

# Model-based Mutation Testing

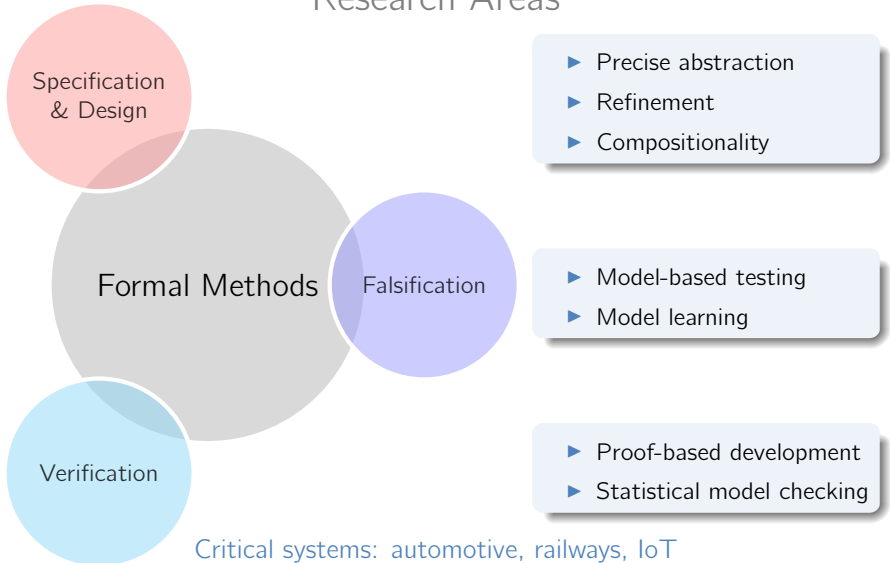
## The Science of Killing Bugs in a Black Box

Bernhard K. Aichernig

Institute of Software Technology  
Graz University of Technology  
Austria

8th Halmstad Summer School on Testing, HSST 2018,  
Halmstad University, 11 June 2018

# Research Areas



Critical systems: automotive, railways, IoT

## FM Group Characteristics

- ▶ **Size:** key researcher + 3 research assistants (PhDs)
- ▶ **EU projects:** 4 in last 10 years
- ▶ **LEAD project:** Dependable Things
- ▶ **Funding:** EUR 192K per year (3 years avg.)
- ▶ **Expertise:** falsification + verification + languages
- ▶ **Domains:** automotive, railways, Internet of Things



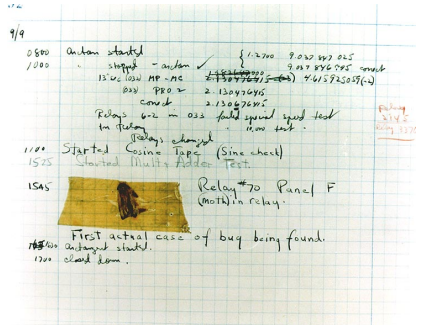
# Agenda

- ▶ Mutation Testing
- ▶ Model-based Testing
- ▶ Model-based Mutation Testing
- ▶ Transformational Systems
  - ▶ Semantics
  - ▶ Test Case Generation
- ▶ Reactive Systems
  - ▶ Semantics
  - ▶ Test Case Generation
- ▶ Model- and Test-Driven Development
- ▶ MoMuT Tools
- ▶ Tool Demo and Examples

# Bugs?

Part of engineering jargon for many decades:

- ▶ Moth trapped in relay of Mark II (Hopper 1946)
- ▶ Little faults and difficulties (Edison 1878):
- ▶ Software bugs



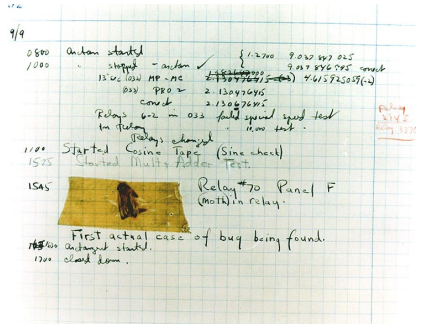
Relay #70 Panel F  
(moth) in relay.

First actual case of bug being found.

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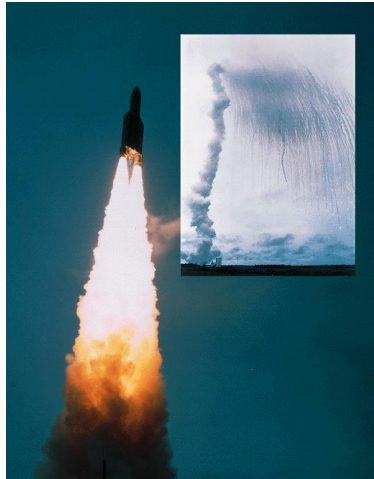
## Definition

A software bug is the common term used to describe an

- ▶ error, flaw, mistake, failure, or fault in a computer program or system
- ▶ that produces an incorrect or unexpected result,
- ▶ or causes it to behave in unintended ways. (Wikipedia 2012)

# Some Bugs Become Famous!

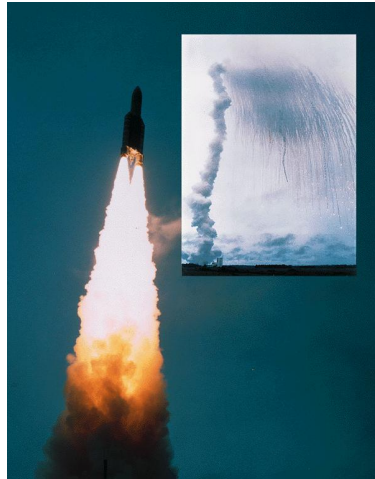
- ▶ Ariane 5 test flight (1996)
  - ▶ out of control due to software failure
  - ▶ controlled destruction!
- ▶ Loss of
  - ▶ money and time
  - ▶ satellites
  - ▶ research (TU Graz)
- ▶ Dijkstra (EWD 1036):
  - ▶ call it error, not bug
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# Some Bugs Hide for a Long Time!

## Binary search bug in Java

- ▶ JDK 1.5 library (2006)
- ▶ out of boundary access of large arrays
- ▶ due to integer overflow
- ▶ 9 years undetected

```
1 public static
2 int binarySearch(int[] a,int key)
3 {
4     int low = 0;
5     int high = a.length - 1;
6
7     while (low <= high) {
8         int mid = (low + high) / 2;
9         int midVal = a[mid];
10
11         if (midVal < key)
12             low = mid + 1;
13         else if (midVal > key)
14             high = mid - 1;
15         else
16             return mid; // key found
17     }
18     return -(low + 1); // key not found
19 }
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“Beware of bugs in the above code;  
I have only proved it correct, not tried it.”  
[Knuth77]

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# Observations

- ▶ Verification failed (wrong assumption)
- ▶ Established testing strategies failed:
  - ▶ statement coverage
  - ▶ branch coverage fails
  - ▶ multiple condition coverage
  - ▶ MC/DC: standard in avionics [DO-178B/ED109]
- ▶ Long array needed: `int[] a = new int[Integer.MAX_VALUE/2+2]`

## Lesson

- ▶ Concentrate on possible faults, not on structure.
- ▶ Generate test cases covering these faults
- ▶ **Mutation Testing** [Lipton71, Hamlet77, DeMillo et al.78]

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# What Is Mutation Testing?

Originally: Technique to verify the quality of test cases

“There is a pressing need to address the, currently unresolved, problem of test case generation.” [Jia&Harman11]

Y Jia, M Harman: *An analysis and survey of the development of mutation testing*. IEEE transactions on software engineering 37 (5), 2011.



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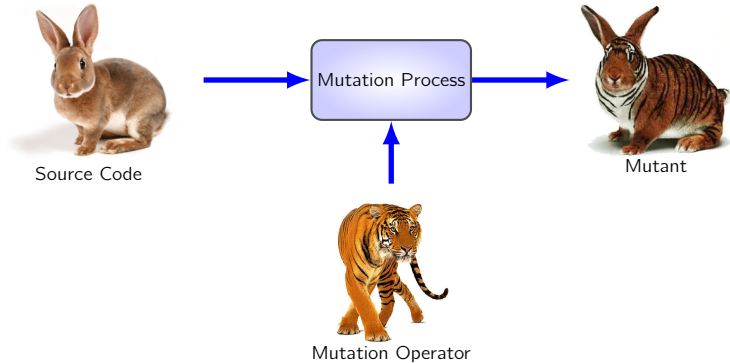
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# How Does It Work?

## Step 1: Create mutants



# Example: Transformational System

- ▶ Kind of triangles:
  - ▶ equilateral 
  - ▶ isosceles 
  - ▶ scalene 
- ▶ Create mutants
  - ▶ mutation operator  
`==`  $\Rightarrow$  `>=`
  - ▶ creates 5 mutants




