



Model-Based Testing

*There is Nothing More Practical
than a Good Theory*

TNO innovation
for life

Jan Tretmans

*TNO – ESI, Eindhoven, NL
and Radboud University, Nijmegen, NL*

Embedded Systems
Innovation **BY TNO**

Jan Tretmans

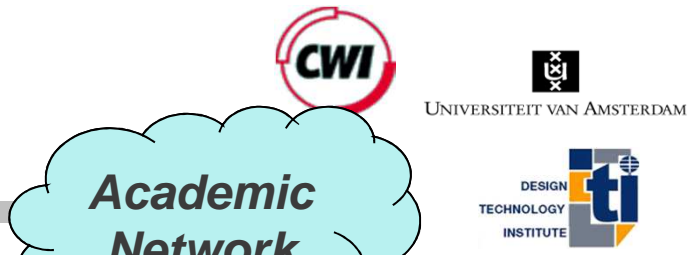
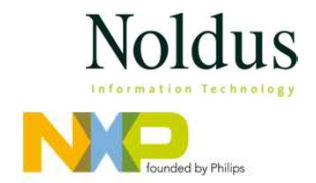
Embedded Systems
Innovation **BY TNO**

*TNO
Embedded Systems Innovation
Eindhoven
The Netherlands*



*Radboud University
Nijmegen
The Netherlands*

Embedded Systems
Innovation **BY TNO**



Industrial Network

Academic Network

Research cooperation with leading Dutch high-tech multinational industries & SME's

Research cooperation with all Dutch universities with embedded systems research

Research cooperation in EU projects

Overview

Model-Based Testing

Theory

Jan Tretmans

- MBT: What and Why
- MBT: A theory with labelled transition systems and ioco
- Variations:
 - Test selection
 - Test-based modelling

Model-Based Testing

Practice

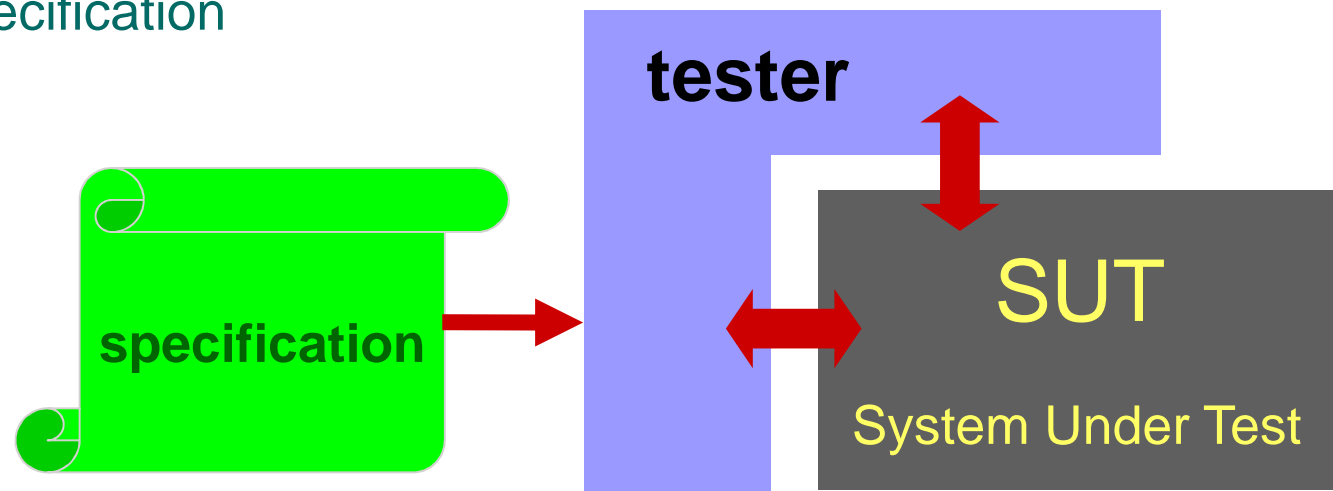
Machiel van der Bijl

- MBT: Practical exercises with Axini Test Manager
- MBT: The difference between theory and practice

Model-Based Testing

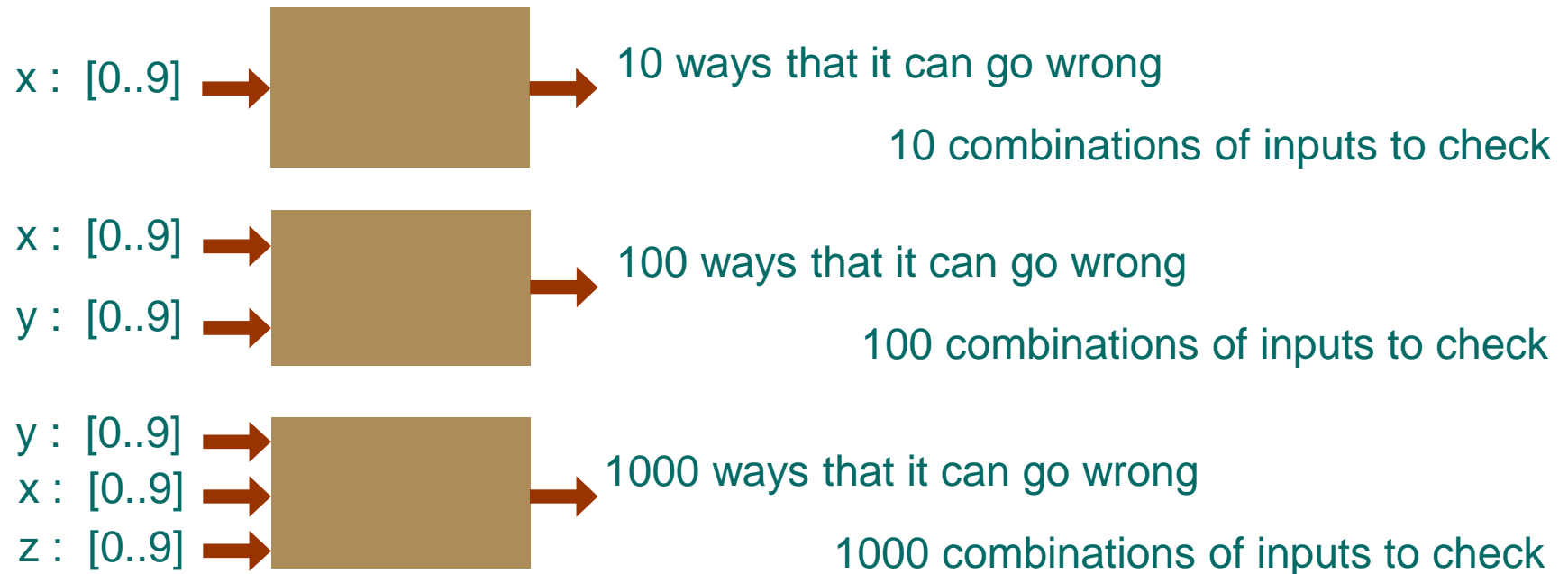
(Software) Testing

checking or measuring
some quality characteristics
of an executing object
by performing experiments
in a controlled way
w.r.t. a specification



Testing Complexity

testing effort grows exponentially with system size
testing cannot keep pace with development



Automation of testing is necessary

Testing Challenges

- **Increasing complexity**
 - more functions, more interactions, more options and parameters
- **Increasing size**
 - building new systems from scratch is not possible anymore
 - integration of legacy-, outsourced-, off-the shelf components
 - abstract from details: **models**
- **Blurring boundaries between systems**
 - more, and more complex interactions between systems
 - systems dynamically depend on other systems, systems of systems
- **Blurring boundaries in time**
 - requirements analysis, specification, implementation, testing, installation, maintenance overlap
 - more different versions and configurations

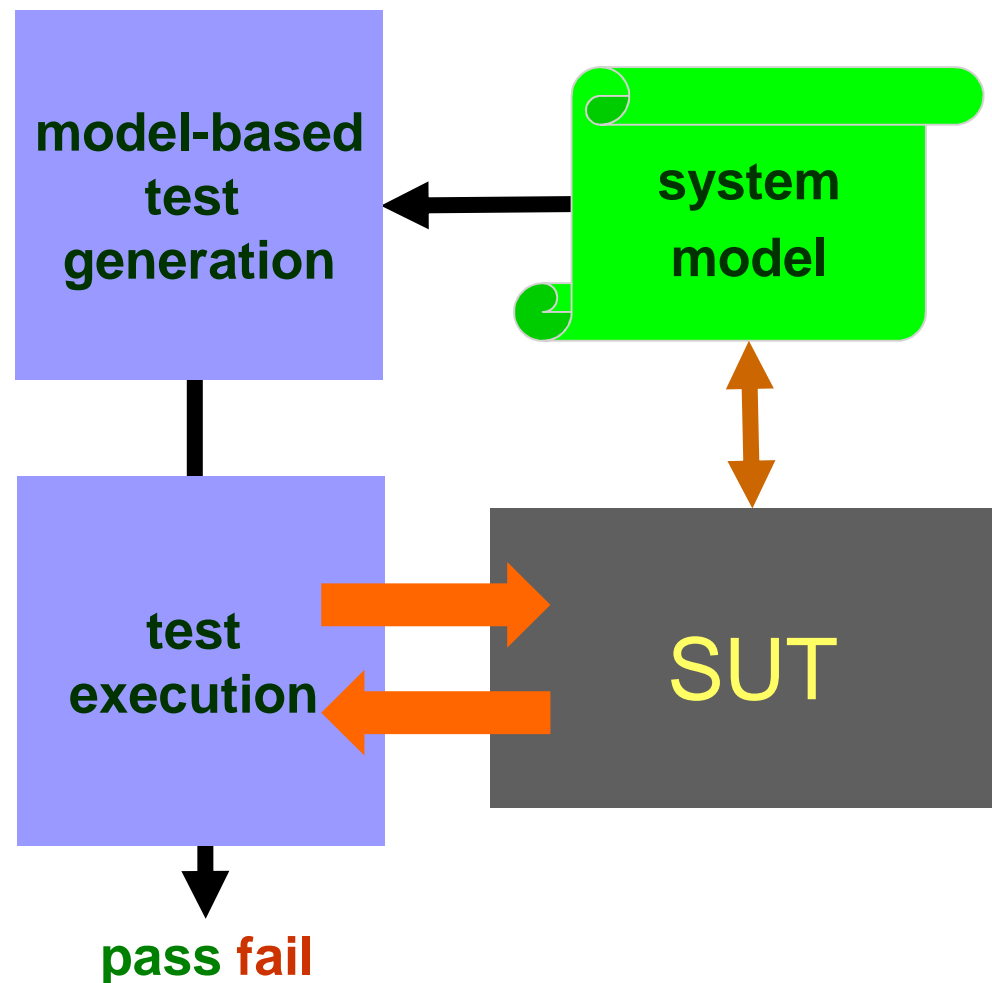
Model-Based Testing: Why

- Mastering increase in complexity, and quest for higher quality
 - testing cannot keep pace with development

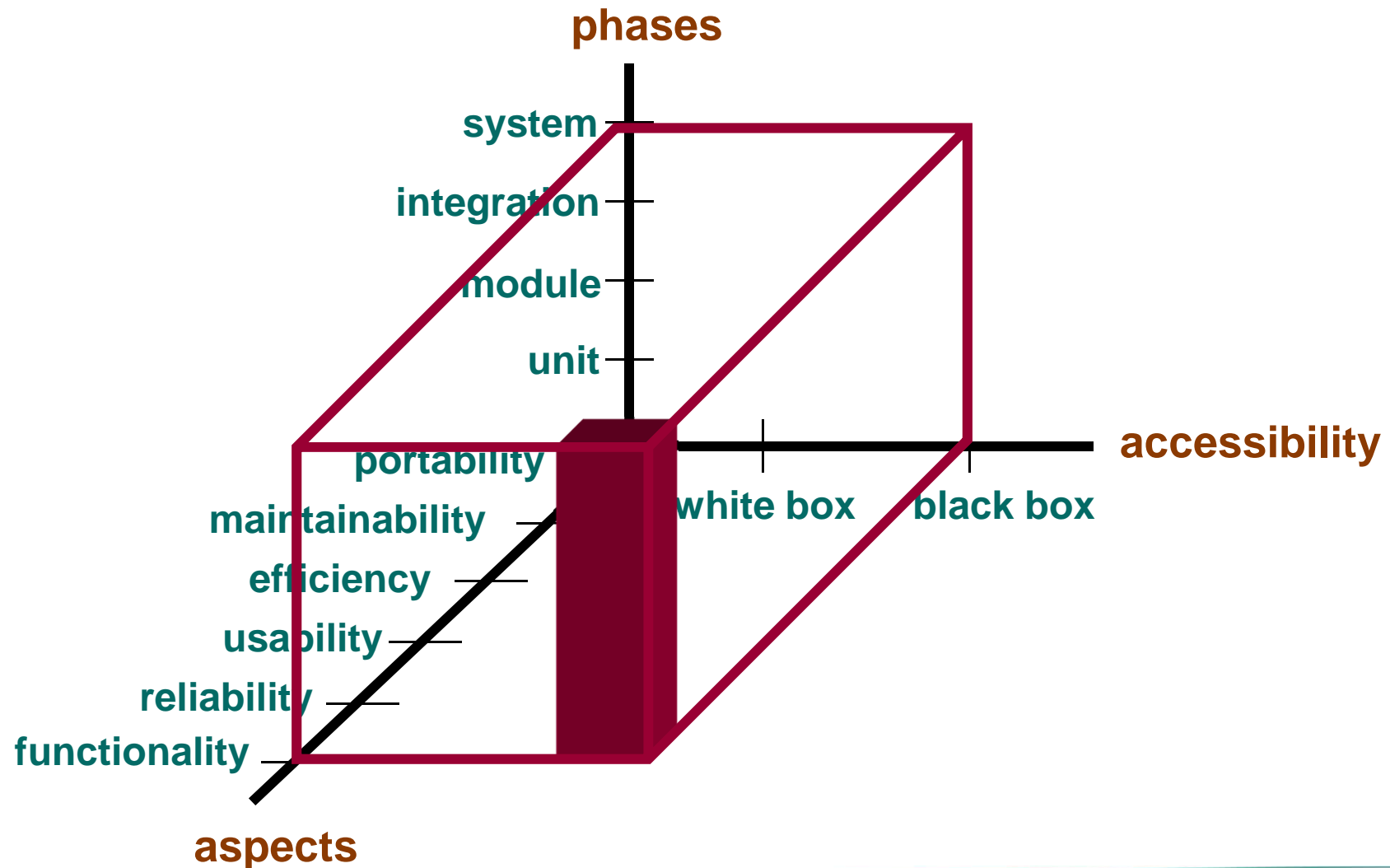
Software bugs / errors cost US economy yearly:
\$ 59.500.000.000 (www.nist.gov)
\$ 22 billion could be eliminated...

- Dealing with models and abstraction
 - model-based development: UML, MDA, Simulink/Matlab
- Promises better, faster, cheaper testing
 - algorithmic generation of tests and test oracles: tools
 - maintenance of tests through model modification

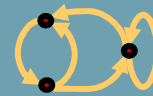
Model-Based Testing (MBT)



