

System Validation: Bisimulation

Mohammad Mousavi and Jeroen Keiren



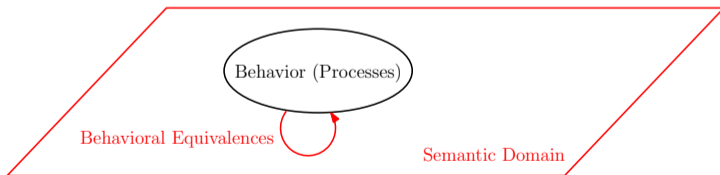
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General Overview

System Models

System Requirements



Bisimulation

$R \subseteq S \times S$ is **strong bisimulation** iff

for $s, t \in S$ s.t. $s R t$, and $a \in Act$:

- ▶ if $s \xrightarrow{a} s'$ then $\exists_{t' \in S}$ s.t. $t \xrightarrow{a} t'$ and $s' R t'$,
- ▶ if $t \xrightarrow{a} t'$ then $\exists_{s' \in S}$ s.t. $s \xrightarrow{a} s'$ and $s' R t'$,
- ▶ $s \in T$ iff $t \in T$.

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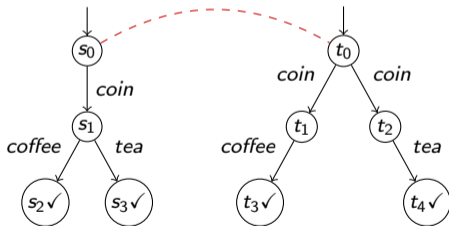
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Bisimulation

Example

$\forall sRt$

- ▶ $s \xrightarrow{a} s' \implies \exists t' \in S \ t \xrightarrow{a} t'$ and $s' R t'$, and vice versa,
- ▶ $s \in T \iff t \in T$.

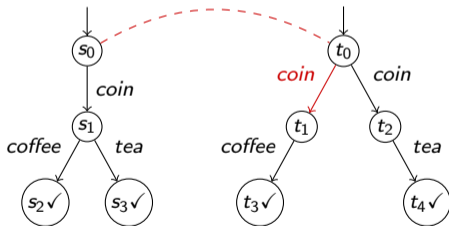


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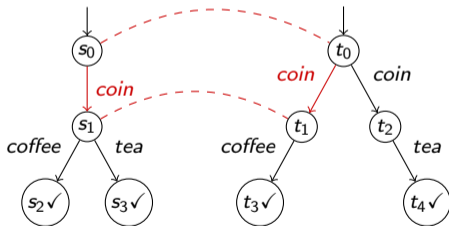


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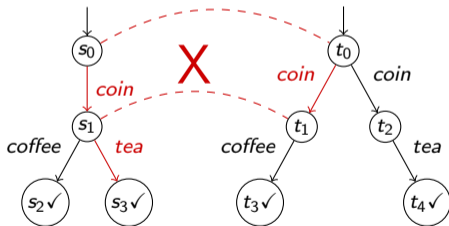


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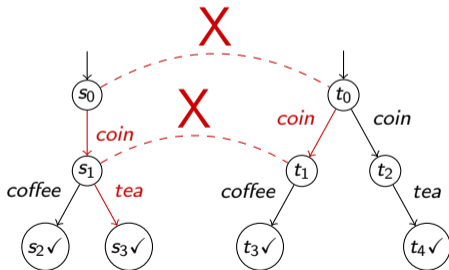


Bisimulation

Example

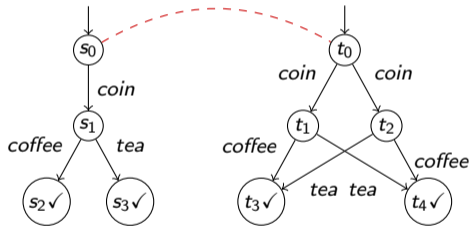
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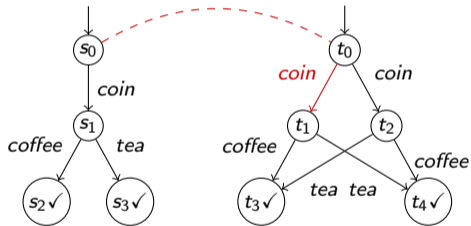
Bisimulation