```

1  object triangle {
2
3  def tritype(a : Int, b : Int, c: Int) =
4  (a,b,c) match {
5  case _ if (a <= c-b) => "no triangle"
6  case _ if (a <= b-c) => "no triangle"
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9                                "equilateral"
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Source code in Scala

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Mutant

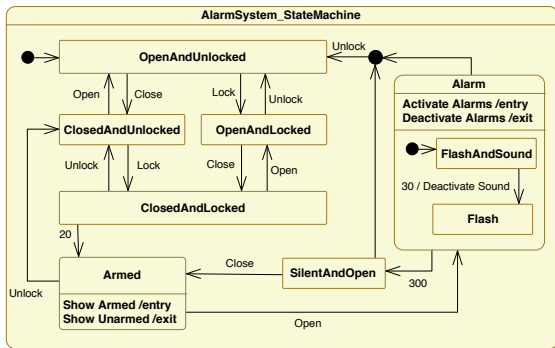
# Example: Reactive System

## ► Car Alarm System

- event-based
- controllable events
- observable events

## ► Mutate the model

- mutation operator  
→ ⇒ ↻
- 17 mutants



State machine model in UML

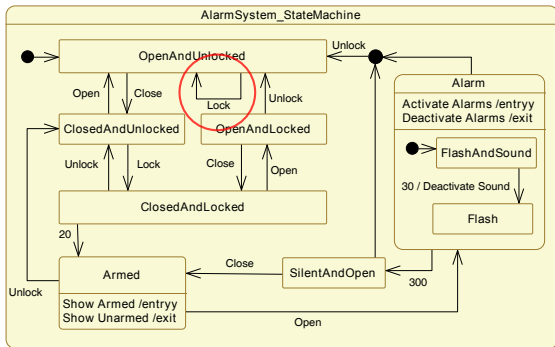
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 $\rightarrow \Rightarrow \curvearrowright$
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Mutated UML model

# How Does It Work?

Step 2: Try to kill mutants



A test case kills a mutant if its run shows different behaviour.

# Example: Transformational System

- ▶ Mutant survives  
path coverage (MC/DC):

tritype(0,1,1)

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tritype(1,1,0)

tritype(1,1,1)

tritype(2,3,3)

tritype(3,2,3)

tritype(3,3,2)

tritype(2,3,4)

- ▶ Mutant killed by  
tritype(3,2,2)

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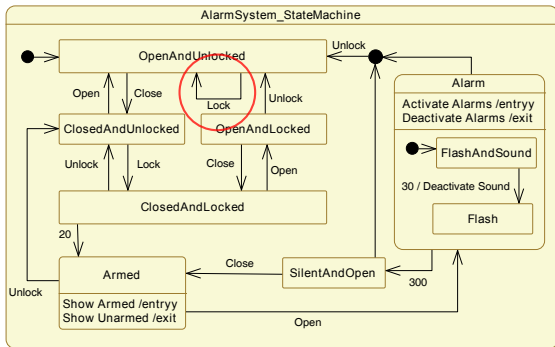


Mutant

# Example: Reactive System

- ▶ Mutant survives
  - ▶ function coverage
  - ▶ state coverage
  - ▶ transition coverage

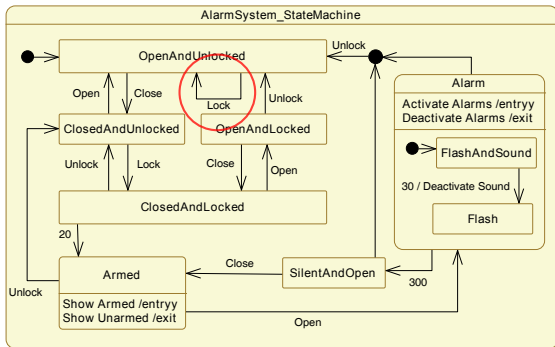
- ▶ Killed by
  - Lock();
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  - After(20);



Mutated UML model

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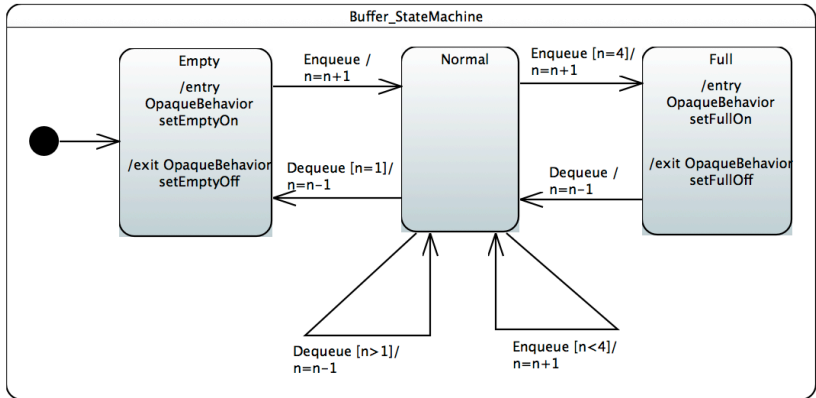
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# Fault-Propagation in Models

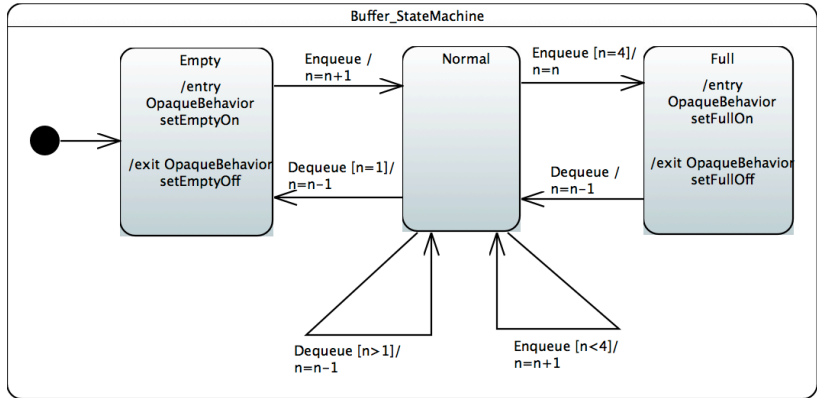
Abstract 5-place buffer model:



Counter variable  $n$  is internal!

# Fault-Propagation in Models

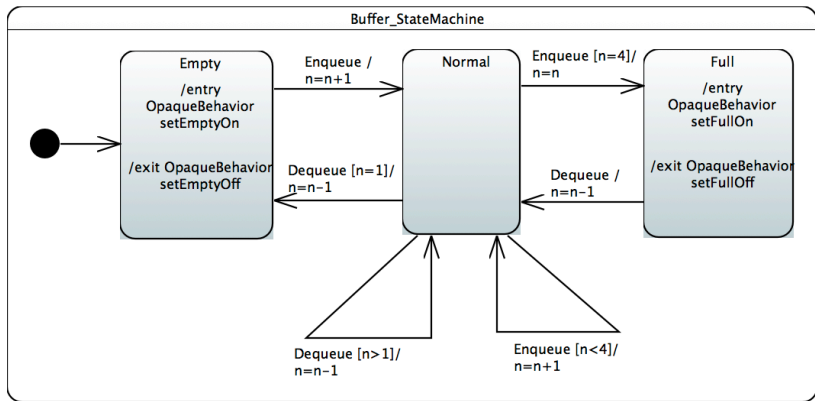
Let's inject a fault:



How does this fault propagate?

# A Good Test Case

... triggers this fault and propagates it to a (visible) failure:



`<!setEmptyOn, ?Enqueue, !setEmptyOff, ?Enqueue, ?Enqueue, ?Enqueue, ?Enqueue, !setFullOn, ?Dequeue, !setFullOff, ?Enqueue, !setFullOn>`

# From Analysis to Synthesis

State of art:

## Analysis of test cases

How many mutants killed by test cases?

$$\text{mutation score} = \frac{\#killed\ mutants}{\#mutants}$$

**Problem:** equivalent mutants

**Solution:** review of surviving mutants

Research:

## Synthesis of test cases

Find test cases that maximise mutation score.

Idea:

- ▶ Check equivalence between original and mutant
- ▶ Use counter-example as test case.

**Problem:** equivalence checking is hard (undecidable in general)

**Solution:** generate from models (abstraction)

→ **model-based mutation testing**

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# Model-based Testing

Model-based testing (MBT) is

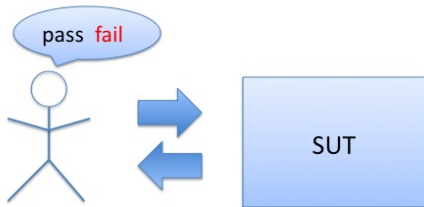
- ▶ the **automatic generation** of software test procedures,
- ▶ using models of system requirements and behavior
- ▶ in combination with automated test execution.