MBT : Black-Box Testing of Functionality



Evolution of Testing



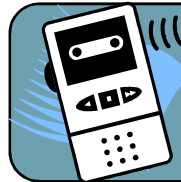
Model-Based Testing

keyword	parameters
customer	Jan Pieters
price	€ 20.45
number	3

Keyword-Driven



Scripted



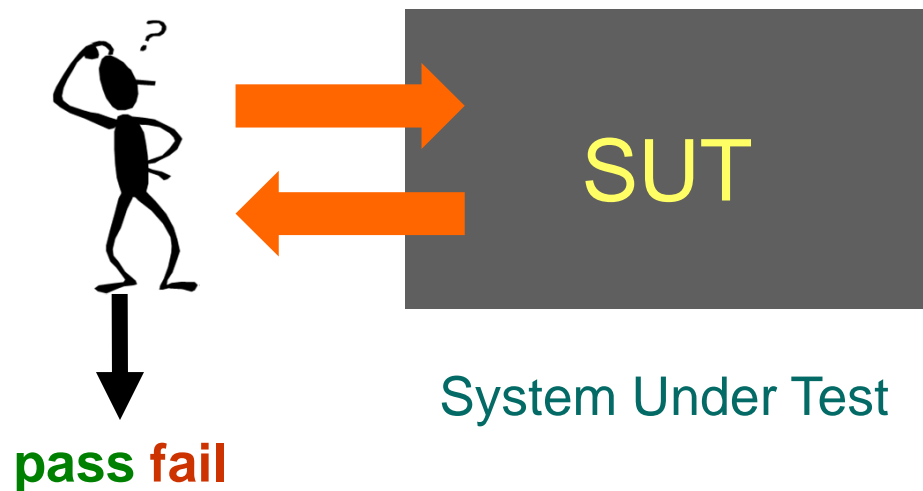
Record & Playback



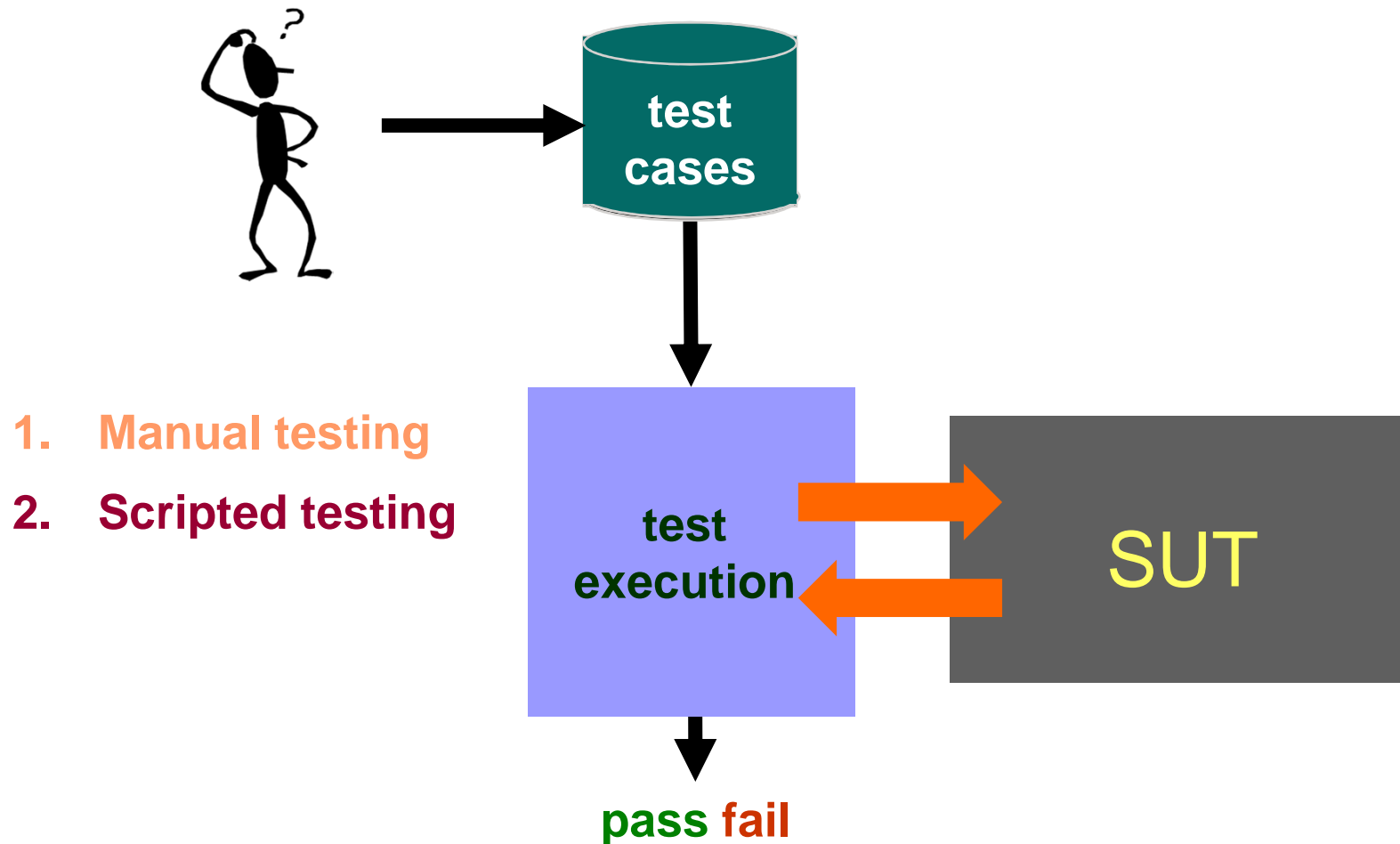
Manual Testing

Testing 1 : Manual Testing

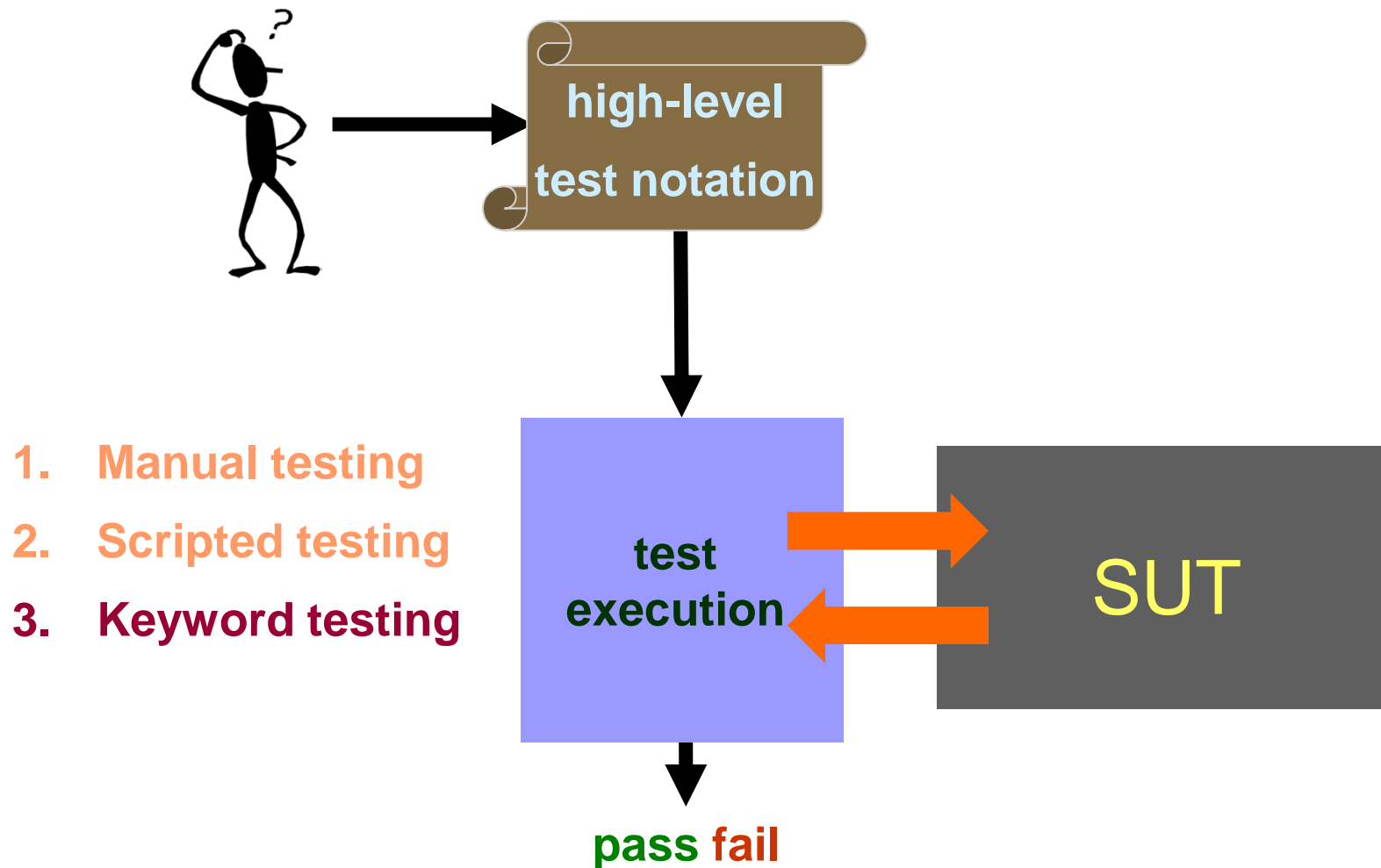
1. Manual testing



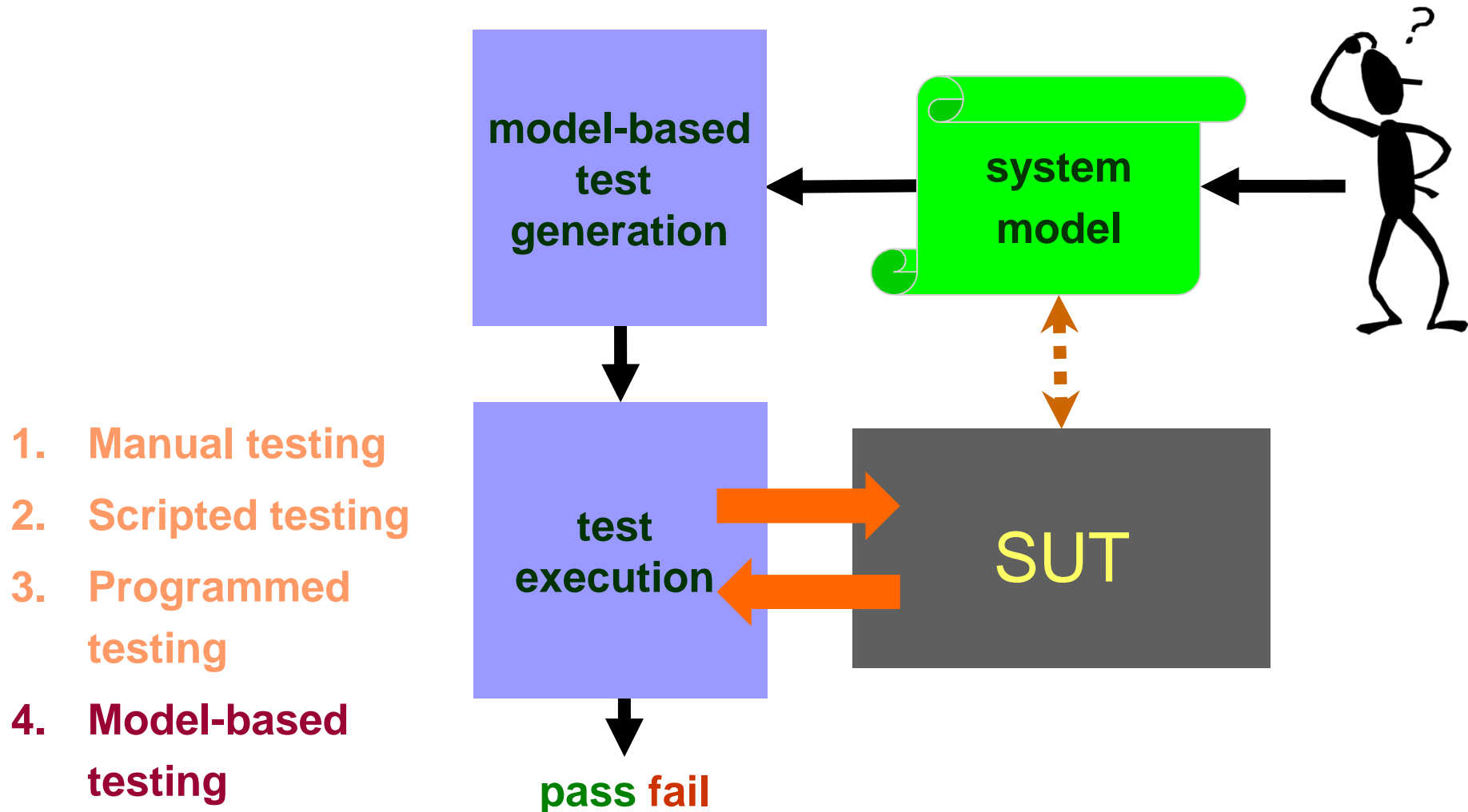
Testing 2 : Scripted Testing



Testing 3 : Keyword-Driven Testing

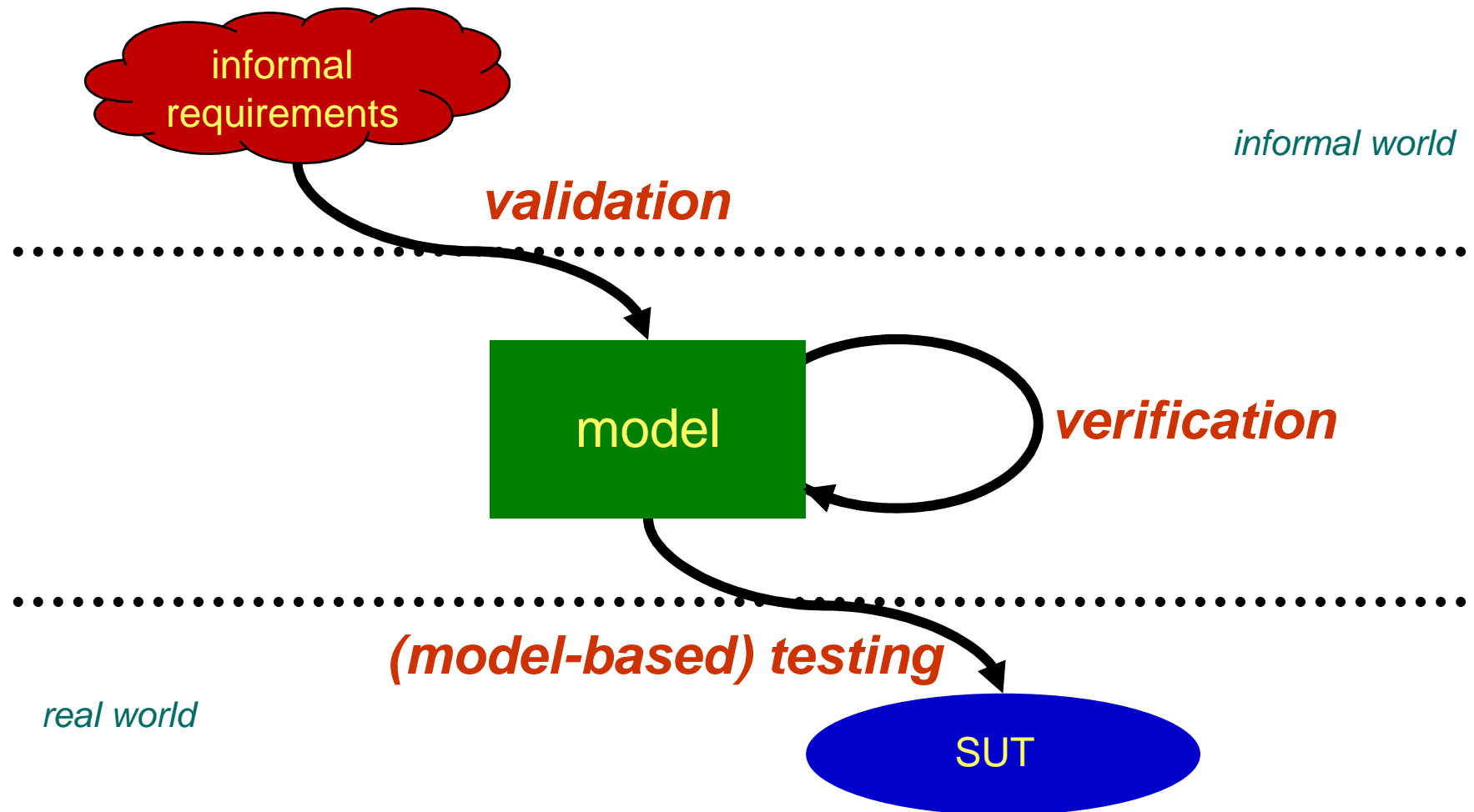


Testing 4 : Model-Based Testing



Model-Based Verification, Validation, Testing,

Validation, Verification, and Testing



Verification and Testing

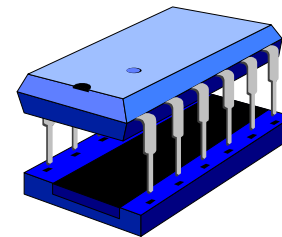
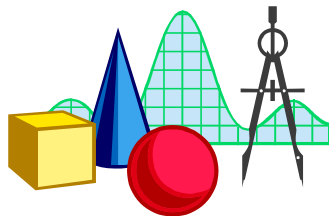
Model-based verification :

- formal manipulation
- prove properties
- performed on model

Model-based testing :

- experimentation
- show error
- concrete system

*formal
world*



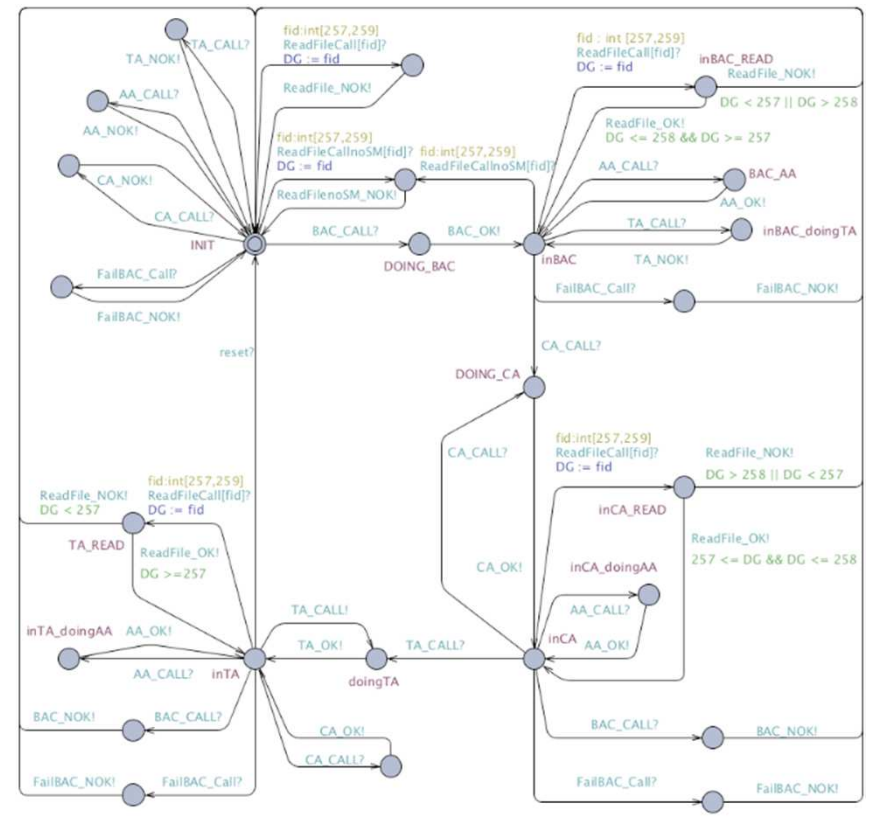
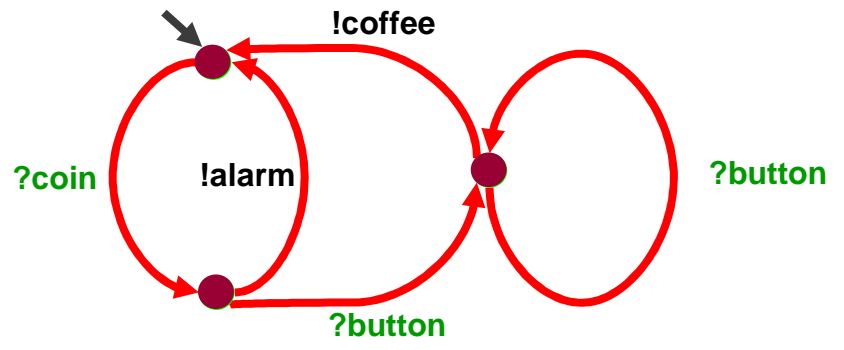
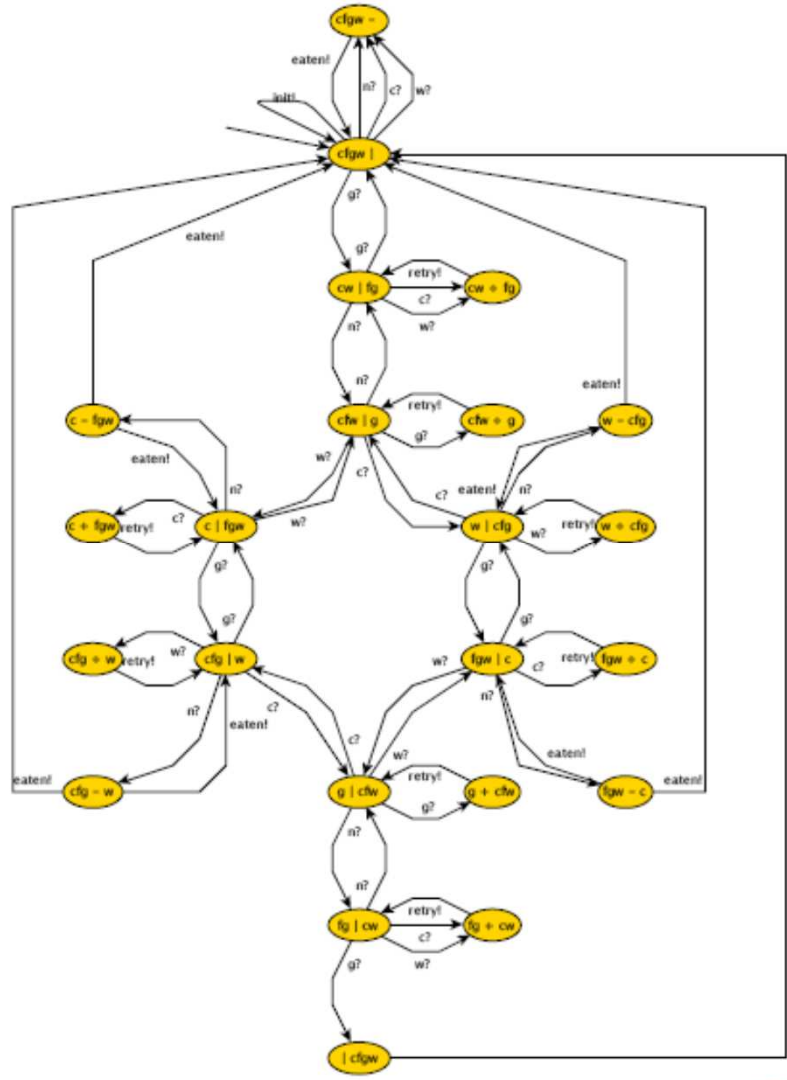
*concrete
world*

