 2. Reproduce the failure
- 3. Automate and simplify the test-case: minimal test-case \Leftarrow
- 4. Find possible origins: where it first went wrong
- 5. Focus on the most likely origins: what part of state is infected
- 6. Isolate the chain: what causes the state to be infected \Leftarrow



7. Correct the defect



Automated Debugging is about Perfection

Perfection

Perfection is achieved not when you have nothing more to add, but when there is nothing more left to take away.

Antoine de Saint-Exupéry

Automated Debugging

Take out all that has nothing to do with the failure...

Debugging: An Example

- My slides for today (in LATEX) did not compile
- some part of it did work before (older slides)
- divide the new parts into two:
 - 1. remove first half part
 - 2. if the problem is there, repeat until one (new) slide is left
 - 3. if not, put back the second half and and remove the first, repeat
- apply the same technique to the content of the remaining slide

This is called delta debugging: our order of business for today.



(Ack. figures are due to Andreas Zeller.)

Mousavi: Debugging and Slicing

Minimizing Delta Debugging: Basic Idea

Try to find the minimal environment causing the failure by:

- Divide the circumstances C in n parts C_i,
- remove a part C_i such that C \ C_i causes failure, repeat the algorithm with C \ C_i,
- if no such part exists, choose a bigger n < |C| and repeat.

Minimizing Delta Debugging: Formalization

- Circumstances: C (input but could be: program, environment, etc.)
- Test: $test: 2^{\mathcal{C}} \rightarrow \{\times, \checkmark, ?\}$
- ▶ Starting state: $C_x \subseteq C$, such that $test(C_{\times}) = \times$
- ▶ Goal: find a minimal subset $C'_{\times} \subseteq C_{\times}$ such that $test(C'_{\times}) = \times$

Minimizing Delta Debugging: Algorithm

 $ddmin(C_{\times}, 2)$, where

 $ddmin(C'_{\times}, n) =$

$$\begin{array}{ll} C'_{\times}, & \text{if } \mid C'_{\times} \mid = 1, \\ ddmin(C'_{\times} \setminus C_i, max(n-1,2)) & \text{else if } \exists_{i \leq n} test(C'_{\times} \setminus C_i) = \times \\ ddmin(C'_{\times}, max(2n, \mid C'_{\times} \mid)) & \text{else if } n < \mid C'_{\times} \mid \\ C'_{\times} & \text{otherwise} \end{array}$$

where C_i 's are partitions of C'_{\times} of (almost) equal size.

Application in Random Testing

Idea

- feed huge inputs to the system (guaranteed crash on huge input)
- simplify input
- present the simplified result as a test-case

Application in Random Testing

Examples

- applied to command UNIX tools
- FLEX (lexical analyzer): crashed on a test-case of 2121 characters
- NROFF (document formatter): crashed on a single control character
- CRTPLOT (plotter output): crashed on single characters 't' or 'f'

Improvements

- caching: save the test outcomes, use the saved data
- stop early: define a criterion to stop the algorithm, e.g.,
 - 1. no progress
 - 2. reaching a certain granularity
 - 3. upper bound on time
- use structures, e.g., blocks instead of characters
- differences vs. circumstances (compare sane with insane)

What is a Cause?

- Effect: the failure
- Cause: an event preceding effect, without which effect would not have happened

Isolating the cause

- Cause: the minimal difference between the worlds with and without the failure
- Challenge: the world without failure: the goal of debugging
- Two solutions:
 - 1. manipulate the world by a debugger: turn infected to sane
 - 2. use another test-case in which no fault appears

Isolating: The Sorting Program Case

- 1. ./sample produces a failure on 5 4 3 666666
- 2. works fine on 5 4 3
- 3. find combinations of
 - 3.1 states of 1 with 2 such that the program passes
 - 3.2 states of 2 with 1 such that the program fails
- 4. the difference between the two leads to a cause



Mousavi: Debugging and Slicing

Delta Debugging: The Algorithm

Start from:

- $C_{\checkmark} = \emptyset$: passing circumstances and
- ► C_×: failing circumstances
- 1. compute the difference Δ between the failing and the passing circ., divide into *n* parts: Δ_i ,
- 2. remove Δ_i from the failing circ.; it is the new passing circ., if it passes
- 3. add Δ_i to the passing circ.; it is the new failing circ., if it fails
- 4. add Δ_i to the passing circ.; it is the new passing circ., if it passes
- 5. remove Δ_i from the failing circ.; it is the new failing circ., if it fails
- 6. increase *n* if none of the above holds
- 7. repeat until the difference is a singleton