# Objective

"Don't write test cases,  
generate them!"

(John Hughes)

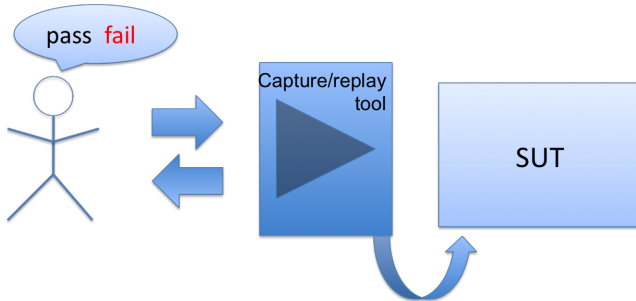
# Levels of Testing: Manual



# Levels of Testing: Manual

- + easy & cheap to start
- + flexible testing
- expensive every execution
- no auto regression testing
- ad-hoc coverage
- no coverage measurement

# Levels of Testing: Capture & Replay

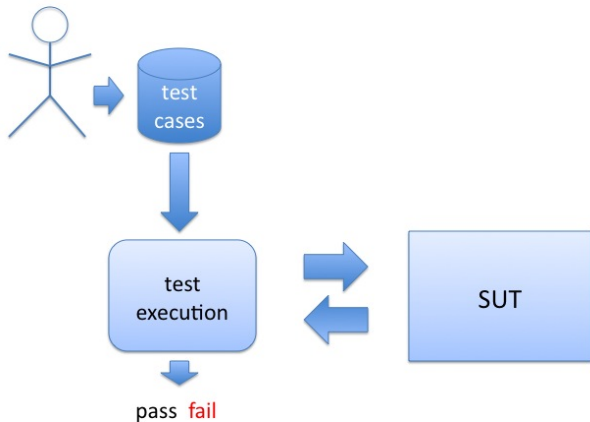




## Levels of Testing: Capture & Replay

- + auto regression testing
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- expensive first execution
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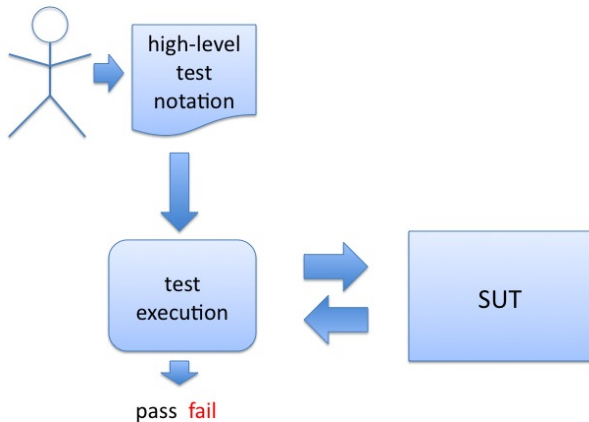
# Levels of Testing: Scripts



## Levels of Testing: Scripts

- + auto regression testing
- + automatic execution
- +/- test impl. = programming
  - fragile tests break easily?  
(depends on abstraction)
  - ad-hoc coverage
  - no coverage measurement

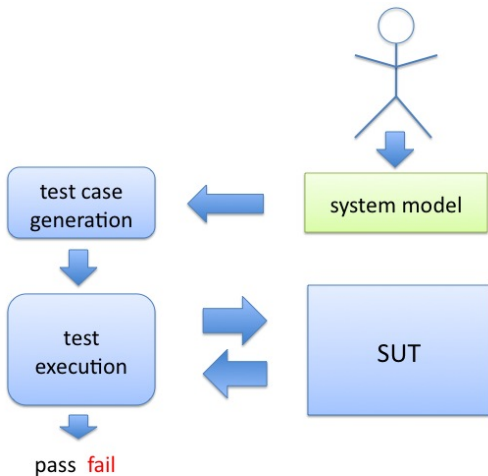
# Levels of Testing: Test Scenarios



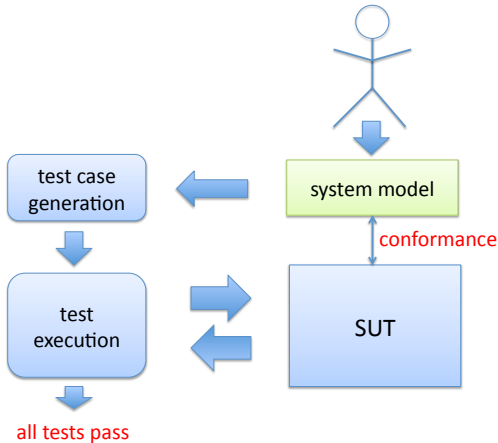
# Levels of Testing: Test Scenarios

- + abstract tests
- + automatic execution
- + auto regression testing
- + robust tests
- ad-hoc coverage
- no coverage measurement

# Levels of Testing: Model-Based Testing



# Levels of Testing: Model-Based Testing

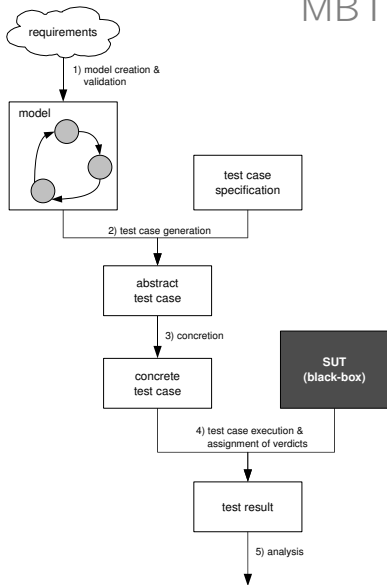


# Levels of Testing: Model-Based Testing

- + abstract tests
- + automatic execution
- + auto regression testing
- + auto design of tests
- + systematic coverage
- + measure coverage of model and requirements
- modelling efforts



# MBT Workflow



## Manual tasks:

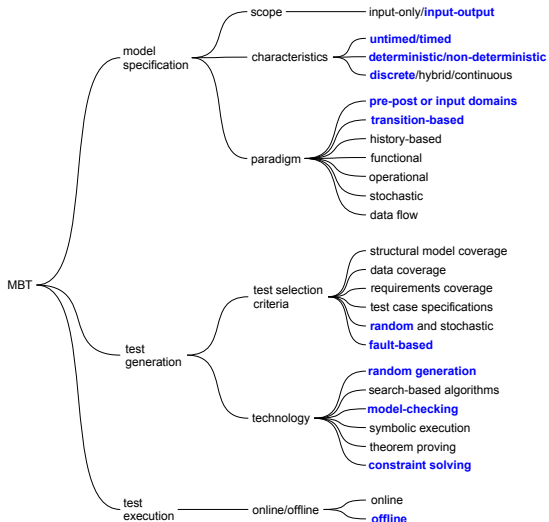
- ▶ (requirements analysis)
- ▶ model creation
- ▶ model validation
- ▶ concretion implementation

## Automated tasks:

- ▶ model verification
- ▶ test-case generation
- ▶ test-case concretion
- ▶ test-case execution
- ▶ assignment of verdicts

# Taxonomy

M. Utting, A. Pretschner, B. Legeard: *A taxonomy of model-based testing approaches*. Software Testing, Verification and Reliability, 22(5), 2012.