Verification is only as good as
the validity of the model on
which it is based

Testing can only show the
presence of errors, not their
absence

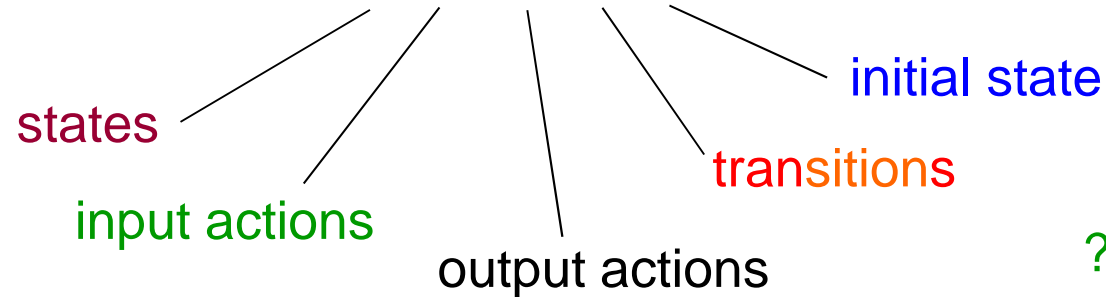
Models

Models

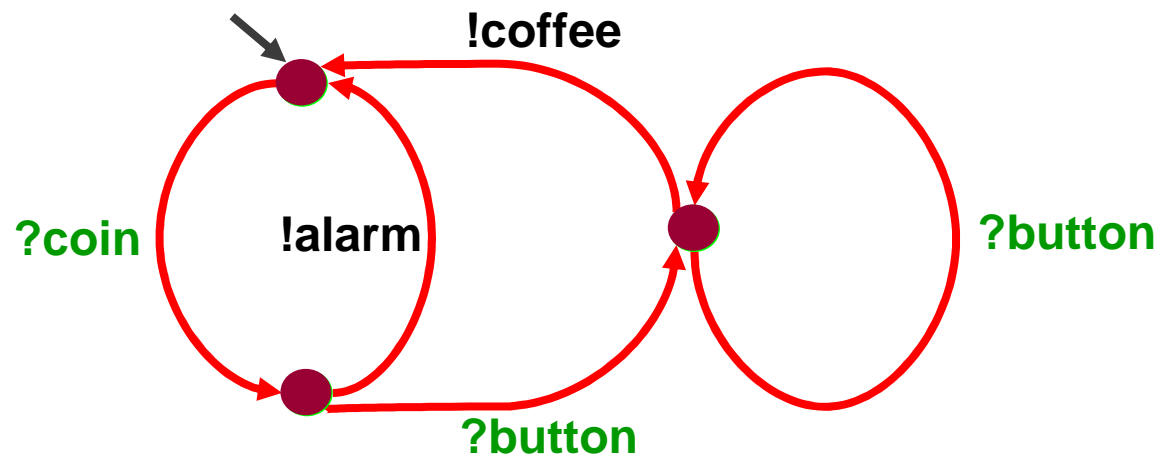


Models: Labelled Transition Systems

Labelled Transition System: $\langle S, L_i, L_o, T, s_0 \rangle$

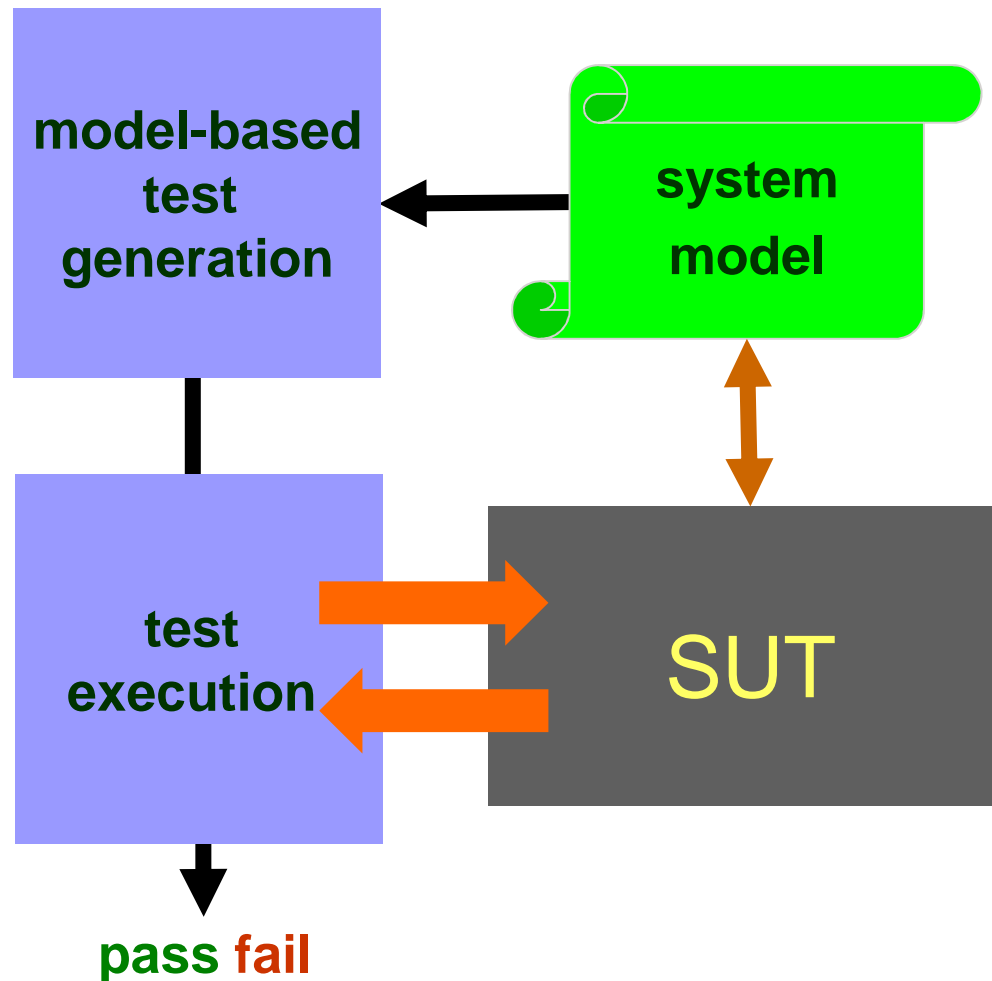


? = input
! = output

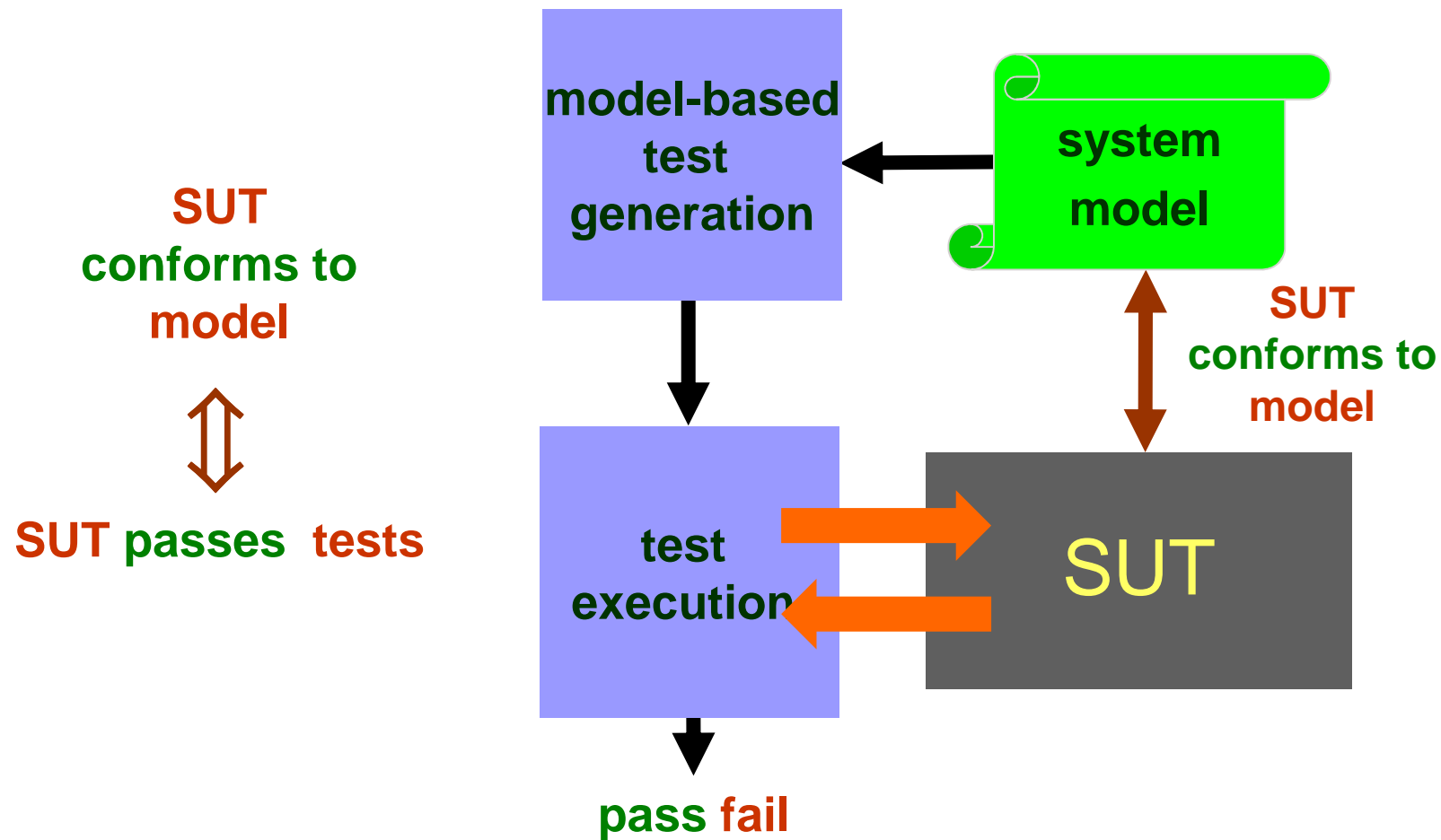


A Theory of Model-Based Testing with Labelled Transition Systems

Model-Based Testing

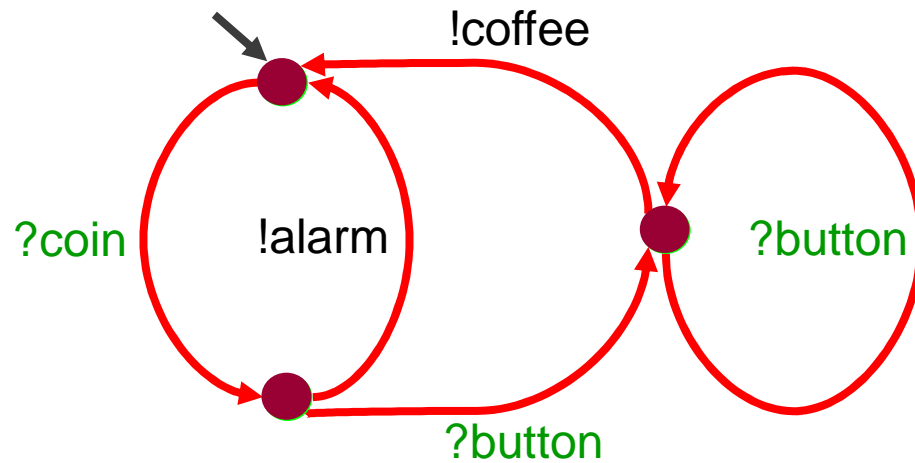


MBT : Validity

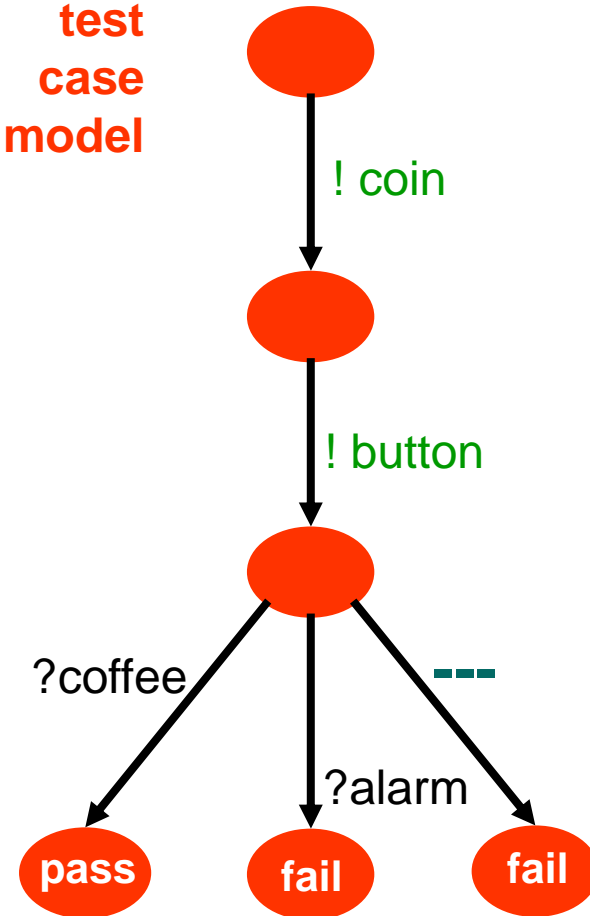


Models: Generation of Test Cases

specification
model

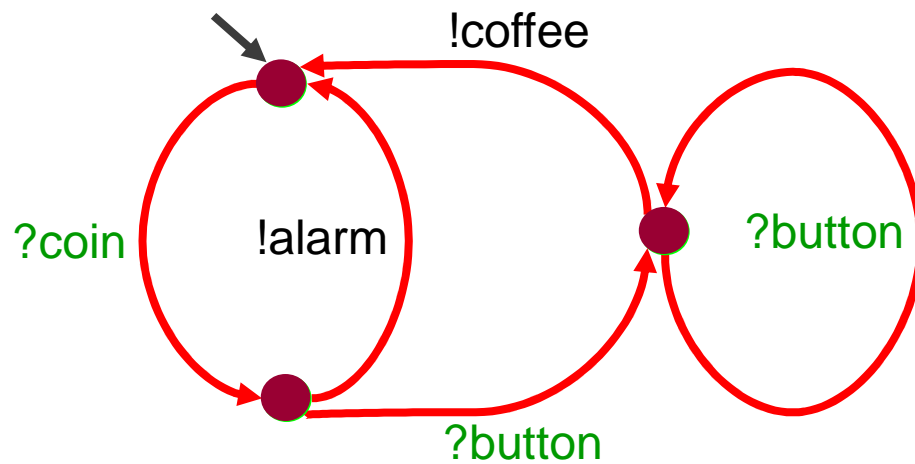


test
case
model

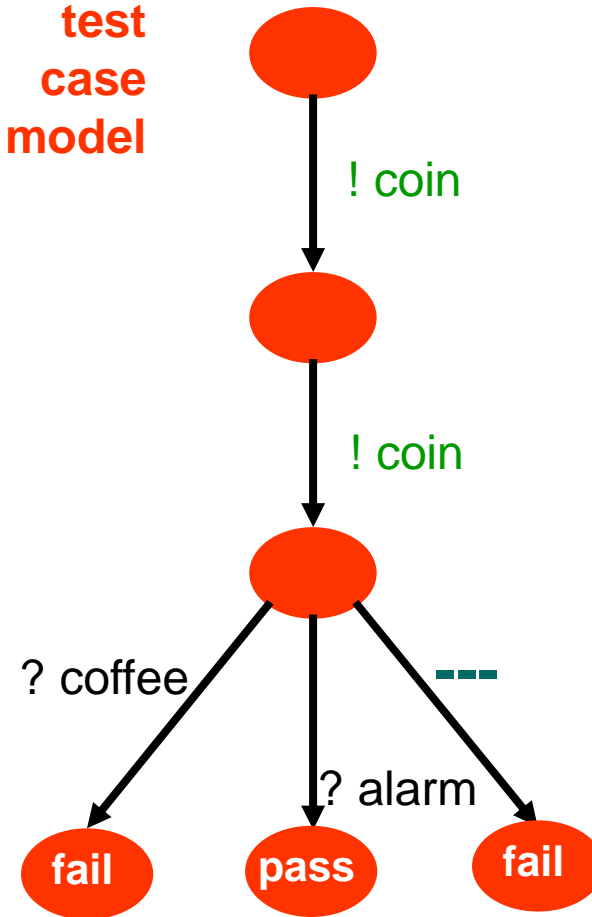


Models: Generation of Test Cases

specification
model



test
case
model



MBT : Abstract from Scheduling Details

- Four components in parallel, in any order

task(start?, ready!)



taskA := task (startA?, readyA!)

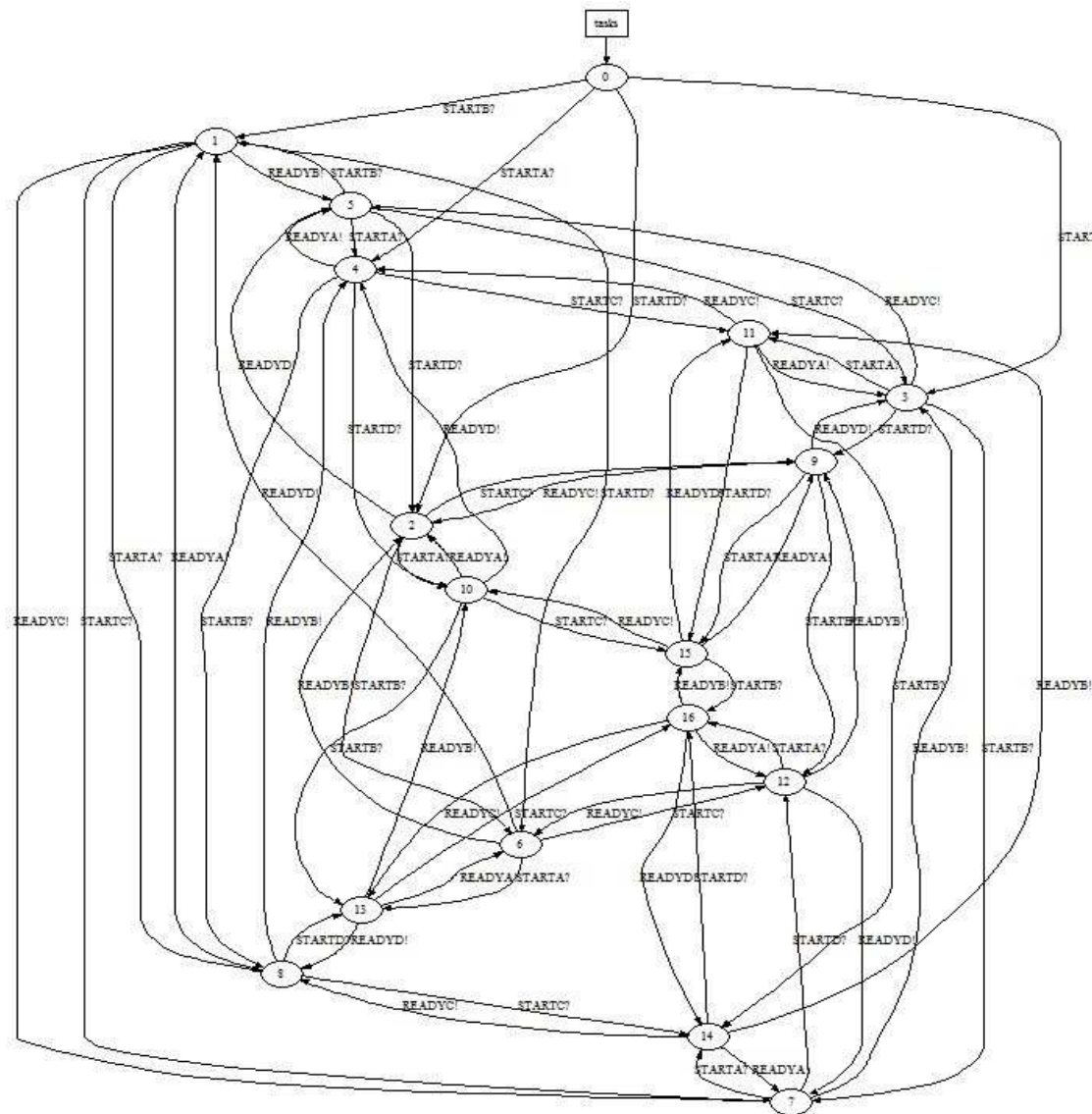
taskB := task (startB?, readyB!)

taskC := task (startC?, readyC!)

