#### **Program Slicing**

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# (Automated) Debugging: A Sorting Program

```
1: int main(int argc, char * argv[])
2: {
3: int *a:
 4: int i;
 5: a = (int *) malloc((argc - 1) * sizeof(int));
 6: for (i = 0; i < argc - 1; i ++)
 7: a[i] = atoi(argv[i + 1]);
 8: shell_sort(a, argc);
 9: printf("Output: ");
10: for (i = 0; i < argc - 1; i++)
   printf(" %d ", a[i]);
11:
12: free(a);
13: return 0:
14: }
```

```
1: void shell_sort(int a[], int size)
 2: { int i, j; int h = 1;
 3: do {
 4. h = h * 3 + 1:
 5: \} while (h \leq size);
 6: do {
   h /= 3;
 8:
      for (i = h; i < size; i++)
 9:
        int v = a[i];
10:
        for (j = i; j >= h \&\& a[j - h] > v; j -= h)
11:
             a[i] = a[i - h]:
12:
    if (i != i) a[i] = v:
13:
14:
15: \} while (h != 1);
16: }
```

# (Automated) Debugging: A Sorting Program

Once upon a time, a tester found the following bug:

```
$ ./simple 5 4 3 2 1 666666
Output: 0 1 2 3 4 5
```

How do we find the fault?

Debugging Sequential Slicing Structured Slicing Automated Debugging Simplifying the Test-Case Isolating the Causes

#### Find and Focus

- Scientific method:
  - 1. assume,
  - 2. organize an experiment,
  - 3. if refuted, refine your assumption and repeat. possible formalization: invariants and assertions
- Observing: logging the value of infected variables
  - e.g., print command in gdb
- Watching: keeping an eye on infected variables e.g., break and watch commands in gdb
- ► Slicing: find the slice responsible for infection see the lecture on slicing



#### Getting Our Hands Dirty...

We use gdb (any other debugger will do)

- Reproduce the test: run 5 4 3 2 1 666666 Damn, the tester was right! (Not always that easy, try 55 4.)
- ➤ Simplify the test-case run 5 4 3 2
- Find the possible the origins, focus on a problem area, e.g., a[0] and shell\_sort (See slicing next...)
- ► Isolate the causes what makes a [0] wrong? compare it with the sane situation, what is different?
- Correct the problem



Debugging Sequential Slicing Structured Slicing Automated Debugging Simplifying the Test-Case Isolating the Causes

#### **TRAFFIC**

- 1. Track the problem
- 2. Reproduce the failure
- Automate and simplify the test-case:
   minimal test-case ←
- 4. Find possible origins: where it first went wrong
- Focus on the most likely origins: what part of state is infected
- Isolate the chain: what causes the state to be infected \( \Lefta \)
- 7. Correct the defect



#### DU-Paths vs. Slices

#### DU-path

direct dependencies between each definition and use of a single variable.

#### Slice

An executable subset of the program

- capturing possible (indirect) dependencies
- among all definitions and uses
- ▶ influencing the value of a set of variables.

Also called: cone of influence reduction



```
1: Input(x)
 2: Input(y)
 3: total := 0
 4: sum := 0
 5: if x < 1 then
 6:
      sum := y
 7: else
 8: read(z)
 9: total := x * y
10: end if
11: Write(total, sum)
Slice on {total} at 11?
```

```
1: Input(x)
 2: Input(y)
 3: total := 0
 4: sum := 0
 5: if x \le 1 then
 6:
     sum := y
 7: else
 8: read(z)
 9: total := x * y
10: endif
11: Write(total, sum)
Slice on {total} at 11?
```

```
Slice on {total} at 11:

1: Input(x)

2: Input(y)

3: total := 0

4: if x ≤ 1 then

5:

6: else

7: total = x * y

8: end if
```

- 1: Input(b)
- 2: c := 13: d := 3
- J. u .— S
- 4: a := d
- 5: d := b + d
- 6: b := b + 1
- 7: a := b + c
- 8: Write(a)
- Slice on  $\{d, c\}$  at 6?

```
Slice on \{d, c\} at 6:

1: Input(b)

2: c := 1

3: d := 3

4: d := b + d

(6, \{d, c\}) (in general (n, V)): the slicing criterion
```

### Outline of the algorithm

#### Slice criterion (n, V)

- Statements in the slice: those define the relevant variables.
- $\blacktriangleright$  At  $n, v \in V$ : relevant.
- ▶ A relevant  $v \in DEF(m)$ : v is no more relevant above m,
- **but** then all variables in REF(m) become relevant above m.