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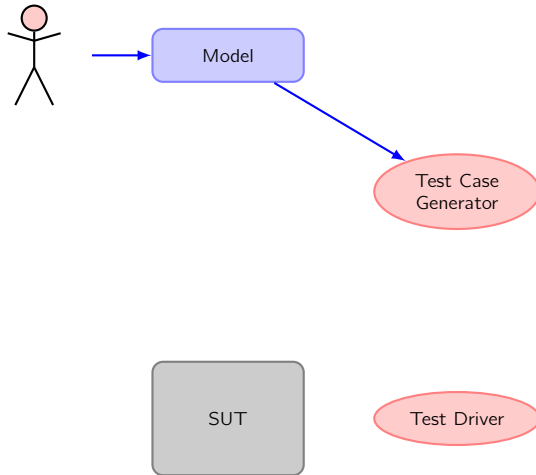


Test Case  
Generator

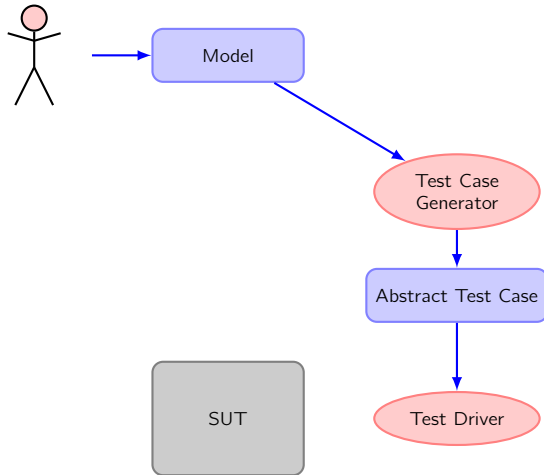
SUT

Test Driver

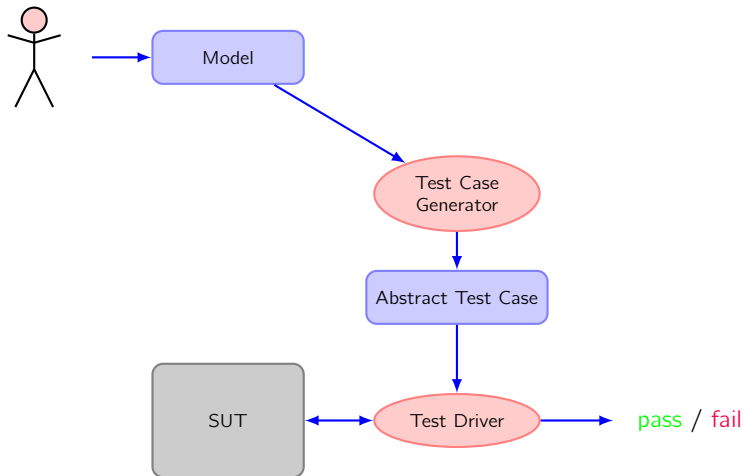
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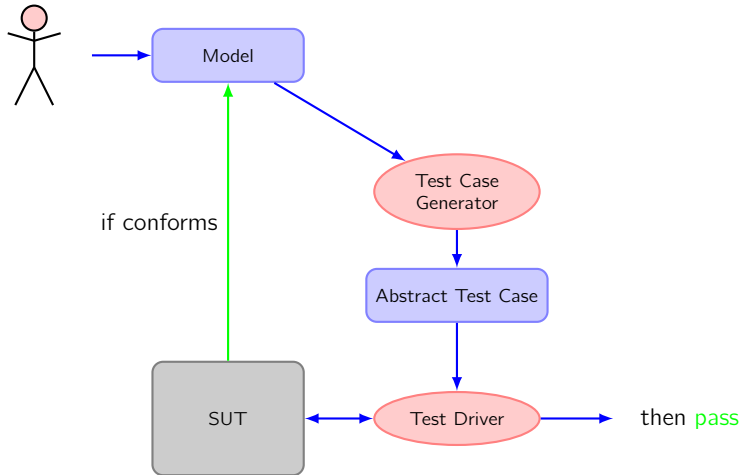
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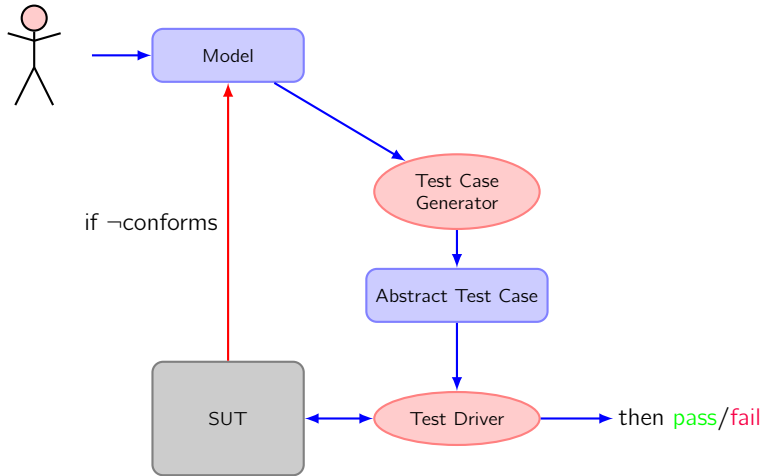


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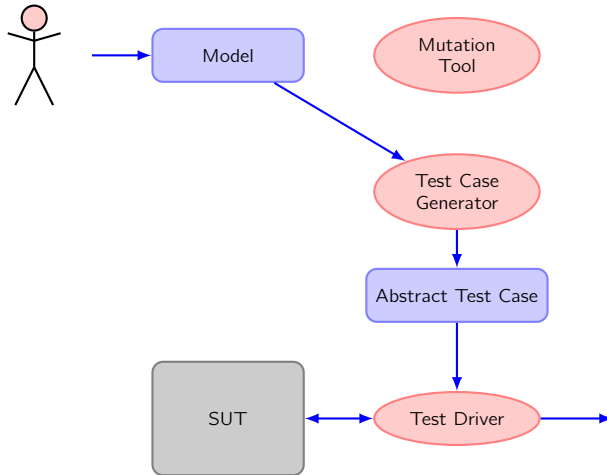




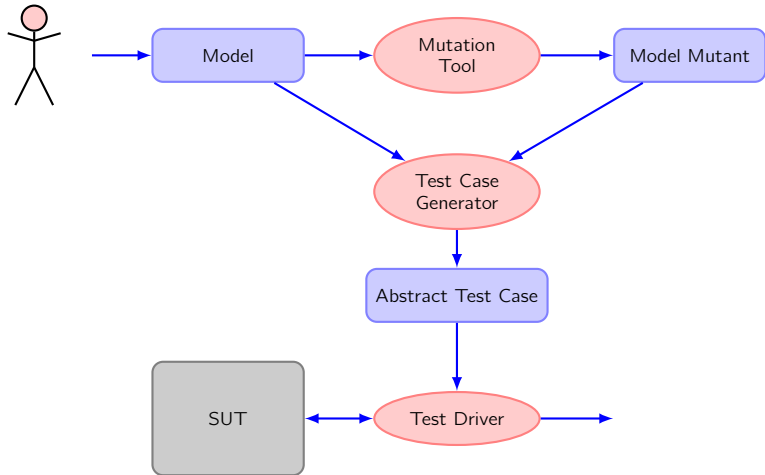
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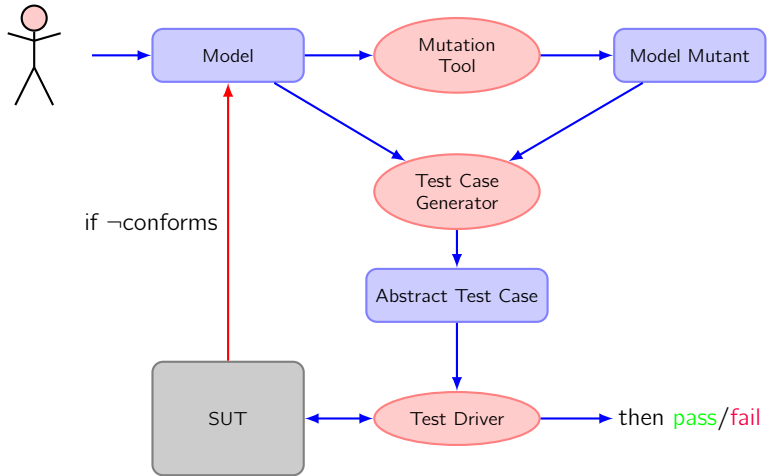
# Model-Based Mutation Testing



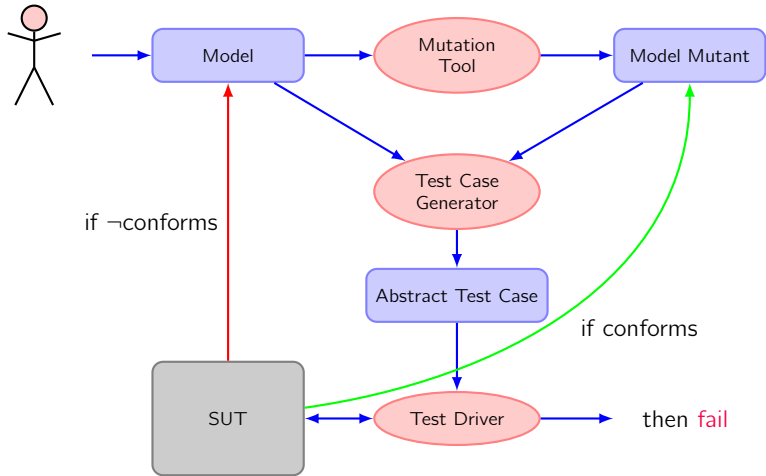
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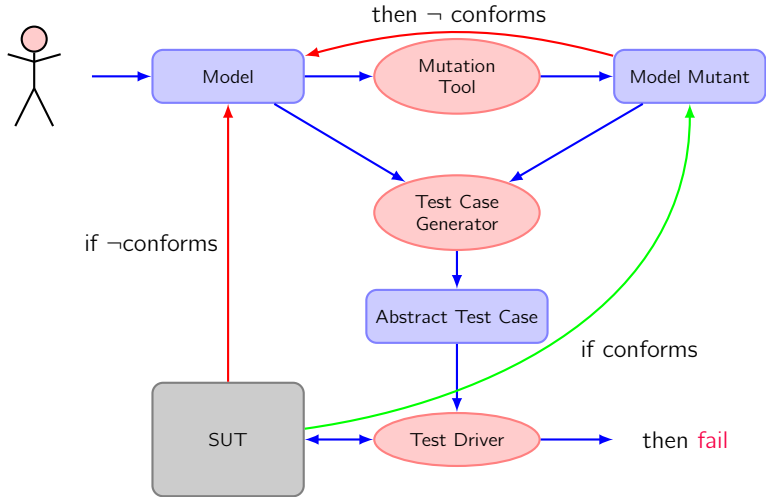
# Model-Based Mutation Testing