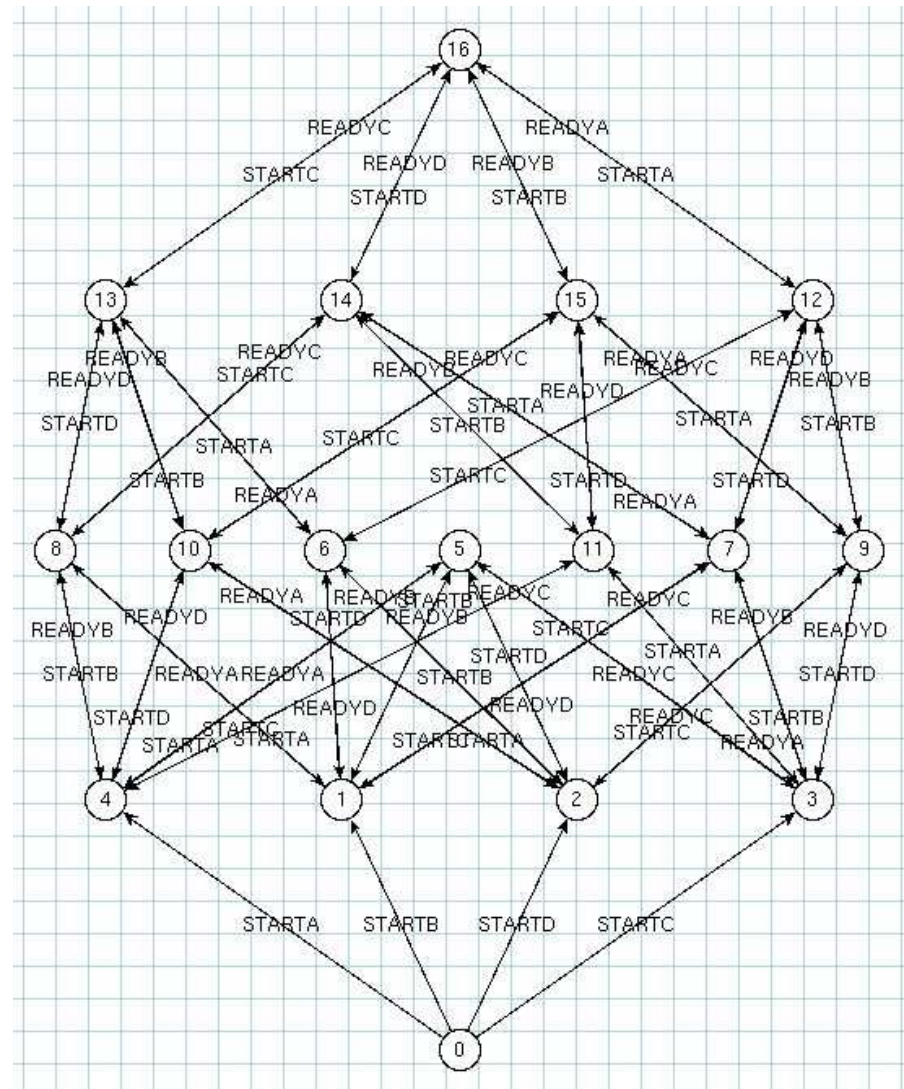
taskD := task (startD?, readyD!)

model := taskA ||| taskB ||| taskC ||| taskD

MBT : Abstract from Scheduling Details

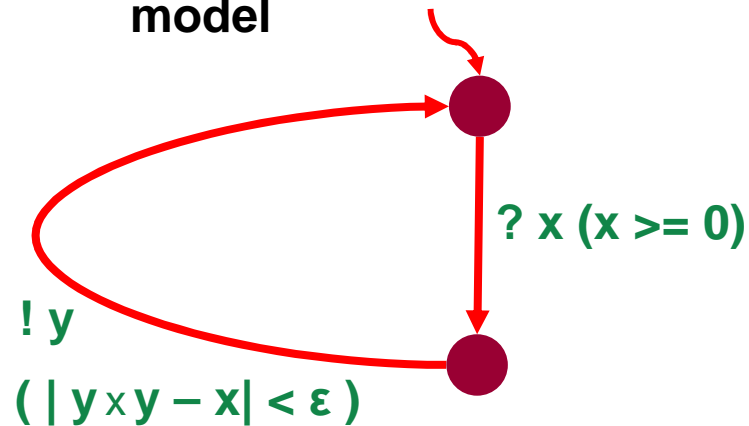


MBT : Abstract from Scheduling Details

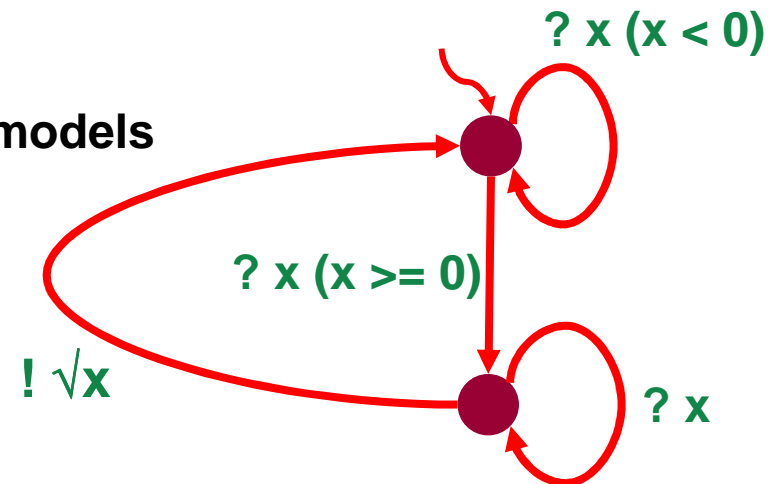


MBT : Nondeterminism, Underspecification

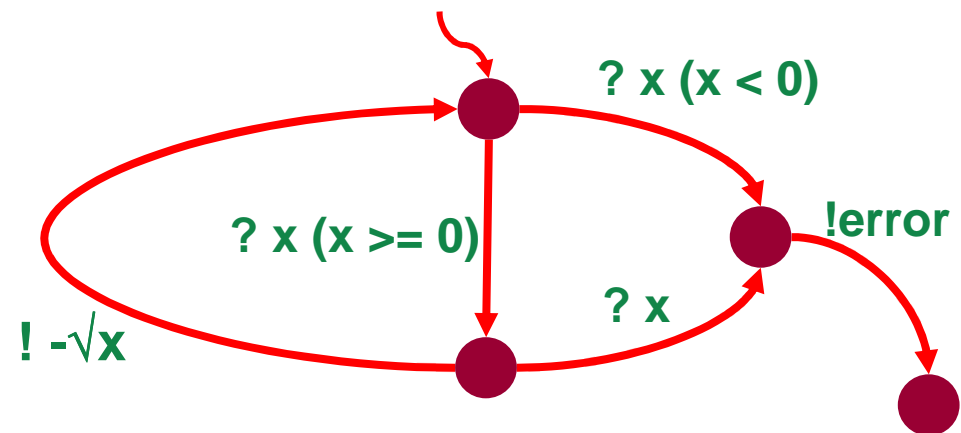
specification
model



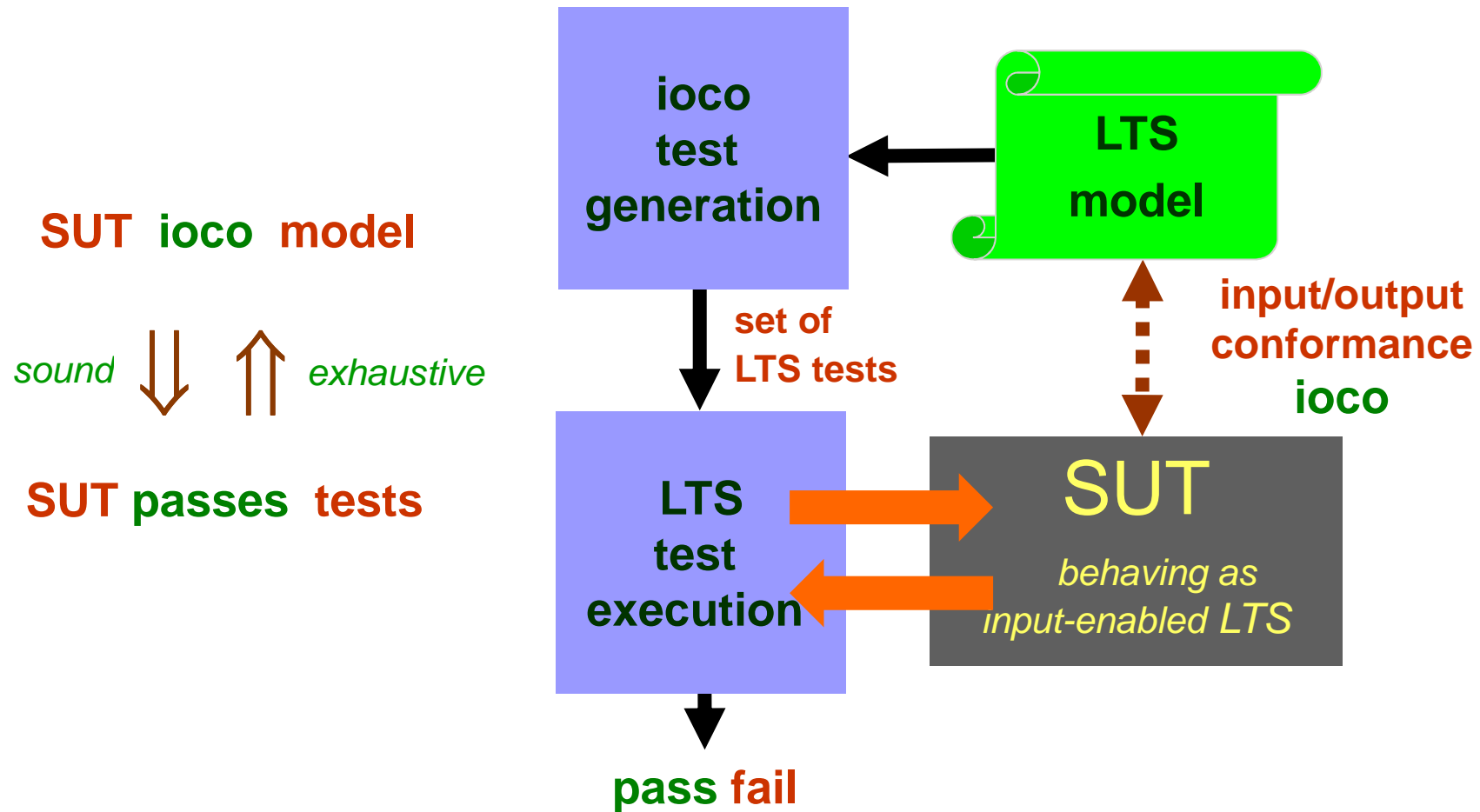
SUT models



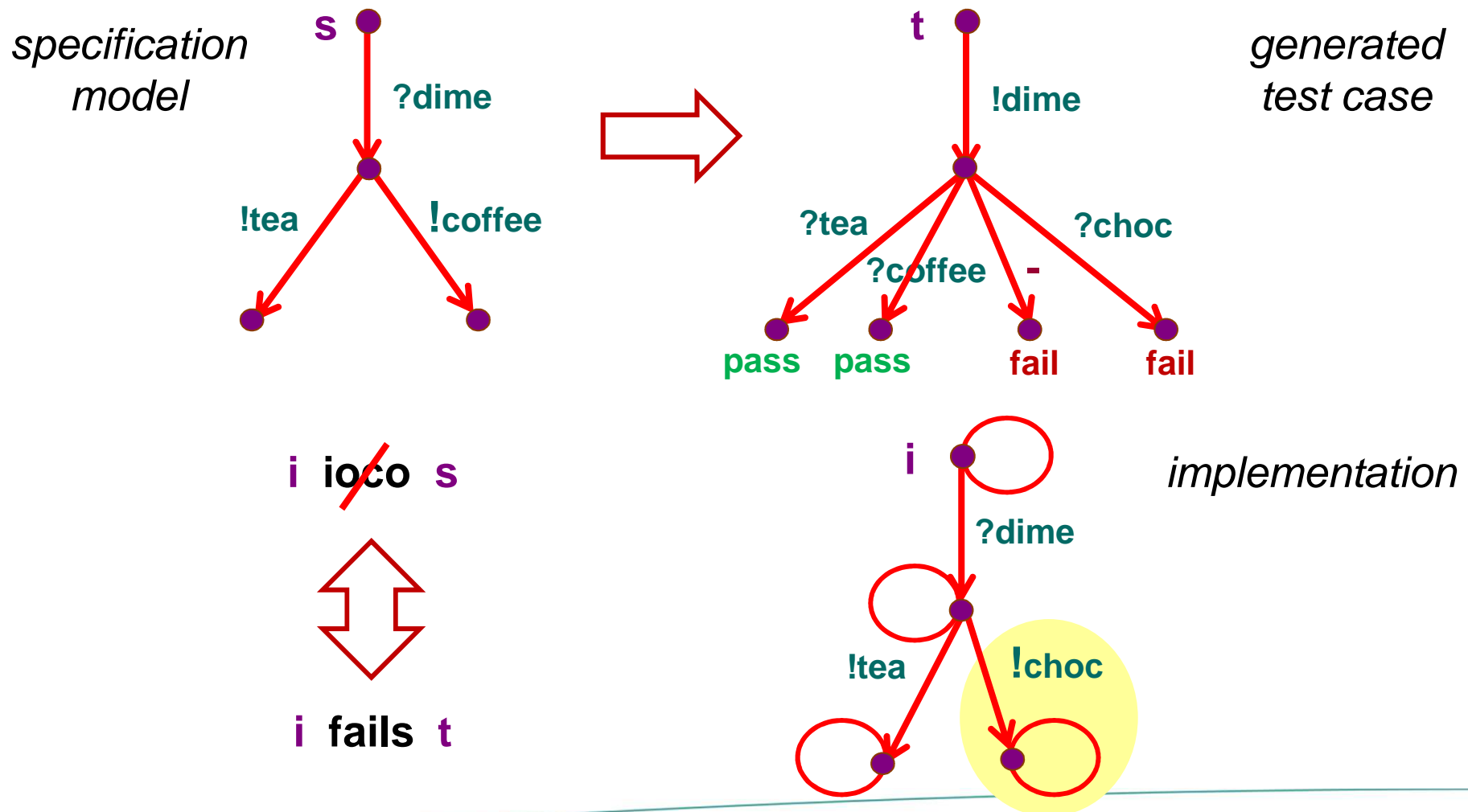
- non-determinism
- under-specification
- specification of properties rather than construction



MBT with LTS and ioco



MBT : Argue about Validity of Tests



Model-Based Testing with Labelled Transition Systems

There is Nothing More Practical
than a Good Theory

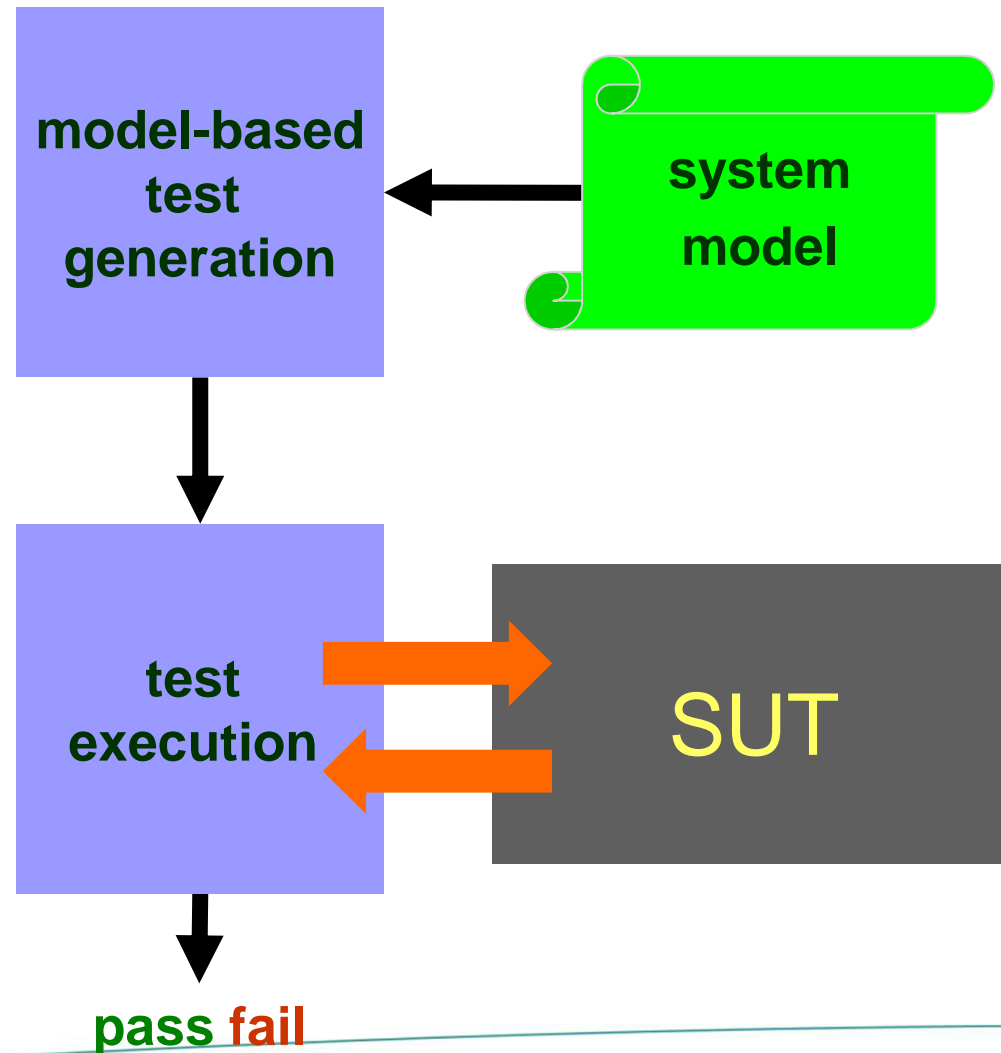
Overview

- MBT: Tools
- MBT: Under-specification
- MBT: Test selection
- MBT: Towards test selection for ioco
- Refinement for ioco
- Test-based modelling = Automata learning