#### Relevant Variables

```
Given a slicing criterion (n, V), Relevant_0(m) = \begin{cases} 1 & V \\ 2a)\{v \mid \exists_{m \to m'}(v \in relevant(m') \setminus DEF(m) \lor \\ 2b) & (DEF(m) \cap relevant(m') \neq \emptyset \land v \in USE(m)))\} \end{cases} otherwise
```

- 1) base case: all variables in V are initially relevant
- 2a) v remains relevant: has been relevant below and not defined at m
- 2b) v becomes relevant: defines relevant variables

if m = n + 1

otherwise

```
Slicing criterion: (6, \{d, c\})?
Relevant_{0}(m) =
\begin{cases} 2\mathsf{a})\{v \mid \exists_{m \to m'}(v \in relevant(m') \setminus DEF(m) \lor \\ 2\mathsf{b}) & (DEF(m) \cap relevant(m') \neq \emptyset \land v \in USE(m))) \end{cases}
                         Relevant<sub>0</sub>(m)
  m
  1 Input(b) \emptyset
  2 c := 1 {b}
  3 d := 3 { c, b}
  4 a := d \qquad \{c, b, d\}
  5 d := b + d \quad \{c, b, d\}
  6 b := b + 1 \{d, c\}
```

# Slicing Sequential Programs

 $m \in Slice_0(n, V)$  when

- 1. n = m and  $DEF(m) \cap V \neq \emptyset$ , or
- 2.  $m \rightarrow \ldots \rightarrow n$  and there exists an m' such that  $m \to m'$  and  $DEF(m) \cap Relevant_0(m') \neq \emptyset$

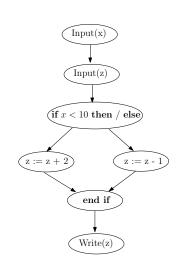
# Slicing Sequential Programs

- $m \in Slice_0(n, V)$  when
  - 1. n = m and  $DEF(m) \cap V \neq \emptyset$ , or
  - 2.  $m \to \ldots \to n$  and there exists an m' such that  $m \to m'$  and  $DEF(m) \cap Relevant_0(m') \neq \emptyset$

m	$Relevant_0(m)$	DEF(m)	$\in Slice_0(6,\{d,c\})$
1 Input(b)	Ø	{ <i>b</i> }	
2 c := 1	$\{b\}$	{ <i>c</i> }	$\sqrt{}$
3 d := 3	$\{c,b\}$	{ <i>d</i> }	$\sqrt{}$
4 a := d	$\{c,b,d\}$	{a}	×
5 d := b + d	$\{c,b,d\}$	{ <i>d</i> }	$\sqrt{}$
6 b := b + 1	$\{d,c\}$	{ <i>b</i> }	×
	$\{d,c\}$		

- 1: Input(x)
- 2: Input(z)
- 3: if x < 10 then
- 4: z := z + 2;
- 5: **else**
- 6: z := z 1;
- 7: end if
- 8: Write(z)

Slice wrt. the criterion  $(3, \{x\})$ ?

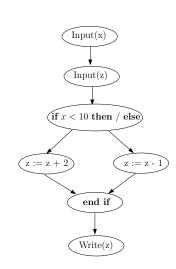


Slice wrt. the criterion  $(3, \{x\})$ ?

m	$Relevant_0(m)$	DEF(m)	$\in Slice_0(3, \{x\})$
1  Input(x)	Ø	{ <i>x</i> }	$\checkmark$
2 Input(z)	{ <i>x</i> }	{z}	×
3,5 <b>if</b> $x < 10$ <b>then</b> / <b>else</b>	{ <i>x</i> }	Ø	×
,	$\{x\}$		

- 1: Input(x)
- 2: Input(z)
- 3: if x < 10 then
- 4: z := z + 2;
- 5: **else**
- 6: z := z 1;
- 7: end if
- 8: Write(z)

Slice wrt. the criterion  $(8, \{z\})$ ?



m	$Relevant_0(m)$	DEF(m)	<b>∈</b> Slice <sub>0</sub> (8, {z})
1 Input(x)	Ø	{ <i>x</i> }	×
2 Input(z)	Ø	$\{z\}$	$\sqrt{}$
3,5 <b>if</b> $x < 10$ <b>then</b> / <b>else</b>	{z}	Ø	×
4 z := z + 2	{z}	$\{z\}$	$\sqrt{}$
6 z := z - 1	{z}	{z}	$\sqrt{}$
7 end if	{z}	Ø	×
8 Write(z)	{z}	Ø	×
	{ <i>z</i> }		

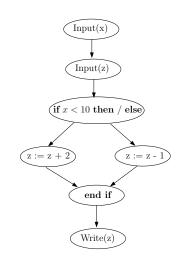
### Slicing Structured Programs: Informal Idea

- 1. Start with sequential slicing algorithm:  $Slice_0(n, v)$
- 2. Find all conditionals  $Cond_{k+1}(n, V)$  influencing  $m \in Slice_k(n, V)$
- 3. Add the following node to  $Slice_k(n, V)$ , the result:  $Slice_{k+1}(n, V)$ 
  - 3.1 the conditional in  $c \in Cond_k n, V$  and
  - 3.2 those statement influencing the conditions of c
- 4. repeat 2 until a fixed-point

# (Inverse) Denominators

```
m \in IDen(n) (m inversely denominates n)
when m appears in all paths n \to \ldots \to n_t.
m = NIDen(n) (the nearest inverse denominator of n) when
m \in IDen(n) and
for all m' \in IDen(n) either m = m' or there is a simple path
m \to \ldots \to m'
m \in Infl(n) (m is influenced by n) when
m appears in a path from n to NIDen(n)
(m \neq n, m \neq NIDen(n), NIDen(n)) may not appear in the path).
```

- 1: Input(x)
- 2: Input(z)
- 3: if x < 10 then
- 4: z = z + 2;
- 5: **else**
- 6: z = z 1;
- 7: end if
- 8: Write(z)
- NIDen(1)? 2. Infl(1)?  $\emptyset$ .
- *NIDen*(2)? 3. *Infl*(2)? ∅.
- Observation, for sequential nodes  $Infl(n) = \emptyset$ .
- NIDen(3)? 7. Infl(3)?  $\{4,6\}$ .