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# Model-Based Mutation Testing



# Non-Conformance & Test Cases

## Theorem

Given a transitive conformance relation  $\sqsubseteq$ , then

$$(Model \not\sqsubseteq SUT) \wedge (Mutant \sqsubseteq SUT) \Rightarrow (Model \not\sqsubseteq Mutant)$$

- ▶ What are the cases of non-conformance?
- ▶ Test these cases on the SUT!
- ▶ These test cases will detect if mutant has been implemented.

# Test Cases as Partial Specifications

- ▶ A test case can be interpreted as a partial specification (model)
  - ▶ defines output for one input case, rest undefined.
- ▶ If a SUT (always) passes a test case, we have conformance:

$$\textit{Test case} \sqsubseteq \textit{SUT}$$

- ▶ If we generate a test case from a model, we have selected a partial behaviour such that

$$\textit{Test case} \sqsubseteq \textit{Model}$$

- ▶ If SUT conforms to the model:

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# Fault-Detecting Test Case

- ▶ Generated from the model
- ▶ Kills the mutant

*Test case*  $\sqsubseteq$  *Model*

- ▶ It is a counter-example to conformance, hence

*Model*  $\not\sqsubseteq$  *Mutant*

iff

$\exists$  *Test case* : (*Test case*  $\sqsubseteq$  *Model*  $\wedge$  *Test case*  $\not\sqsubseteq$  *Mutant*)

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# Agenda

- ▶ Mutation Testing
- ▶ Model-based Testing
- ▶ Model-based Mutation Testing
- ▶ Transformational Systems
  - ▶ Semantics
  - ▶ Test Case Generation
- ▶ Reactive Systems
  - ▶ Semantics
  - ▶ Test Case Generation
- ▶ Model- and Test-Driven Development
- ▶ MoMuT Tools
- ▶ Tool Demo and Examples

# Transformational Systems: Semantics

- ▶ Model and Mutant interpreted as predicates  $Model(s, s')$  and  $Mutant(s, s')$  describing state transformations ( $s \rightarrow s'$ )
- ▶ Conformance:

$$Model \sqsubseteq Mutant =_{df} \forall s, s' : Mutant(s, s') \Rightarrow Model(s, s')$$

- ▶ Non-conformance:

$$Model \not\sqsubseteq Mutant = \exists s, s' : Mutant(s, s') \wedge \neg Model(s, s')$$

- ▶ Read: a behaviour allowed by mutant but not by original model?
- ▶ This is a constraint satisfaction problem!

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# Transformational Systems: Example

Triangle semantics:

$$\text{Mutant}(a, b, c, \text{res}') \wedge \neg \text{Model}(a, b, c, \text{res}') \stackrel{\text{df}}{=}$$

(...

$$\neg(a \leq c - b \vee a \leq b - c \vee b \leq a - c) \wedge (a \geq b \wedge b = c \wedge \text{res}' = \text{equilateral})$$

...)

¬(...

$$\neg(a \leq c - b \vee a \leq b - c \vee b \leq a - c) \wedge (a = b \wedge b = c \wedge \text{res}' = \text{equilateral})$$

...)



- ▶ Simplifies to  $a > b \wedge b = c \wedge \text{res}' = \text{equilateral}$
- ▶ Solver produces solution:  $a = 3, b = 2, c = 2, \text{res}' = \text{equilateral}$
- ▶ Test case with expected result:  $a = 3, b = 2, c = 2, \text{res}' = \text{isosceles}$

# Transformational Systems: Tools

Implemented with different solvers:

- ▶ OCL contracts  
(Constraint Handling Rules)
- ▶ Spec# contracts (Boogie, Z3)
- ▶ Reo connector language  
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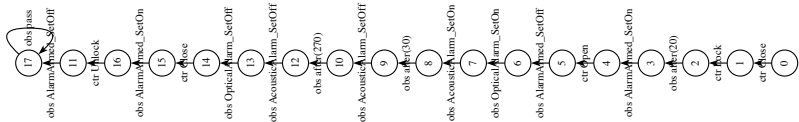
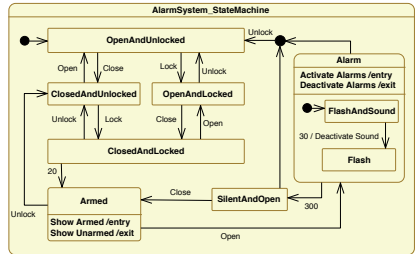
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- ▶ Mutation Testing
- ▶ Model-based Testing
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- ▶ **Reactive Systems**
  - ▶ Semantics
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# Reactive Systems

- ▶ React to the environment
- ▶ Do not terminate
- ▶ Servers and Controllers
- ▶ **Events:** controllable and observable communication events
- ▶ **Test cases:** sequences of events



Adaptive test cases: trees branching at **non-deterministic** observations



# Semantics

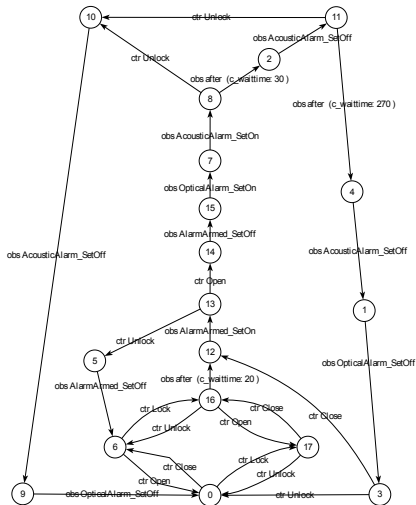
- ▶ Operational semantics  
e.g. Labelled Transition Systems

- ▶ Input-output conformance (ioco) [Tretmans96]

$SUT \text{ ioco } Model \Rightarrow_{gr}$

$\forall \sigma \in \text{traces}(Model) :$   
 $\text{out}(SUT \text{ after } \sigma) \subseteq \text{out}(Model \text{ after } \sigma)$

out ... outputs + quiescence  
 after ... reachable states after trace





# Semantics

- ▶ Operational semantics  
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[Tretmans96]

$SUT \text{ ioco } Model \stackrel{df}{=}$

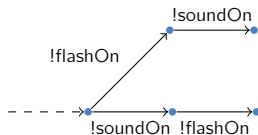
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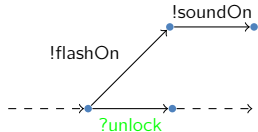
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Model:



SUT:

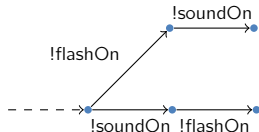


$SUT \text{ ioco } Model$  ✓

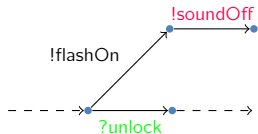
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- ▶ Model and Mutant  $\rightarrow$  LTS
- ▶ Determinisation

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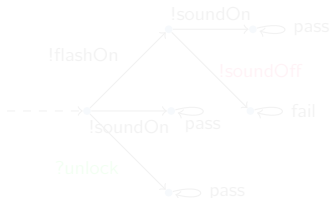


Mutant:



- ▶ Build synchronous product modulo  $ioco$
- ▶ If mutant has additional
  - ▶ !output:  $\rightarrow$  fail sink state
  - ▶ ?input:  $\rightarrow$  pass sink state

Model  $\times_{ioco}$  Mutant:

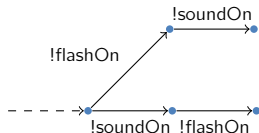


- ▶ Extract test case covering fail state

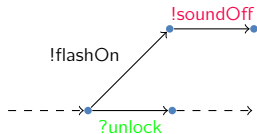
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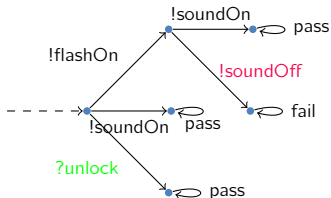