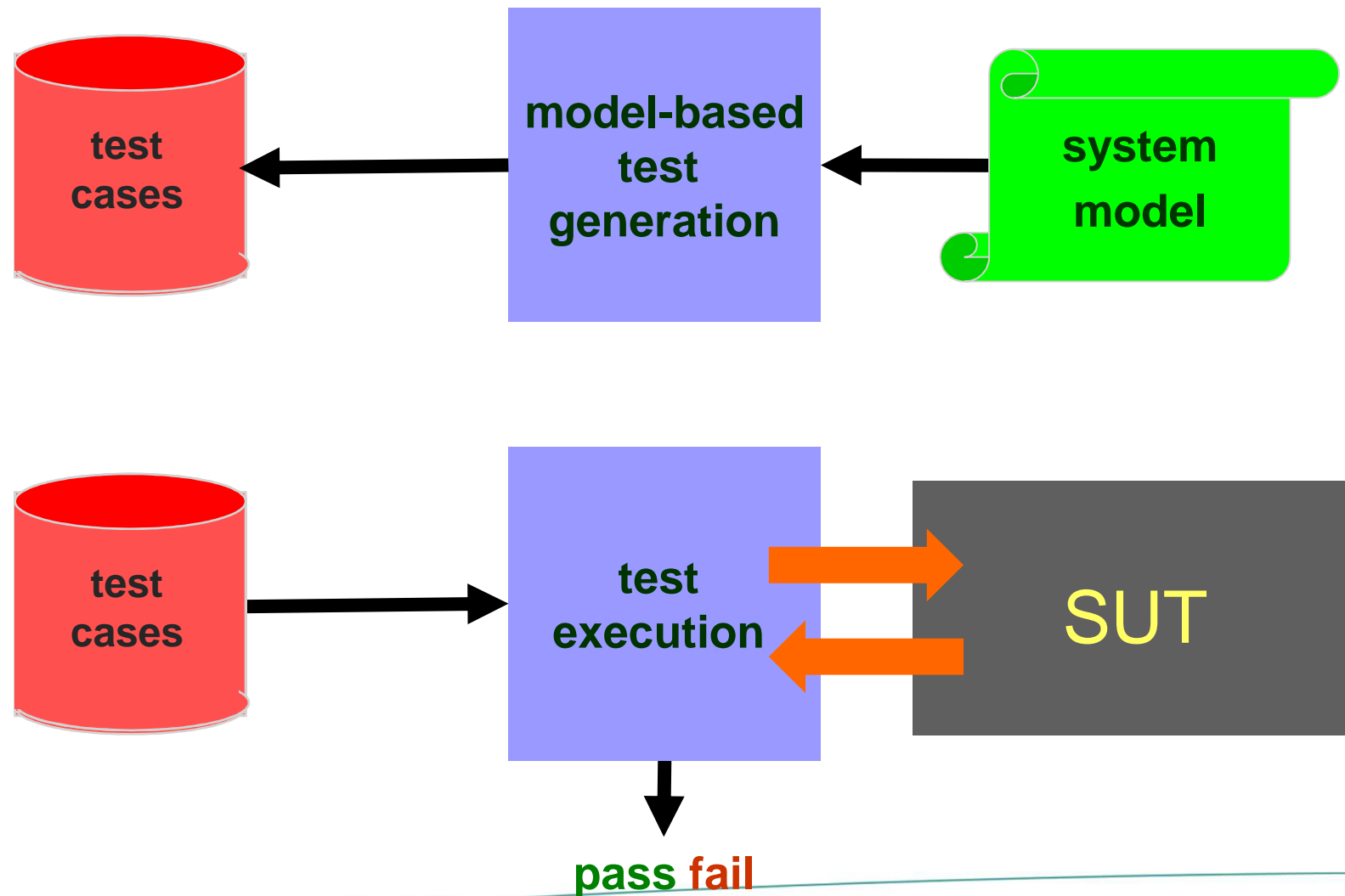
Model-Based Testing

Tools

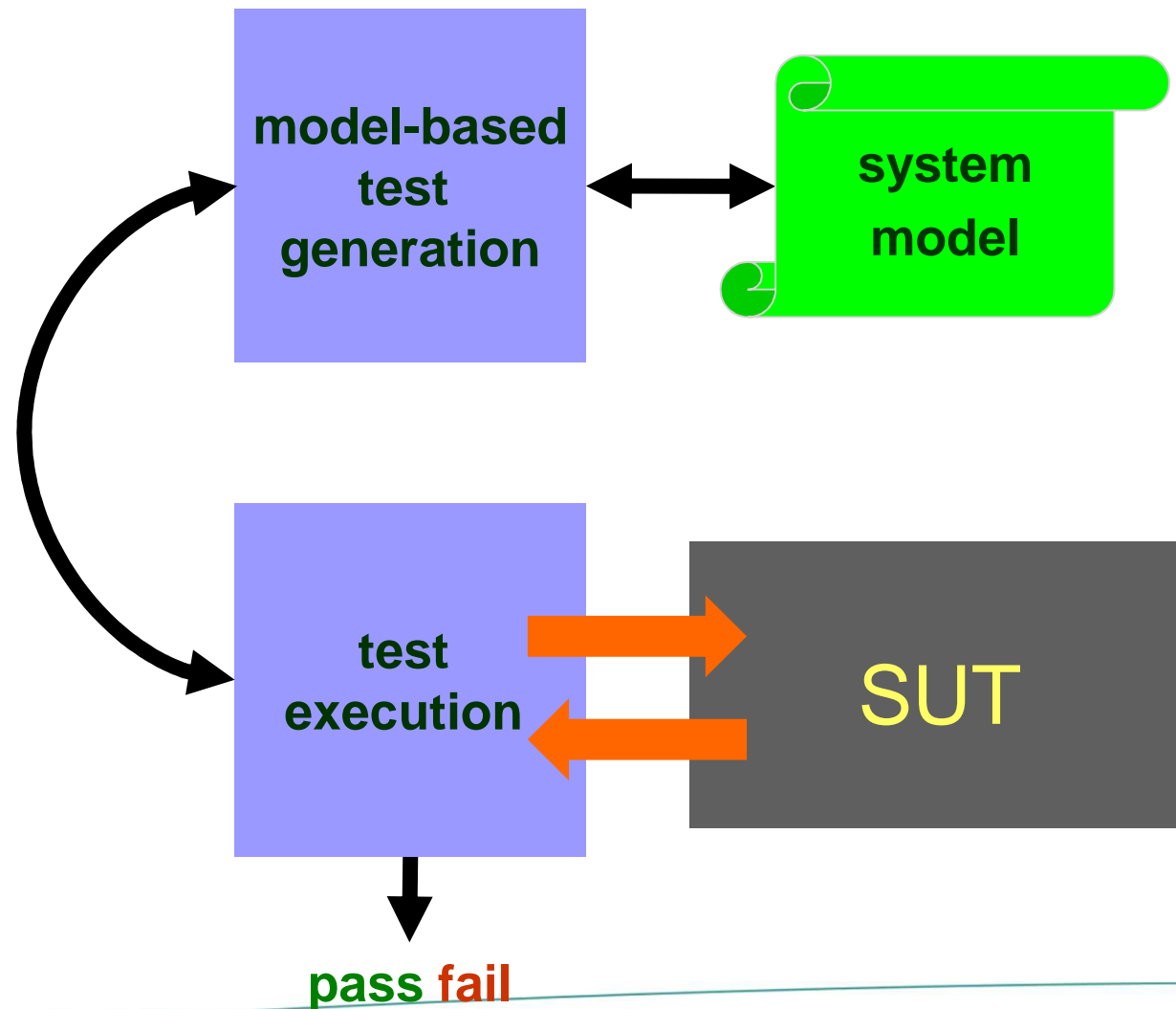
MBT : Off-Line - On-Line



MBT : Off-Line = Batch



MBT : On-Line = On-the-Fly



Model-Based Testing : Variations for Underspecification

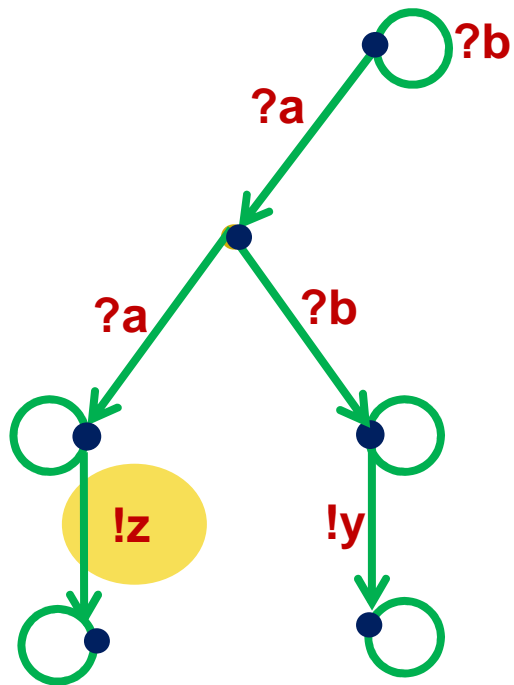
Variations on a Theme

- $i \text{ ioco } s \Leftrightarrow \forall \sigma \in \text{Straces}(s) : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$
- $i \leq_{\text{iOr}} s \Leftrightarrow \forall \sigma \in (L \cup \{\delta\})^* : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$
- $i \text{ iocnf } s \Leftrightarrow \forall \sigma \in \text{traces}(s) : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$
- $i \text{ ioco}_F s \Leftrightarrow \forall \sigma \in F : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$
- $i \text{ uioco } s \Leftrightarrow \forall \sigma \in \text{Utraces}(s) : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$
- $i \text{ mioco } s$ multi-channel ioco
- $i \text{ wioco } s$ non-input-enabled ioco
- $i \text{ eco } e$ environmental conformance
- $i \text{ sioco } s$ symbolic ioco
- $i \text{ (r)tioco } s$ (real) timed tioco (Aalborg, Twente, Grenoble, Bordeaux,.....)
- $i \text{ rioco } s$ refinement ioco
- $i \text{ hioco } s$ hybrid ioco
- $i \text{ qioco } s$ quantified ioco
- $i \text{ poco } s$ partially observable game ioco
- $i \text{ stioco}_D s$ real time and symbolic data
-

Underspecification: ioco and uioco

$$i \text{ ioco } s \quad =_{\text{def}} \quad \forall \sigma \in \text{Straces}(s) : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$$

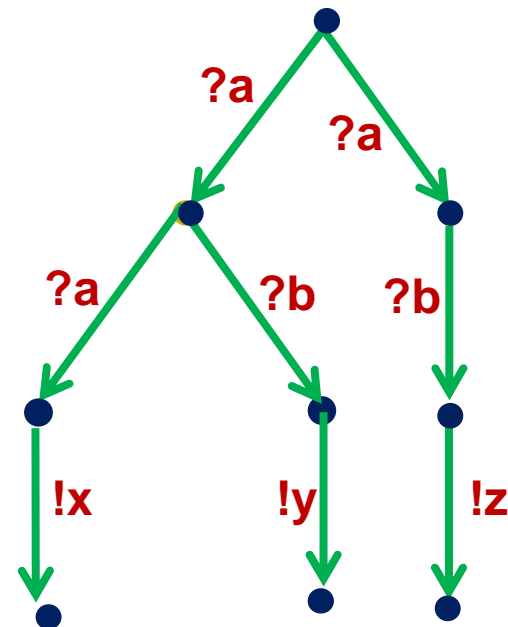
Implementation *i*



~~*i ioco s*~~

i uioco s

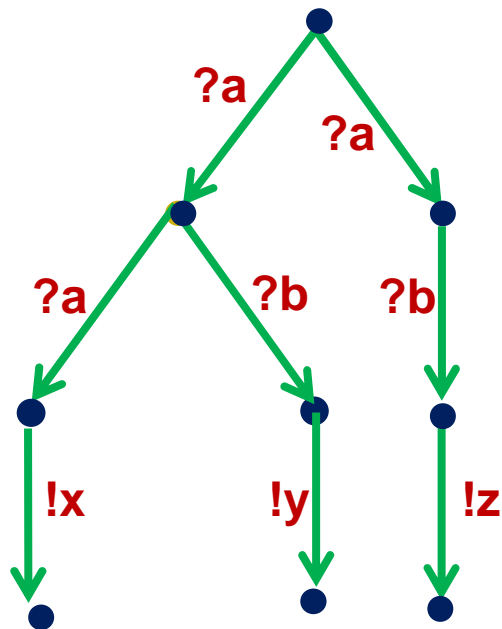
Specification *s*



Underspecification: uioco

$i \text{ ioco } s \stackrel{\text{def}}{=} \forall \sigma \in \text{Straces}(s) : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$

$i \text{ uioco } s \stackrel{\text{def}}{=} \forall \sigma \in \text{Utraces}(s) : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$



$\text{Utraces}(s) =$

$\{ \sigma \in \text{Straces}(s) \mid$

$\forall \sigma_1 \text{ ?b } \sigma_2 = \sigma :$

$s \text{ after } \sigma_1 \text{ must ?b } \}$

$?a ?a \in \text{Straces}(s)$

$?a ?a \notin \text{Utraces}(s)$

$\text{ioco} \subset \text{uioco}$

Test Selection in Model-Based Testing

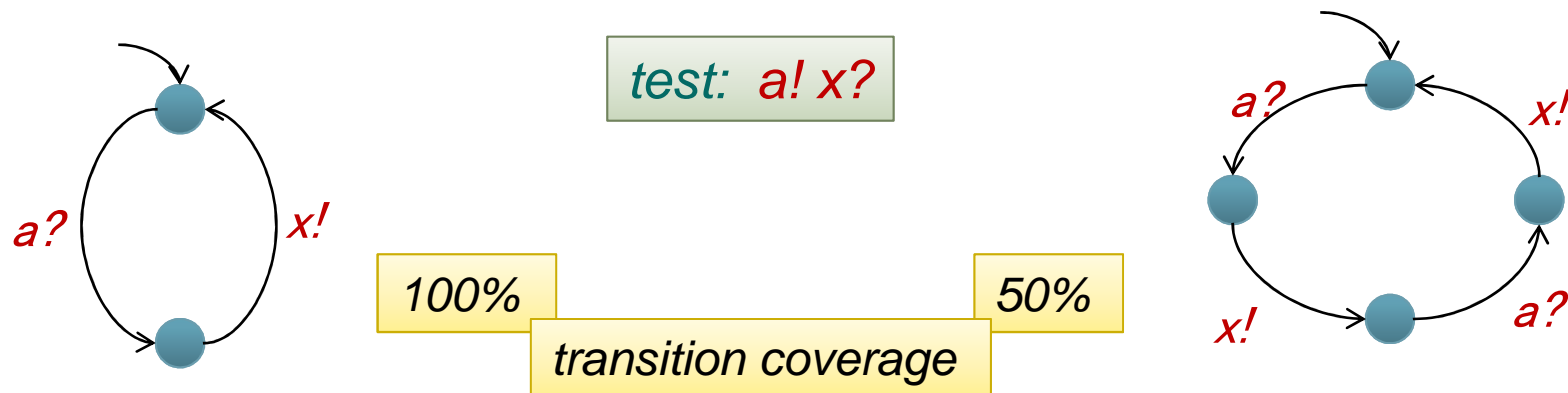
Test Selection

- Exhaustiveness never achieved in practice
- Test selection = select subset of exhaustive test suite, to achieve confidence in quality of tested product
 - select best test cases capable of detecting failures
 - measure to what extent testing was exhaustive : *coverage*
- Optimization problem

best possible testing ↔ *within cost/time constraints*

Test Selection: Approaches

1. random
2. domain / application specific: test purposes, test goals, ...
3. model / code based: coverage
 - usually structure based



Towards Test Selection in the ioco Framework

Test Selection for **uioco**

$$i \text{ uioco } s \stackrel{\text{def}}{=} \forall \sigma \in \text{Utraces}(s) : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$$

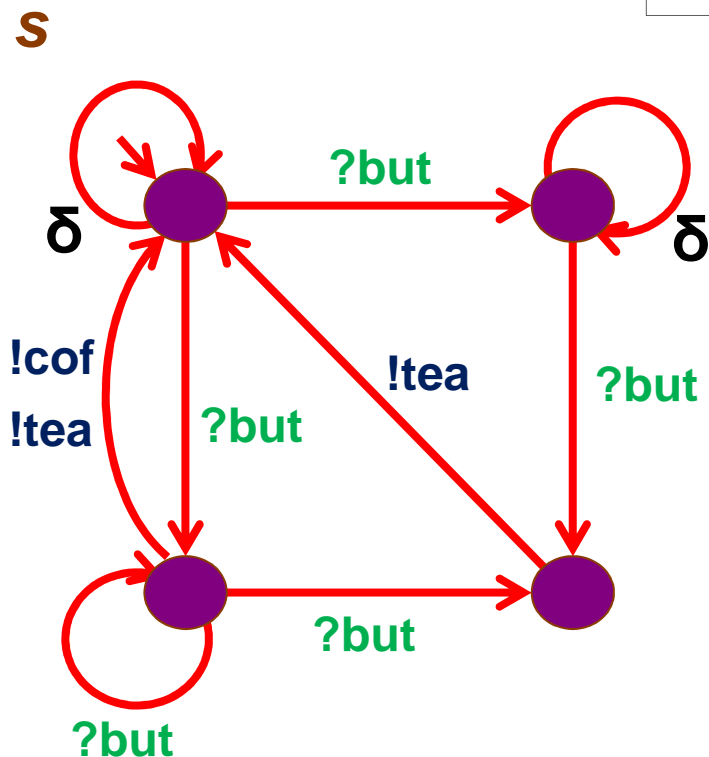
Selection of Sub-Set of UTraces

- Select: $M \subset \text{Utraces}(s)$
- Test for: $i \text{ uioco}_M s$
 $\Leftrightarrow \forall \sigma \in M : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$
- Coverage: $\frac{\# M}{\# \text{Utraces}(s)}$

Test Selection for **uioco**

$$out(s \text{ after } ?but \delta \delta ?but) = out(s \text{ after } ?but \delta ?but)$$

*i.e. if already tested for ?but δ ?but
what does testing for ?but δ δ ?but add ?*



$$out(s \text{ after } ?but) = \{ !cof, !tea, \delta \}$$

*i.e. everything is allowed -
what shall be tested then ?*

**The set *Utraces* is not minimal,
i.e., elements are dependent**

Test Selection for uioco

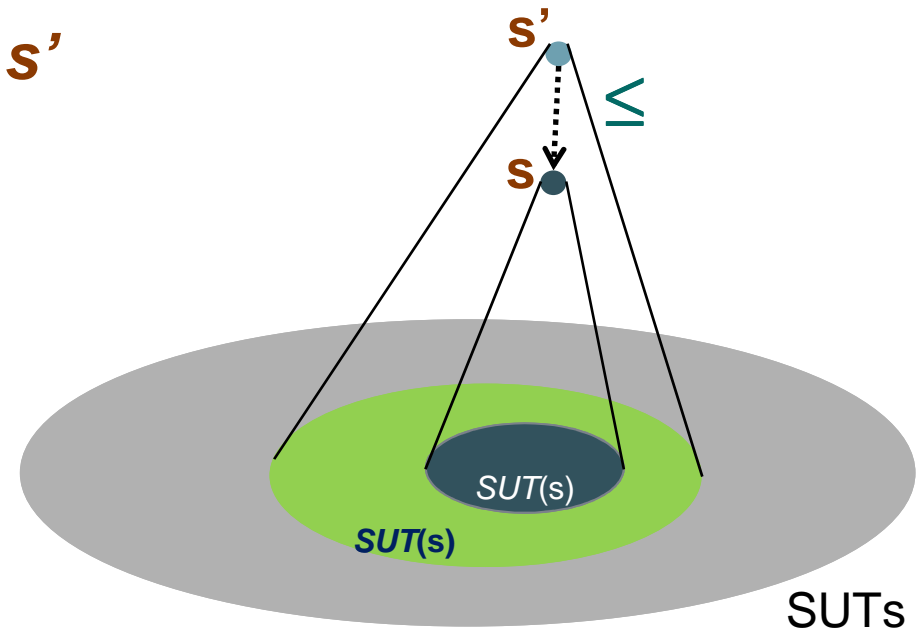
$$i \text{ uioco } s \stackrel{\text{def}}{=} \forall \sigma \in \text{Utraces}(s) : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$$

Take *weaker* specification s'
= inverse of refinement

$$s \leq s'$$

$$\Leftrightarrow \text{SUT}(s) \subseteq \text{SUT}(s')$$

$$\Leftrightarrow \{i \mid i \text{ uioco } s\} \subseteq \{i \mid i \text{ uioco } s'\}$$