An Exercise



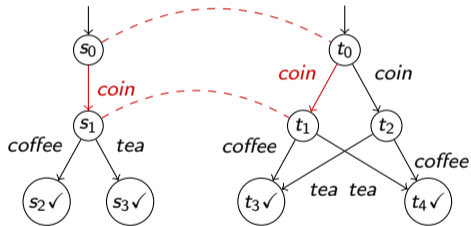
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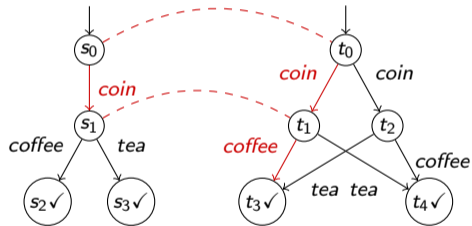
Bisimulation

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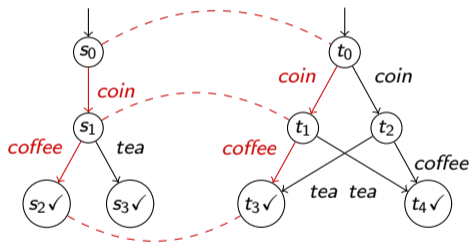
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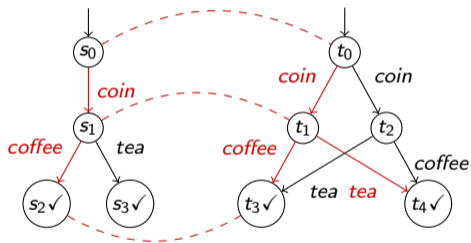
Bisimulation

An Exercise



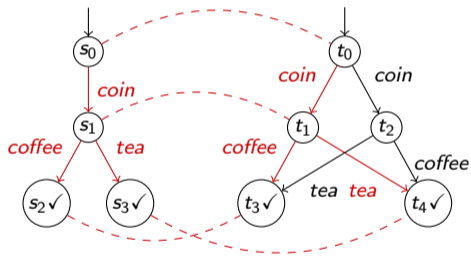
Bisimulation

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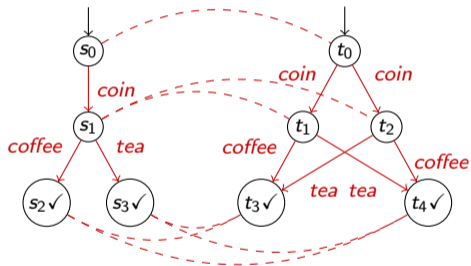
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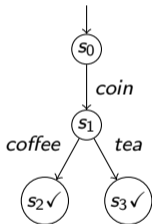
Bisimulation

An Exercise



Intermezzo

Specifying LTSs in mCRL2



mCRL2 specification:

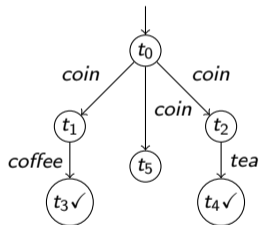
```
act coin, coffee, tea;
```

```
proc s0 = coin . s1;  
      s1 = coffee + tea;
```

```
init s0;
```

Intermezzo

Specifying LTSs in mCRL2



mCRL2 specification:

```
act coin, coffee, tea;  
  
proc t0 = coin . t1 +  
          coin . t2 +  
          coin . delta;  
  t1 = coffee;  
  t2 = tea;  
  
init t0;
```

Comparing LTSs in mCRL2

Example

`mcr122lps` Transformation into linear process form

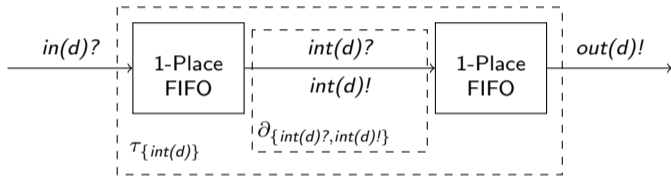
`lps2lts` Transformation into labeled transition systems

`ltsgraph` Draw the LTS (suitable for small)

`ltscompare` Checking for behavioral equivalences

Motivation

Verifying two-place buffer



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Thank you very much.