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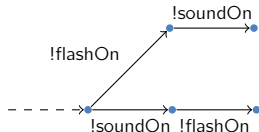


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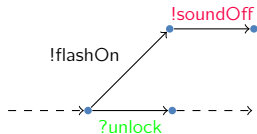
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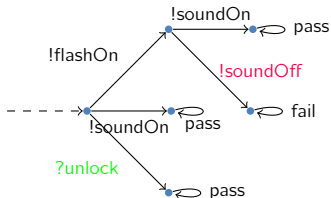


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# Applications of Explicit Conformance Checking

- ▶ HTTP Server (LOTOS)
- ▶ SIP Server (LOTOS)
- ▶ Controllers (UML)
- ▶ Hybrid Systems (Action System)

Scalability: abstractions for  
data-intensive models

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# Action Systems

- ▶ Action Systems [Back83]
- ▶ Non-deterministic choice of actions
- ▶ Actions are guarded commands
- ▶ Loop over Actions
- ▶ Terminates if all guards disabled
- ▶ Actions are labelled and represent events
- ▶ Two semantics:
  - ▶ Labelled Transition Systems
  - ▶ Predicative semantics

```

var closed : Bool := false;
    locked : Bool := false;
    armed : Bool := false;
    sound : Bool := false;
    flash : Bool := false;

actions
Close :: ¬closed → closed := true;
Open  :: closed → closed := false;
SoundOn :: armed ∧ ¬closed ∧ ¬sound →
    sound := true;
FlashOn :: armed ∧ ¬closed ∧ ¬flash →
    flash := true
...
do Close
  □
  Open
  □
  SoundOn; FlashOn
  □
  FlashOn; SoundOn
...
od
  
```

# Predicative Semantics of Action Systems

The transition relation (one step) is

- ▶ translated to a constraint over state variables  $s$  and event-traces  $tr$ :

$$\begin{array}{ll}
 I :: g \rightarrow B & =_{df} \quad g \wedge B \wedge tr' = tr \hat{\wedge} [I] \\
 I(\bar{x}) :: g \rightarrow B & =_{df} \quad \exists \bar{x} : g \wedge B \wedge tr' = tr \hat{\wedge} [I(\bar{x})] \\
 x := e & =_{df} \quad x' = e \wedge y' = y \wedge \dots \wedge z' = z \\
 g \rightarrow B & =_{df} \quad g \wedge B \\
 B(s, s'); B(s, s') & =_{df} \quad \exists s_0 : B(s, s_0) \wedge B(s_0, s') \\
 B_1 \square B_2 & =_{df} \quad B_1 \vee B_2
 \end{array}$$

- ▶ then simplified (DNF + quantifier elimination)

# Symbolic Conformance Checking

$$\exists s, s', tr, tr' : \text{reachable}(s, tr) \wedge \text{Mutant}(s, s', tr, tr') \wedge \neg \text{Model}(s, s', tr, tr')$$

- ▶ Is non-conformance reachable?
- ▶ Fast, but stronger than ioco.
- ▶ ioco for complete models:

$$\exists s_1, s'_1, s_2, s'_2, tr, !a : \text{reachable}(\text{Mutant}, tr, s_1) \wedge \text{reachable}(\text{Model}, tr, s_2)$$

$$\wedge$$

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# Symbolic Conformance Checkers

- ▶ Two implementations for Action Systems
  - ▶ Constraint Logic Programming: Sicstus Prolog
  - ▶ SMT solving: Scala + Z3
- ▶ Timed Automata: Scala + Z3 (tioco)
- ▶ After optimisations:

Bernhard K. Aichernig and Elisabeth Jöbstl. *Towards symbolic model-based mutation testing: Combining reachability and refinement checking*, MBT 2012.

Bernhard K. Aichernig and Elisabeth Jöbstl. *Efficient Refinement Checking for Model-Based Mutation Testing*, QSIC 2012.

Bernhard K. Aichernig, Florian Lorber and Dejan Nickovic. *Time for Mutants: Mutation testing with timed automata*, TAP 2013

Bernhard K. Aichernig, Elisabeth Jöbstl and Matthias Kegele. *Incremental refinement checking for test case generation*, TAP 2013



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# Symbolic Conformance Checkers

- ▶ Two implementations for Action Systems
  - ▶ Constraint Logic Programming: Sicstus Prolog
  - ▶ SMT solving: Scala + Z3
- ▶ Timed Automata: Scala + Z3 (tioco)
- ▶ After optimisations:

Prolog and SMT equally fast!

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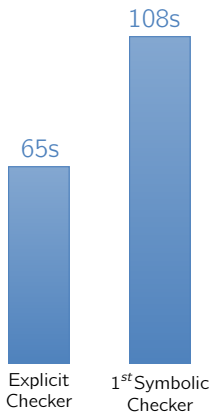
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Performance gains for checking 207 mutants of the Car Alarm System.



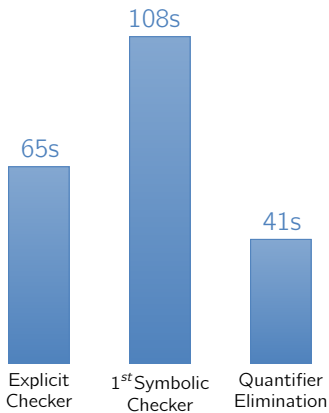
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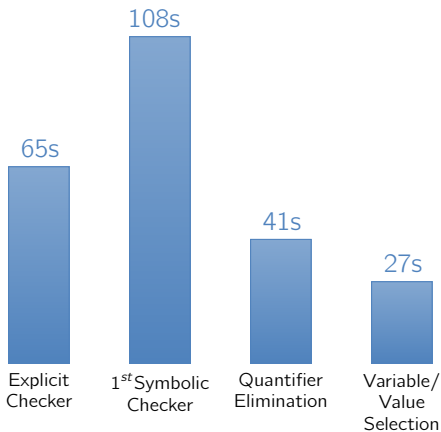
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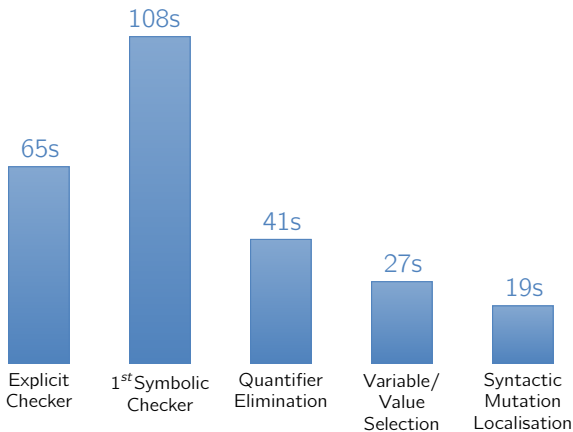
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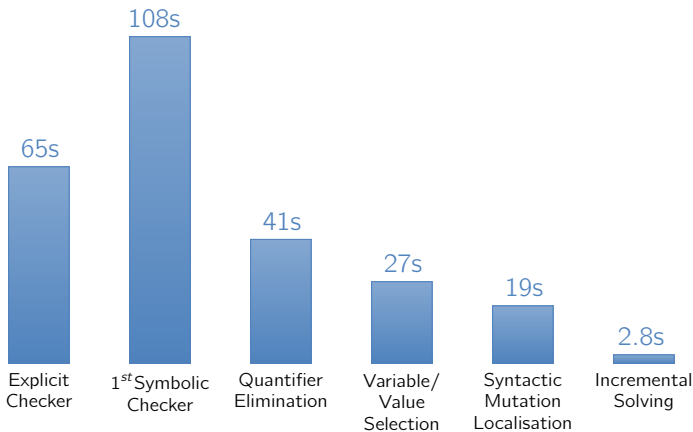
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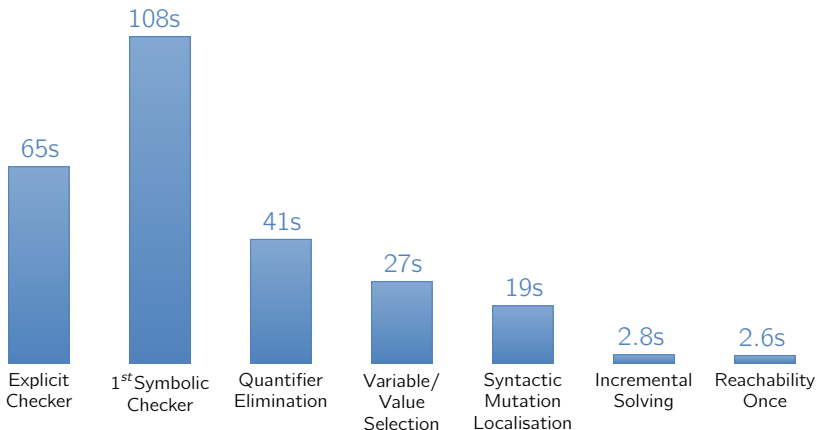
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# Optimisations