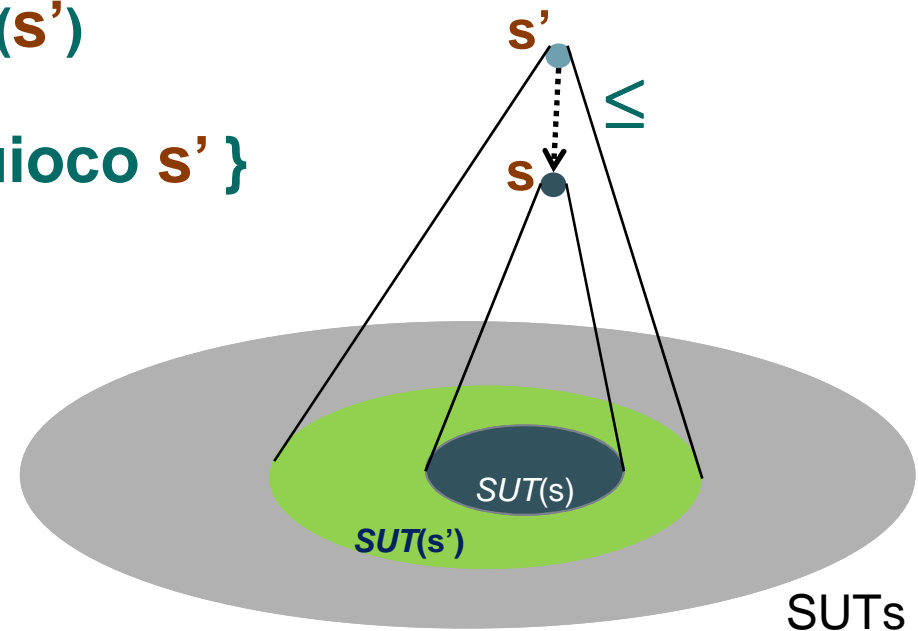


Test Selection for uioco

$$i \text{ uioco } s \quad =_{\text{def}} \quad \forall \sigma \in \text{Utraces}(s) : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$$

$$s \leq s' \quad \Leftrightarrow \quad \text{SUT}(s) \subseteq \text{SUT}(s')$$

$$\Leftrightarrow \{ i \mid i \text{ uioco } s \} \subseteq \{ i \mid i \text{ uioco } s' \}$$



Coverage: $\frac{\# \text{SUT}(s)}{\# \text{SUT}(s')}$

Test Selection: Lattice of Specifications

S_1 is stronger than $S_2 \iff$

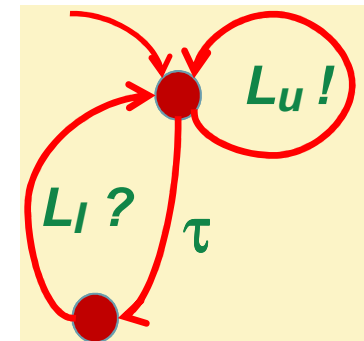
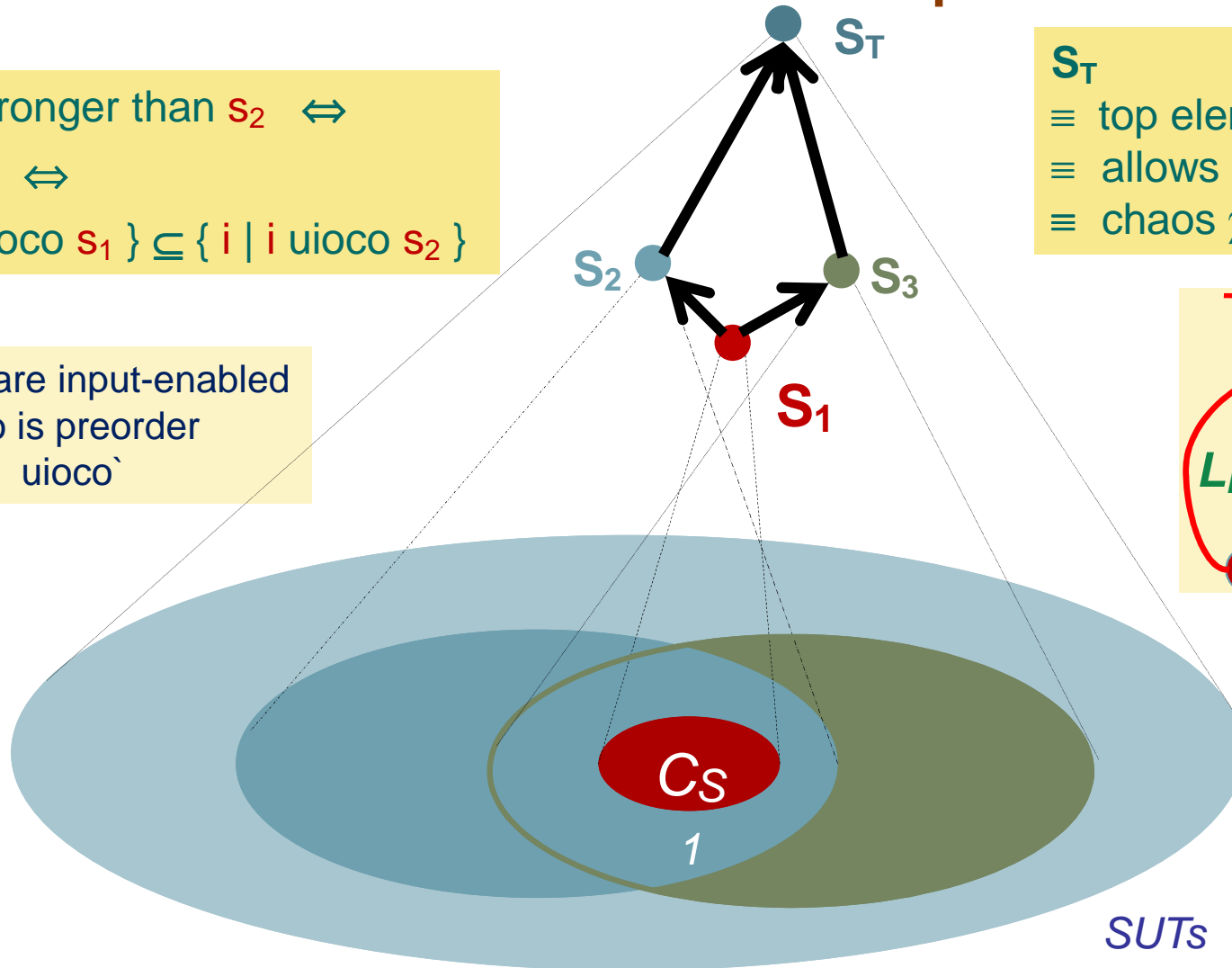
$S_1 \leq S_2 \iff$

$\{i \mid i \text{ uioco } S_1\} \subseteq \{i \mid i \text{ uioco } S_2\}$

if specs are input-enabled
then ioco is preorder
then $\leq \equiv \text{uioco}$

S_T

\equiv top element
 \equiv allows any impl.
 \equiv chaos χ

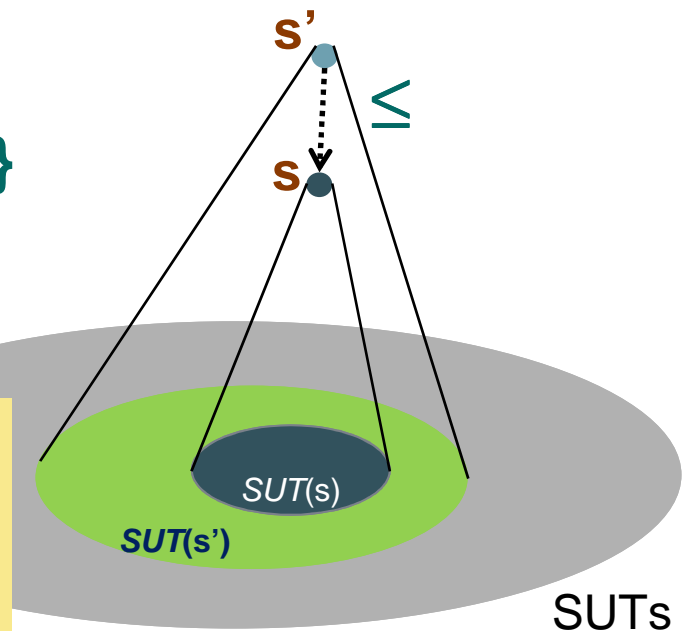


Test Selection for uioco

$$i \text{ uioco } s \stackrel{\text{def}}{=} \forall \sigma \in \text{Utraces}(s) : \text{out}(i \text{ after } \sigma) \subseteq \text{out}(s \text{ after } \sigma)$$

$$s \leq s' \Leftrightarrow \text{SUT}(s) \subseteq \text{SUT}(s')$$

$$\Leftrightarrow \{i \mid i \text{ uioco } s\} \subseteq \{i \mid i \text{ uioco } s'\}$$



Requires refinement preorder
 \leq on specifications.

ioco / uioco are not refinement
preorders and are only defined for
input-enabled implementations

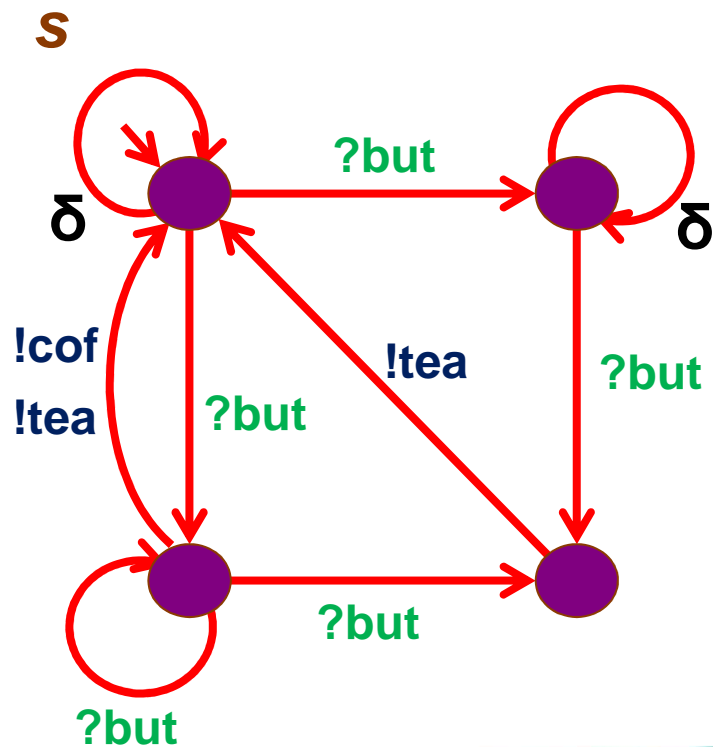
Set of Required Traces

$$Rtraces(s) =_{\text{def}} \{ \sigma \in \underline{Utraces}(s) \mid$$

δ is not a substring of σ ,

σ does not end with δ ,

$out(s \text{ after } \sigma) \neq L_U \cup \{ \delta \} \}$



?but δ δ ?but
?but
 δ

$\notin \underline{Rtraces}(s)$

$\in \underline{Utraces}(s)$

Set of Required Traces

Rtraces throw away superfluous traces, and only those

1. For input enabled implementations:

$$\begin{aligned} \mathbf{i} \text{ uioco } \mathbf{s} &=_{\text{def}} \forall \sigma \in \mathbf{Utraces}(\mathbf{s}) : \text{out}(\mathbf{i} \text{ after } \sigma) \subseteq \text{out}(\mathbf{s} \text{ after } \sigma) \\ &\iff \forall \sigma \in \mathbf{Rtraces}(\mathbf{s}) : \text{out}(\mathbf{i} \text{ after } \sigma) \subseteq \text{out}(\mathbf{s} \text{ after } \sigma) \end{aligned}$$

2. ***Rtraces*** is “minimal” : For $\mathbf{A} \subset \mathbf{Rtraces}(\mathbf{s})$ and $\mathbf{A} \neq \mathbf{Rtraces}(\mathbf{s})$,
there exists an input-enabled \mathbf{i} such that

$$\forall \sigma \in \mathbf{A} : \text{out}(\mathbf{i} \text{ after } \sigma) \subseteq \text{out}(\mathbf{s} \text{ after } \sigma)$$

and ~~$\mathbf{i} \text{ uioco } \mathbf{s}$~~

From Required Traces to **wioco**

Refinement preorder \leq is given by **wioco**,
considering superfluous traces and non-input enabledness

$s \text{ wioco } s' \quad =_{\text{def}} \quad \forall \sigma \in Rtraces(s') :$

1. $out(s \text{ after } \sigma) \subseteq out(s' \text{ after } \sigma)$
2. $\forall \sigma_1 \leq \sigma : in(s \text{ after } \sigma_1) \supseteq Rin(s' \text{ after } \sigma_1)$

$in(s \text{ after } \sigma_1) \quad =_{\text{def}} \quad \{ a? \in L_I \mid s \text{ after } \sigma_1 \text{ must } a? \}$

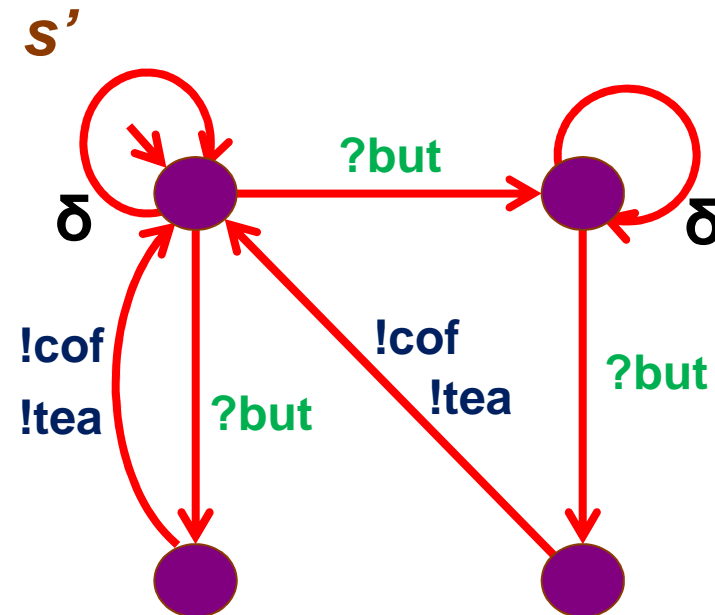
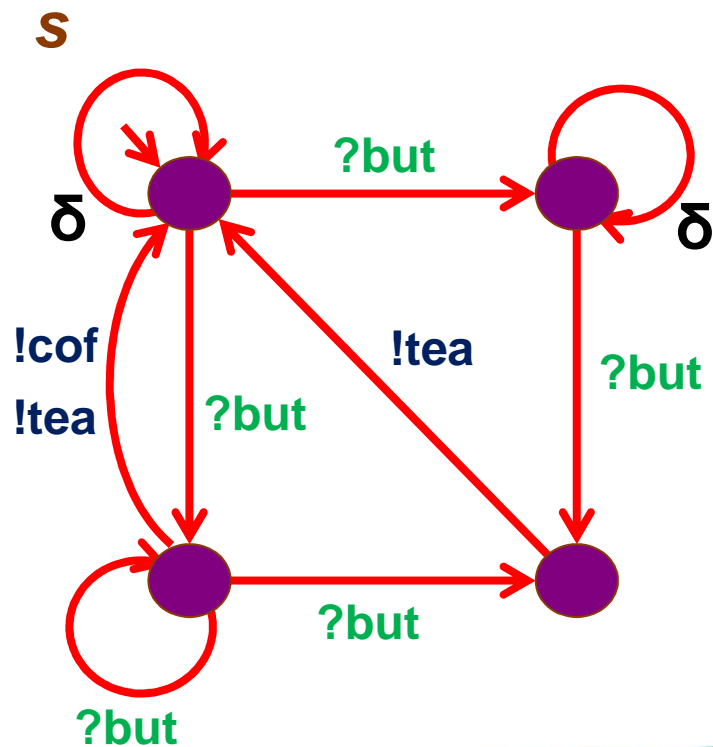
$Rin(s' \text{ after } \sigma_1) \quad =_{\text{def}}$

$\{ a? \in in(s \text{ after } \sigma_1) \mid \exists \sigma_2 \in Rtraces(s') : \sigma_1 a? \leq \sigma_2 \}$

A Weaker Specification through **wioco**

$$s \text{ wioco } s' \iff SUT(s) \subseteq SUT(s')$$

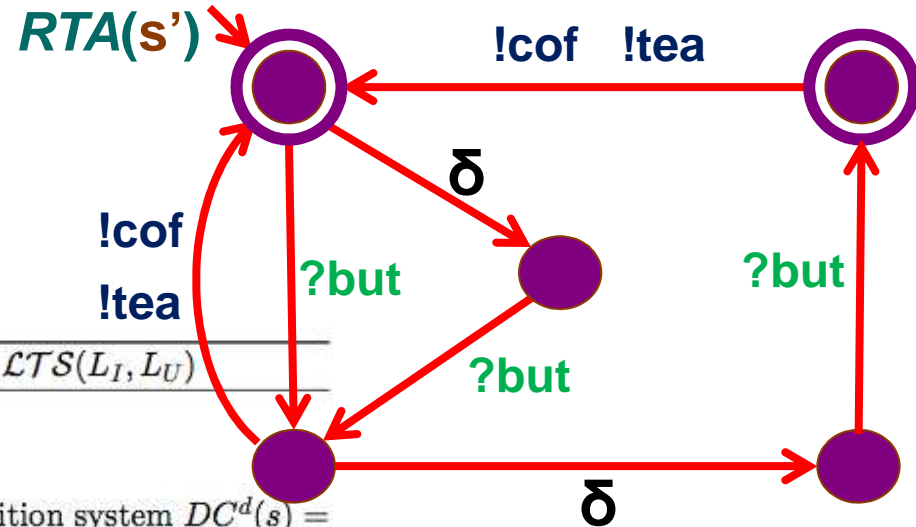
- s' is a weaker than s :
- remove inputs
 - add outputs



Required Traces Automaton

$\sigma \in Rtraces(s)$

$\Leftrightarrow \sigma$ accepted by $RTA(s)$



Algorithm 1 Find the required traces automaton of $s \in LTS(L_I, L_U)$

- 1: add loops $s \xrightarrow{\delta} s$ for all quiescent states
- 2: build $DC(s)$, the demonic completion of s
- 3: determinize $DC(s)$ obtaining a new input-output transition system $DC^d(s) = \langle Q, L_I, L_U, T, q_0 \rangle$
- 4: **for each** $q \in Q$ **do**
- 5: **if** $(out(q) \neq L_U \cup \delta) \wedge (\exists p \mid p \xrightarrow{\lambda} q \wedge \lambda \neq \delta \wedge \lambda \neq \tau)$ **then** mark q as accepting
- 6: **for each** $q \in Q$ **do**
- 7: **if** q is trace equivalent to chaos state χ **then** mark q as *chaotic*
- 8: remove all *chaotic* states from Q
- 9: **for each** $(q, \delta, q_1) \in T$ **do**
- 10: add a new state p to Q { δ sequences optimization steps 1 and 2}
- 11: add (q, δ, p) to T
- 12: **for each** $a \in L_I$ such that $q_1 \xrightarrow{a} q_2$ **do**
- 13: add (p, a, q_2) to T {if s is a valid labelled transition system then $out(q) \not\subseteq L_U$ }
- 14: remove (q, δ, q_1) from T