Delta Debugging: Algorithm

 $dd(C_{\checkmark}, C_{\times}, 2)$, where $ddmin(C'_{\checkmark}, C'_{\times}, n)$ is defined recursively as:

$$\begin{cases} (C'_{\checkmark}, C'_{\times}) & \text{if } |\Delta| = 1, \\ dd(C'_{\times} \setminus \Delta_i, C'_{\times}, 2) & \text{else if } \exists_{i \le n} test(C'_{\times} \setminus \Delta_i) = \checkmark \\ dd(C'_{\checkmark}, C'_{\checkmark} \cup \Delta_i, 2) & \text{else if } \exists_{i \le n} test(C'_{\checkmark} \cup \Delta_i) = \times \\ dd(C'_{\checkmark} \cup \Delta_i, C'_{\times}, max(n-1, 2)) & \text{else if } \exists_{i \le n} test(C'_{\checkmark} \cup \Delta_i) = \checkmark \\ dd(C'_{\checkmark}, C'_{\times} \setminus \Delta_i, max(n-1, 2)) & \text{else if } \exists_{i \le n} test(C'_{\times} \setminus \Delta_i) = \times \\ dd(C'_{\checkmark}, C'_{\times}, min(2n, |\Delta|)) & \text{else if } n < |\Delta| \\ (C'_{\checkmark}, C'_{\times}) & \text{otherwise} \end{cases}$$

where $\Delta = C'_{\times} \setminus C'_{\checkmark}$ and Δ_i 's are *n* partitions of Δ of (almost) equal size.

Delta Debugging: Applied to Test-Case Simplification

Start from:

- $C_{\checkmark} = \emptyset$: the empty test-case
- C_{\times} : the test-case leading to failure
- Much more efficient than minimizing delta debugging

Delta Debugging: Applied to Regression Testing

Start from:

- Goal: find out what went wrong in the new development (the old version worked well)
- $C_{\checkmark} = \emptyset$: basis is the old program, no changes needed
- ► C_×: difference between the old and the new i.e., changes needed to obtain the new program from the old one

Isolating the Cause: Idea

- Capture the state of the program
- Compare the states of a passes and a failed run
- The smallest difference Δ is the variable causing the problem
- Find out what influences this variable

Program State: Memory Graphs



Comparing the Differences



Implementable as debugger commands, e.g., set variable size = 2.

Isolating the Cause: Implementation

- Compute the common subgraph of the passing and failing memory graphs. Let the difference be C_×.
- ► Implement *C*_× as debugger commands.
- \blacktriangleright Apply delta-debugging to $\mathit{C_{\!\checkmark}}=\emptyset$ and $\mathit{C_{\!\times}}$
 - 1. Apply differences to the memory graphs and test.
 - 2. At each step of *dd* if the changed state is not a valid state (program does not run), return ?, if it is a valid state, return the result of the test,
- The result Δ leads to a cause.

Isolating the Cause: Sorting Case

Run the algorithm before calling shell_sort with the state of ./sample 7 8 9 as passing and ./sample 11 14 as failing. If 0 at the state: test fails \times , passes \checkmark otherwise.

1.
$$\mathcal{C}_{ imes} = \{ \texttt{a[], i, size, argc, argv[]} \}, \ \mathcal{C}_{\checkmark} = \emptyset.$$

- 2. new failing state: a[], argv[1] \times
- 3. new passing state: $argv[1] \checkmark$
- 4. new passing state: $a[0] \checkmark$
- 5. new passing state: a[0] and a[1] \checkmark

6. $\Delta = \{ a[2] \}$

Isolating the Cause: Illustrated Case

= δ is applied, \Box = δ is *not* applied



Isolating the Chain of Causes

- Apply delta-debugging at the start, determine the minimal passing and running state
- Choose a common point (e.g., a function call) in the middle
- Apply delta-debugging on the states of the minimal passing and failing run
- Repeat the algorithm with the rest of the program and the new passing and failing states

Finding the Culprits

- The previous algorithm gives different Δ's (causes at different points)
- Track the change of causes
- A smelling point: a ceases to be a cause and b becomes a cause

Automated Debugging

- A natural mechanization of simple debugging principles
- Provides (partial) solutions to
 - 1. testing,
 - 2. simplifying the test-cases,
 - 3. isolating the causes and
 - 4. isolating the cause-effect chain.

Notes on the Reading Material

- Covered: Chapters 5, 13 (apart from 13.6) and 14
- Chapters 1 and 12 provide background information
- Andreas Zeller's slides are also a very good source (see web page)
- Igor command-line tool can be downloaded from www.askigor.org (unfortunately, the debugging web-service is closed by now)