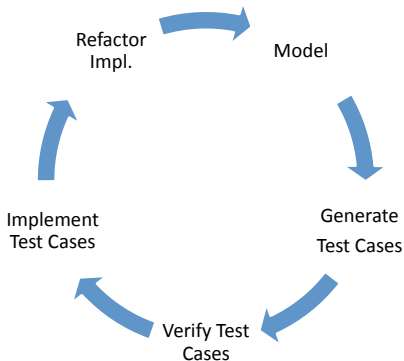
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# Agenda

- ▶ Mutation Testing
- ▶ Model-based Testing
- ▶ Model-based Mutation Testing
- ▶ Transformational Systems
  - ▶ Semantics
  - ▶ Test Case Generation
- ▶ Reactive Systems
  - ▶ Semantics
  - ▶ Test Case Generation
- ▶ Model- and Test-Driven Development
- ▶ MoMuT Tools
- ▶ Tool Demo and Examples

# Agile Development



- ▶ Model-driven development
- ▶ Model-based test case generation
- ▶ Formal verification
- ▶ Test-driven development

# Agenda

- ▶ Mutation Testing
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# MoMuT Tools

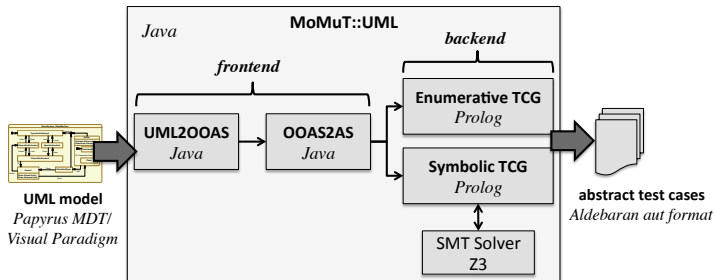
## MoMuT

- ▶ is a family of tools implementing Model-based Mutation Testing.
- ▶ is jointly developed and maintained by AIT and TU Graz
- ▶ supports different modelling styles:
  - ▶ MoMuT::UML
  - ▶ MoMuT::OOAS
  - ▶ MoMuT::TA
  - ▶ MoMuT::Reqs

[www.momut.org](http://www.momut.org)

# MoMuT::UML

- ▶ Test-case generator of AIT and TU Graz
- ▶ Implementing model-based mutation testing for UML state machines



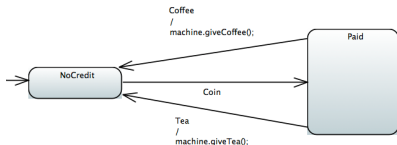
Architecture of the *MoMuT::UML* tool chain

AS ... Action Systems [Back83]

OOAS ... Object-Oriented Action Systems



# MoMuT::UML



- ▶ Enumerative back-end: *ioco*
- ▶ Symbolic back-end supports two conformance relations:
  - ▶ State-based **Refinement**
  - ▶ Event-based *ioco*

## Combined conformance checking:

- ▶ Refinement checker searches for faulty state (fast)
- ▶ *ioco* checker looks if faulty state propagates to different observations

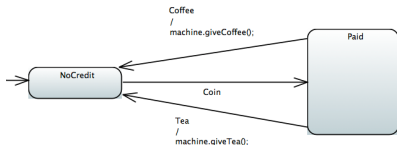
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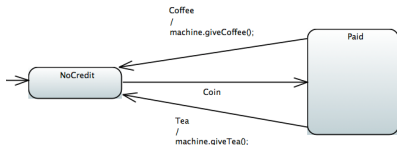
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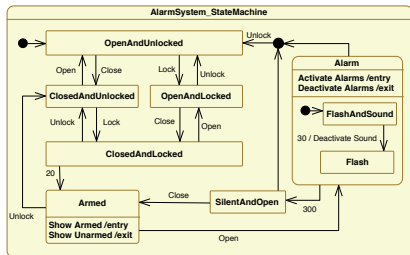
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# Case Study 1: Car Alarm System

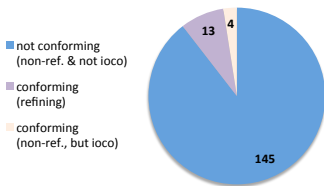


State machine model in UML

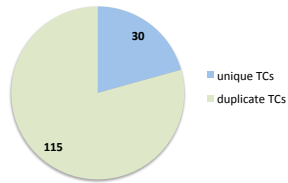
	CAS	UML
actions [#]		51
state variables [#]		35
possible states [#]		$1.7 \cdot 10^{18}$
reachable states [#]		229
required exploration depth		17

## Metrics of Generated Action System

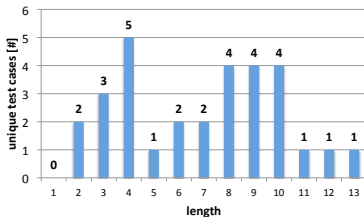
# Case Study 1: TCG



(a) Breakup into conforming and not conforming model mutants.



(b) Breakup into unique and duplicate test cases.



(c) Lengths of the unique test cases.

# Case Study 1: Fault Propagation

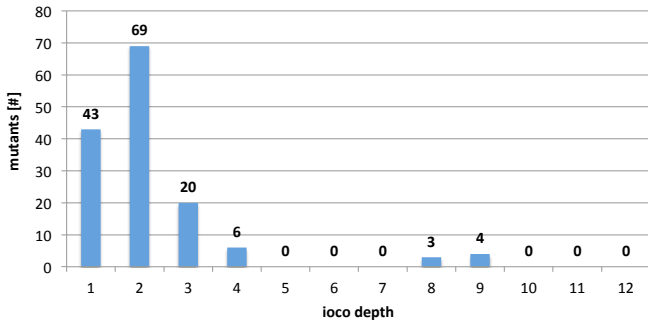


Figure: Number of steps from fault to failure (ioco depths)

## Case Study 1: Run-times

... for combined conformance checking (in sec., max. depth 20+20) :

		conforming (refining)	conforming (non-ref., but ioco)	not conforming (non-ref. & not ioco)	total
mutants [#]		13	4	145	162
ref. check	$\Sigma$	4.03	1.63	56.41	62.07
	$\phi$	0.31	0.41	0.39	0.38
	max	0.41	0.44	0.53	0.53
ioco check	$\Sigma$	-	17.71	1.9 min	2.2 min
	$\phi$	-	4.43	0.79	0.81
	max	-	4.48	2.01	4.48
tc constr.	$\Sigma$	-	-	1.3 min	1.3 min
	$\phi$	-	-	0.55	0.49
	max	-	-	1.48	1.48
total without logging	$\Sigma$	4.25	19.4	4.2 min	4.6 min
	$\phi$	0.33	4.85	1.74	1.7
	max	0.43	4.89	2.77	4.89

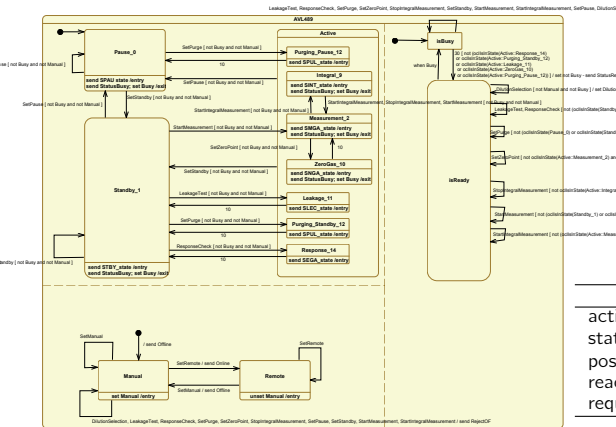
Comparison to stand-alone ioco-check with depth 20: 5.1 min

## Case Study 2: AVL489 Particle Counter

- ▶ One of AVL's automotive measurement devices
- ▶ Measures particle number concentrations in exhaust gas
- ▶ **Focus:** testing of the control logic



# Case Study 2: Test Model of AVL489

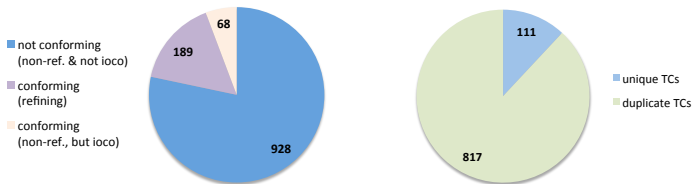


	PC_UML
actions [#]	109
state variables [#]	74
possible states [#]	$1.2 \cdot 10^{31}$
reachable states [#]	> 850 700
required exploration depth	> 25

Metrics of Generated Action System

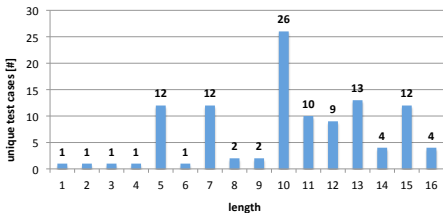


## Case Study 2: TCG



(a) Breakup into conforming and not conforming model mutants.