MBT : Some Tools - ioco

- AETG
- Agatha
- Agedis
- All4Tec MaTeLo
- Autolink
- Axini Test Manager
- Conformiq Qtronic
- Cooper
- G \forall st
- Gotcha
- JTorX
- NModel
- ParTeG
- Phact/The Kit
- QuickCheck
- Reactis
- RT-Tester
- SaMsTaG
- SeppMed MBTsuite
- Smartesting CertifyIt
- Spec Explorer
- Statemate
- STG
- TestGen (Stirling)
- TestGen (INT)
- TestComposer
- TGV
- TorX
- TorXakis
- T-Vec
- Uppaal Cover
- Uppaal-Tron
- Tveda
-

MBT : Some Tools - commercial

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-

Learning

Test-Based Modelling

Models

model-based testing

model-based monitoring

simulation

model checking

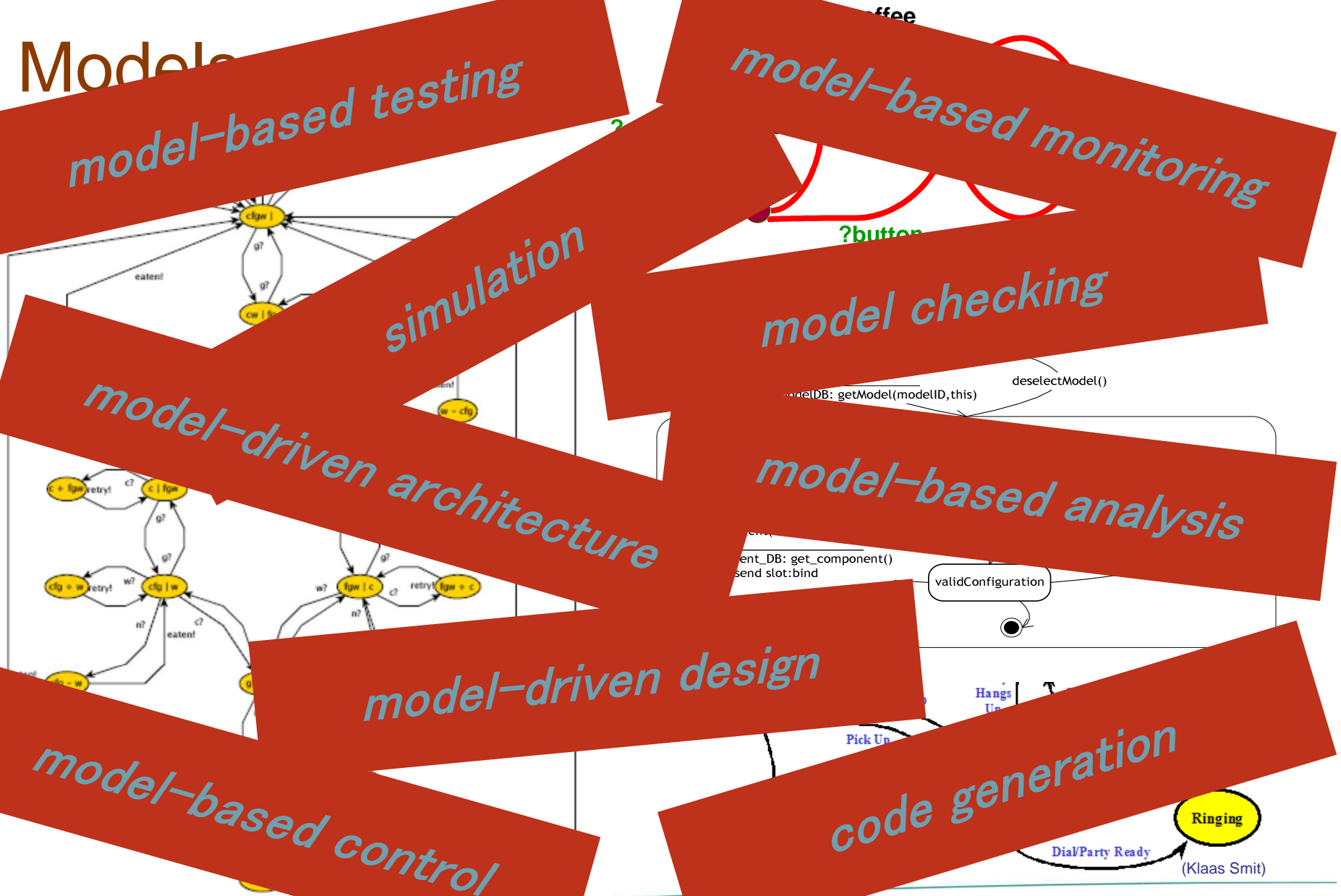
model-driven architecture

model-based analysis

model-driven design

model-based control

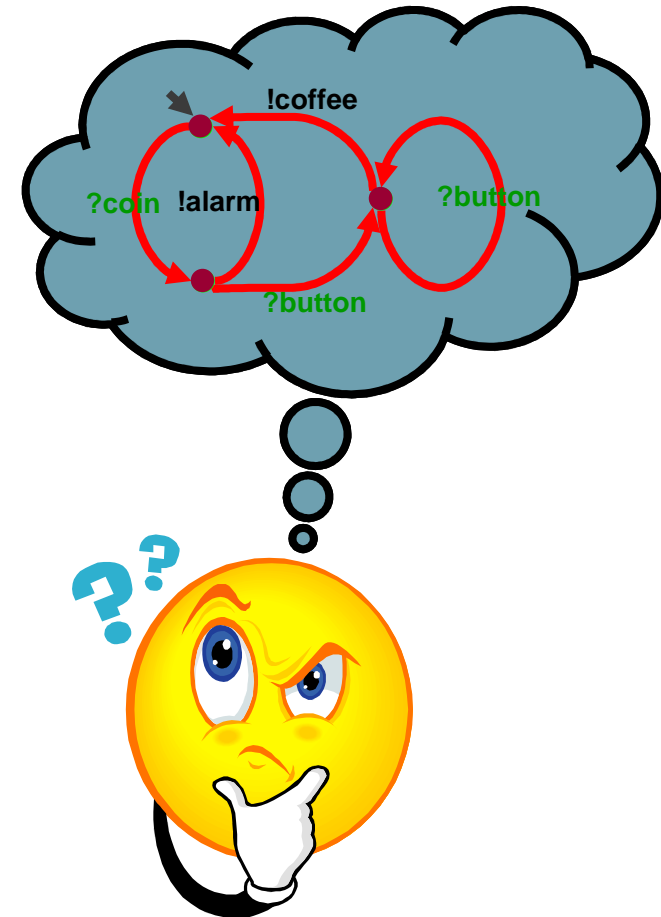
code generation



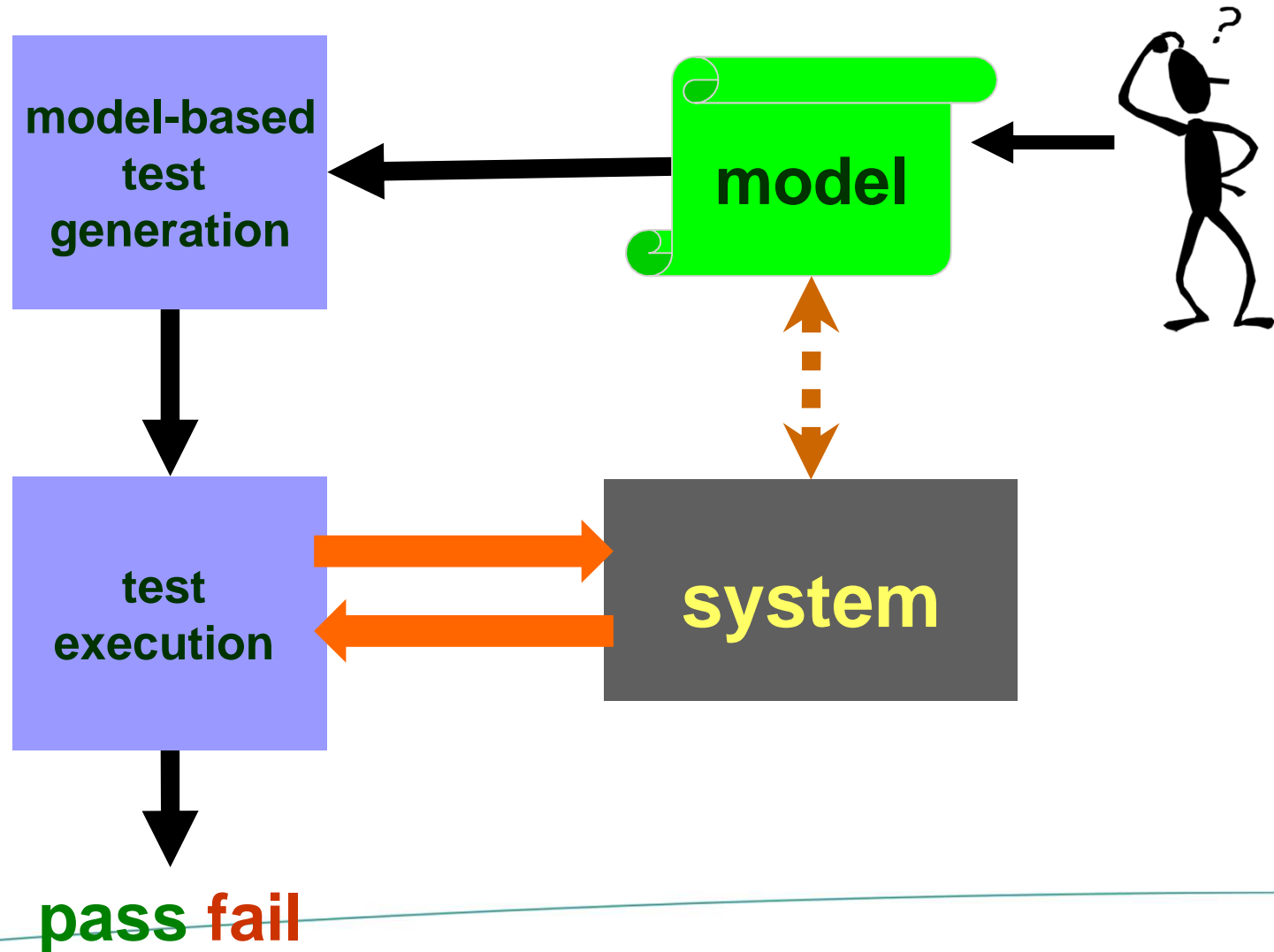
(Klaas Smit)

Models

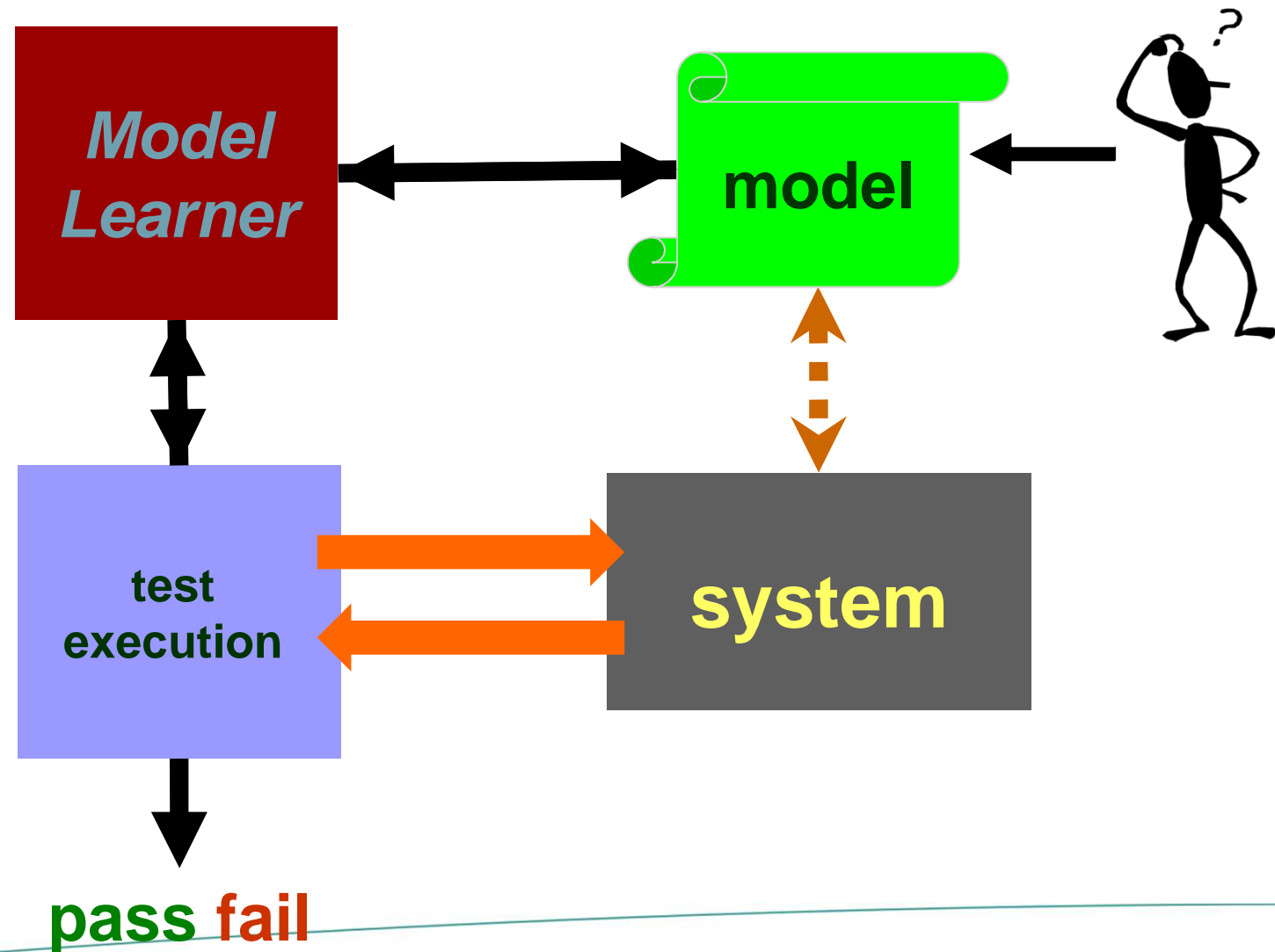
- Everybody wants models
- Doing nice things with models
 - model checking, simulation,
- **How to get these models?**
 - *in particular for:*
legacy, third-party, out-sourced, off-the-shelf,
- **Does the model correspond with the real system?**



Testing : Model-Based Testing



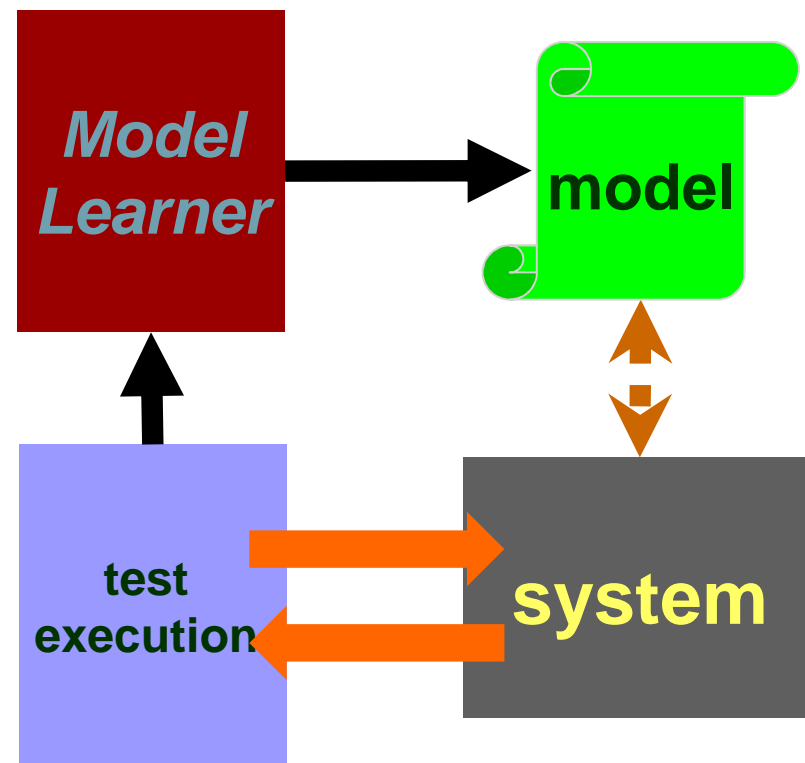
Test-Based Modeling



Test-Based Modeling

Automatically **learning** a model of the behavior of a system from observations made with **testing**

- *test-based modeling*
- *automata learning*
- *black-box reverse engineering*
- *observation-based modeling*
- *behavior capture and test*
- *grammatical inference*

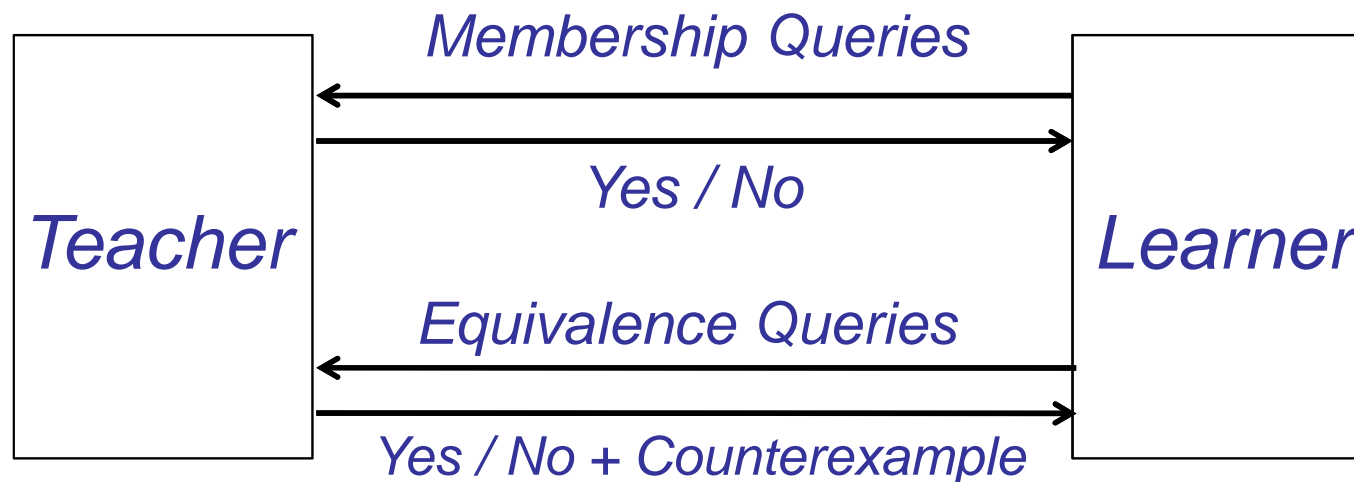


Learning Models of Automata

- Active learning is an active research area:
 - D. Angluin (1987) : L^* -algorithm
 - *LearnLib* : Tool for FSM learning
 -