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(c) Lengths of the unique test cases.

## Case Study 2: Fault Propagation

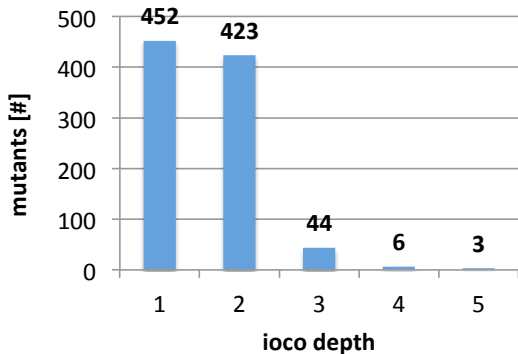


Figure: Number of steps from fault to failure (ioco depths)

## Case Study 2: Run-times

... for **combined conformance checking** (in min., max. depth 15+5) :

		conforming (refining)	conforming (non-ref., but ioco)	not conforming (non-ref. & not ioco)	total
mutants [#]		189	68	928	1185
ref. check	$\Sigma$	6.1 h	7.7	7.1 h	13.3 h
	$\phi$	1.9	6.8 sec	27 sec	40 sec
	max	4.3	1.8	3.9	4.3
ioco check	$\Sigma$	-	0.7 h	1.7 h	2.4 h
	$\phi$	-	38 sec	7 sec	7.4 sec
	max	-	2	27 sec	2
tc constr.	$\Sigma$	-	-	22.9	22.9
	$\phi$	-	-	1.5 sec	1.2 sec
	max	-	-	3.7 sec	3.7 sec
total without logging	$\Sigma$	6.1 h	0.9 h	9.2 h	16.2 h
	$\phi$	1.9	0.8	0.6	0.8
	max	4.3	2.2	4.1	4.3

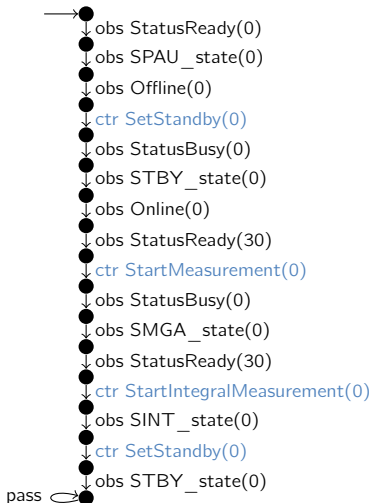
## Case Study 2: Run-times

... comparison to [stand-alone ioco check](#) (in min., max. depth 10):

		not ioco	ioco	total
mutants [#]		719	466	1185
$\Sigma$		9.8 h	22.8 h	32.6 h
time – ioco check	$\phi$	0.8	2.9	1.7
	max	3.9	5.2	5.2
	$\Sigma$	19	-	19
time – tc constr.	$\phi$	1.6 sec	-	1 sec
	max	5.8 sec	-	5.8 sec
	$\Sigma$	10.1 h	22.8 h	<b>32.9 h</b>
total without logging	$\phi$	0.8	2.9	1.7
	max	3.9	5.2	5.2
	$\Sigma$	10.1 h	22.8 h	<b>32.9 h</b>

appr. **16h vs. 33h**

# Abstract Test Case of AVL489



Abstract test cases → concrete C#  
NUnit test cases.

ctr ... controllable event (input)

obs ... observable event (output)

# Test Execution on Particle Counter

We found **several bugs in the SUT**:

- ▶ Forbidden changes of operating state while busy
  - ▶ Pause → Standby
  - ▶ Normal Measurement → Integral Measurement
- ▶ Ignoring high-frequent input without error-messages
- ▶ Loss of error messages in client for remote control of the device

# MoMuT::UML Reimplementation

**Motivation:** Railway Interlocking System (Thales)

- ▶ Reimplementation of enumerative TCG in C by AIT
- ▶ Assuming deterministic systems
- ▶ ioco checking  $\Rightarrow$  ioco testing (random)
- ▶ Short lived mutants: create mutants while exploring

# MoMuT::OOAS

## Object-Oriented Action Systems:

- ▶ Textual **model programs**
- ▶ Guarded Actions in do-od loop
- ▶ Modularization via objects
- ▶ Communication via methods
- ▶ Mutation directly on OOAS

Willibald Krenn, Rupert Schlick, and Bernhard K. Aichernig. *Mapping UML to labeled transition systems for test-case generation - a translation via object-oriented action systems*, FMCO, 2009

```

1  types
2    CoffeeMachine = autocons system
3  || var
4    paid : Boolean = false ;
5    coffee_sel : Boolean = false
6  actions
7    ctr coin =
8      requires true :
9        paid := true
10   end;
11   ctr coffeebutton =
12     requires paid :
13       coffee_sel := true;
14       paid := false ;
15   end ;
16   obs coffee =
17     requires coffee_sel :
18       skip
19   end ;
20 do
21   coin () [] coffeebutton () [] coffee ()
22 od
23 ]] system CoffeeMachine
  
```



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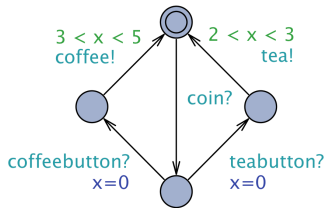
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# MoMuT::TA

## Timed Automata:

- ▶ Modelling in **UPPAAL** model checker
- ▶ Finite-state machines with real-valued **clock** variables
- ▶ Time passage in locations
- ▶ Time restrictions on locations and guards



## MoMuT::TA (cont.)

- ▶ tioco-conformance:  $M$  tioco  $S$ 
  - ▶  $out(M) \subseteq out(S)$
  - ▶ time delay is an output
- ▶ Conformance check via language inclusion
  - ▶ Requires deterministic automata
  - ▶ SMT-Solver Z3
- ▶ Determinization

Application: Crystal Usecase (Volvo)

Bernhard K. Aichernig, Florian Lorber and Dejan Nickovic. *Time for Mutants: Mutation testing with timed automata*, TAP 2013

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# MoMuT::REQs

## Contract-based Requirement Interfaces:

- ▶ Synchronous assume-guarantee pairs
- ▶ Combined via conjunction
- ▶ No model-based mutation testing yet

## Application: Airbag Chip (Infineon)

**Inputs** coin, teabutton, coffeobutton;

**Outputs** coffee, tea;

**Internals** paid;

{I} **not** paid **and not** coffee **and not** tea

{R1} **assume** coin'  
**guarantee** paid'

{R2} **assume** paid **and** teabutton' **and not** coffeobutton'  
**guarantee** tea' **and not** paid'

{R3} **assume** paid **and** coffeobutton' **and not** teabutton'  
**guarantee** coffee' **and not** paid'

{R4} **assume** teabutton' **and** coffeobutton'  
**guarantee** skip

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      guarantee tea' and not paid'
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      guarantee coffee' and not paid'
{R4} assume teabutton' and coffeobutton'
      guarantee skip
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Bernhard K. Aichernig, Klaus Hörmaier, Florian Lorber, Dejan Nickovic, Stefan Tiran. *Require, Test and Trace IT*, FMICS 2015

Bernhard K. Aichernig and Dejan Nickovic and Stefan Tiran. *Scalable Incremental Test-case Generation from Large Behavior Models*, TAP 2015.

Bernhard K. Aichernig, Klaus Hörmaier, Florian Lorber, Dejan Nickovic, Rupert Schlick, Didier Simoneau, Stefan Tiran. *Integration of Requirements Engineering and Test-Case Generation via OSLC*, QSIC 2014

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# Tool Demo



# Conclusions

- ▶ Model-based Testing + Mutation Testing
- ▶ Formal semantics → test case generators → industry
- ▶ **Novelty**: general theory + tools for **non-deterministic** models + different modelling styles
- ▶ **Future**:
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  - ▶ non-functional fault models (resource limitations)

Testing cannot show the absence of **bugs** [Dijkstra72].

Testing can show the absence of **specific bugs** [Aichernig15].

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