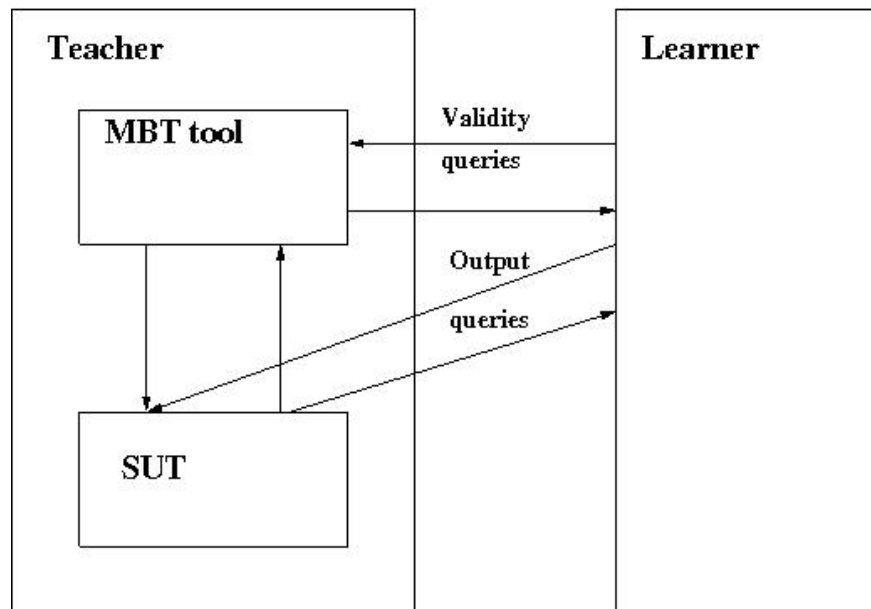


Learning Finite Automata with L^ :*



Learning Models of Reactive Systems

- Tool for active learning of Finite State Machines : **LearnLib**
- Developed by group B. Steffen (U. Dortmund)
- Able to learn models with up to 10.000 states



- **Learner:**
formulate
a hypothesis FSM
- Equivalence query
replaced by
model-based testing
of hypothesized model

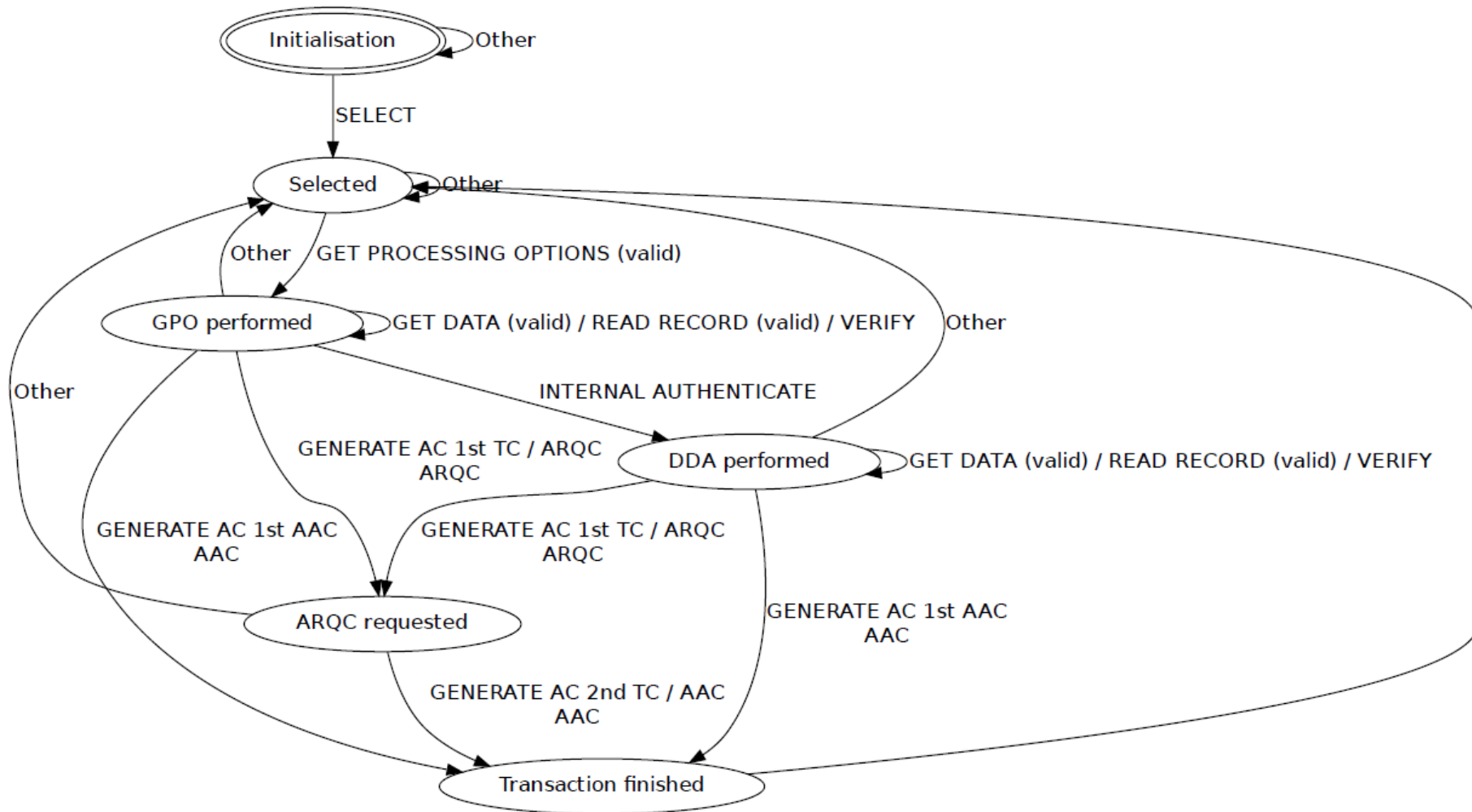
Application: Banking Cards: Learning the EMV protocol

Fides Aarts, Erik Poll, and Joeri de Ruiter

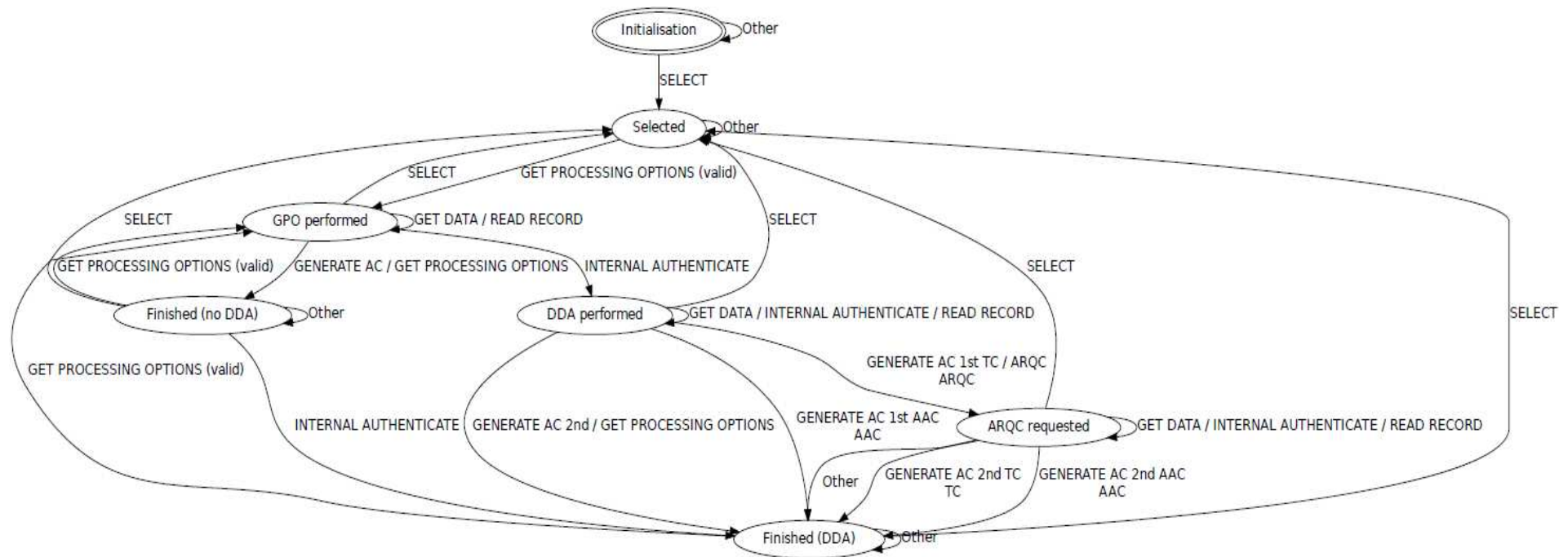
- EMV =
Europay, Mastercard and Visa
- Models from black-box implementations
- Learn behaviour blindly
- Security: absence of unwanted functionality
- Correctness/conformance:
presence of required functionality



Model of Maestro app on Dutch banking card

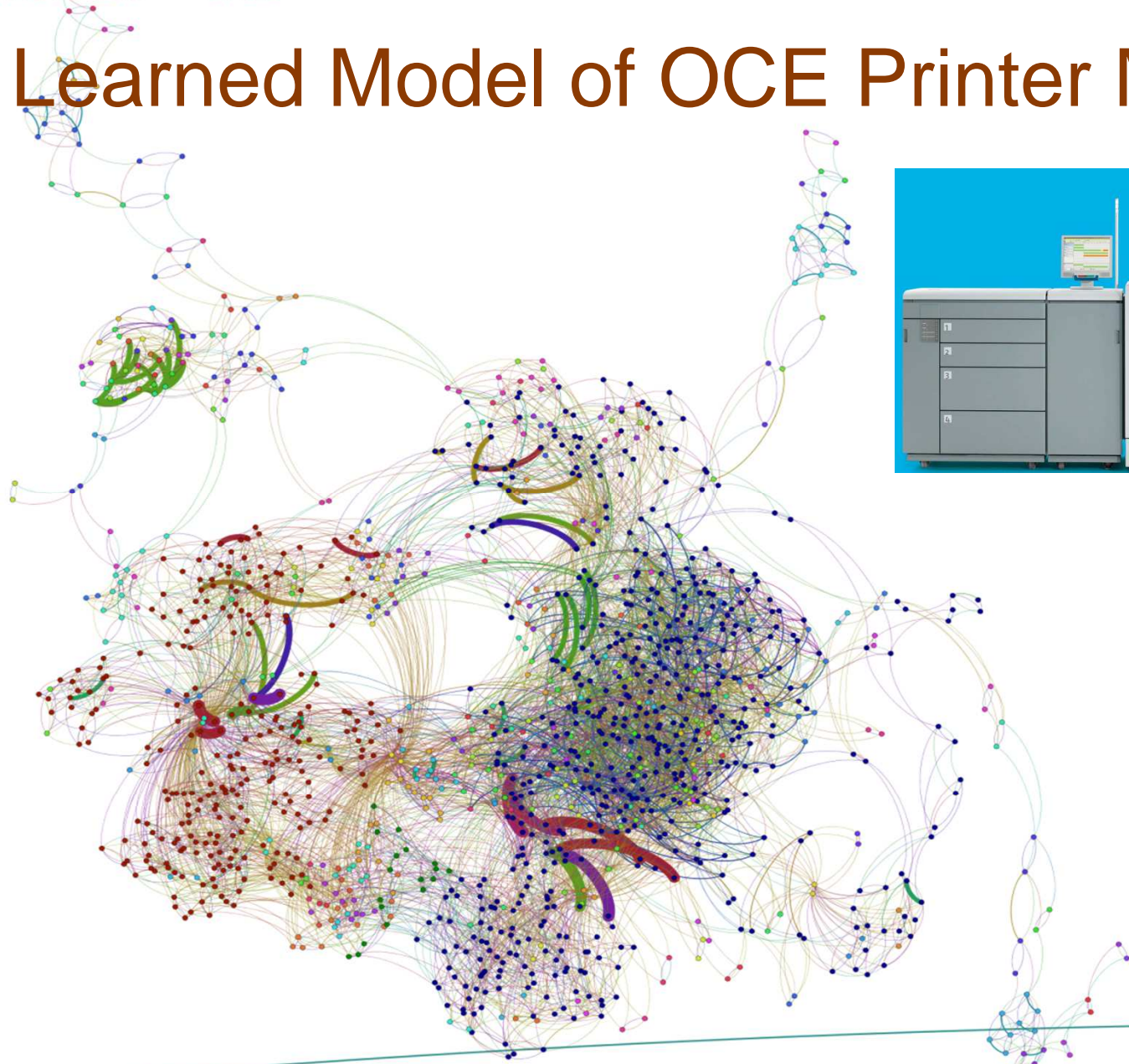


Model of Maestro app on German banking card

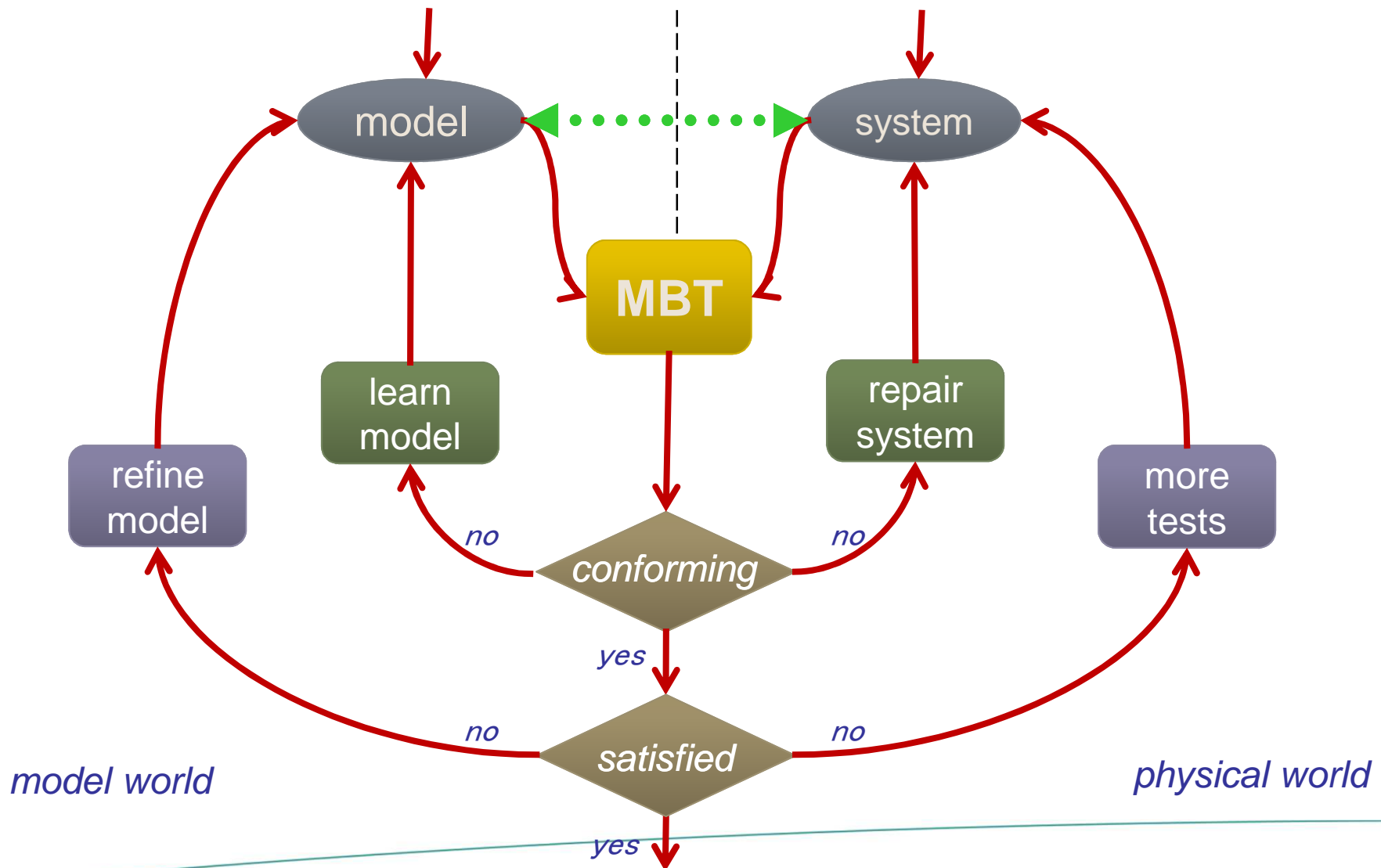


- Dutch vs. German banking card: different handling of errors

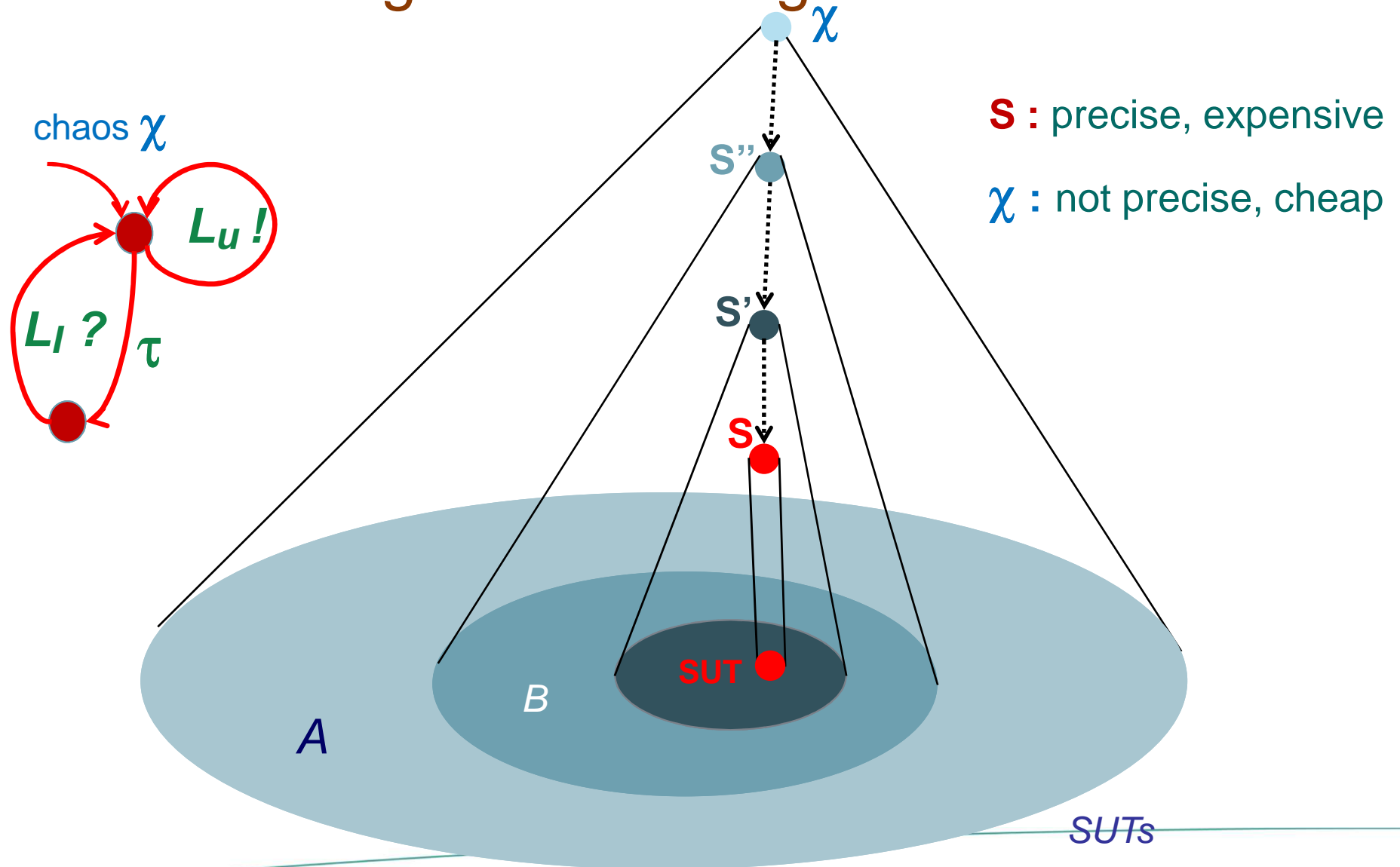
Learned Model of OCE Printer Module



Model-Based Testing & Test-Based Modeling



Test Coverage = Learning Precision



Model-Based Testing

*There is Nothing More Practical
than a Good Theory*