# Slicing Structured Programs

```
Given a slicing criterion (n, V):
m \in Cond_{k+1}(n, V) (conditions influencing Slice_k(n, V)) when
  there exists m' \in Slice_k(n, V) and m' \in Infl(m).
v \in Relevant_{k+1}(m) when
  v \in Relevant_k(m) or
  there exists an m' \in Cond_{k+1}(n, V) and
    v \in Relevant_0(m) w.r.t. the slicing criterion (m', USE(m')).
m \in Slice_{k+1}(n, V) when
  m \in Cond_{k+1}(n, V) or
   there exists an m' such that m \to m' and
     DEF(m) \cap Relevant_{k+1}(m') \neq \emptyset.
```

Debugging

#### Slice wrt. $(8, \{z\})$ 1: Input(x) 2: Input(z) 3: if x < 10 then 4: z = z + 2: 5: else 6: z = z - 1: 7: end if

8: Write(z)

$$Slice_0(8, \{z\}) = \{2, 4, 6\}.$$

 $m \in Cond_{k+1}(n, V)$  (conditions influencing  $Slice_k(n, V)$ ) when there exists  $m' \in Slice_k(n, V)$  and  $m' \in Infl(m)$ .

```
Slice wrt. (8, \{z\})
```

- 1: Input(x)
- 2: Input(z)
- 3: if x < 10 then
- 4: z = z + 2;
- 5: **else**
- 6: z = z 1;
- 7: end if
- 8: Write(z)

$$Slice_0(8, \{z\}) = \{2, 4, 6\}.$$

$$Cond_1(8, \{z\}) = \{3\}$$

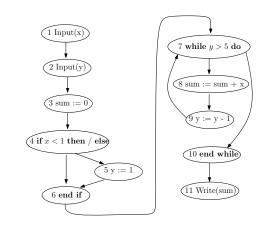
 $Slice_1(8, \{z\})?$ 

m	$Relevant_1(m)$	DEF(m)	$\in$ Slice <sub>1</sub> (8, {z})
1 Input(x)	Ø	{ <i>x</i> }	$\sqrt{}$
2 Input(z)	{ <b>x</b> }	$\{z\}$	$\sqrt{}$
3,5 <b>if</b> $x < 10$ <b>then</b> / <b>else</b>	$\{z, x\}$	Ø	×
4 z := z + 2	{z}	$\{z\}$	$\checkmark$
6 z := z - 1	{z}	$\{z\}$	$\sqrt{}$
7 end if	{z}	Ø	×
8 Write(z)	{z}	Ø	×
	{z}		

### Another Example

Slice wrt.  $(11, \{sum\})$ ?

- 1: Input(x)
- 2: Input(y)
- 3: sum := 0
- 4: **if** x < 1 **then**
- 5: y := 1
- 6: end if
- 7: while  $y \ge 1$  do
- 8: sum := sum + x
- 9: y := y 1
- 10: end while
- 11: Write(sum)



m	DEF(m)	Cond <sub>2</sub>	Rel <sub>2</sub>	Slice <sub>2</sub>	Slice <sup>(*)</sup>
1	{ <i>x</i> }	×	Ø		
2	{ <i>y</i> }	×	{x}		
3	{sum}	×	{ <i>x</i> , <i>y</i> }		
4	Ø		$\{sum, x, y\}$		
5	{ <i>y</i> }	×	$\{sum, x\}$		
6	Ø	×	$\{sum, x, y\}$	×	
7	Ø		$\{sum, x, y\}$		
8	{sum}	×	$\{sum, x, y\}$		
9	{ <i>y</i> }	×	$\{sum, x, y\}$		
10	Ø	×	{sum}	×	
11	Ø	×	{sum}	×	×

(\*) Syntactic check after generating the slice:

if then  $(/\text{else}) \in \textit{Slice} \Rightarrow (\text{the corresponding})$  end if  $\in \textit{Slice}$  while . . . do  $\in \textit{Slice} \Rightarrow (\text{the corresponding})$  end while  $\in \textit{Slice}$ 

. .

# The Ideal Slicing Algorithm?

Slice wrt.  $(2, \{x\})$ ?

- 1: Input(x)
- 2: x := x

Slice wrt.  $(5, \{x\})$ ?

- 1: **if** true **then**
- 2: x := 1
- 3: **else**
- 4: x := 2
- 5: end if

No algorithm for the smallest slice exists! Reason: Undecidability of halting/termination. Debugging Sequential Slicing Structured Slicing Automated Debugging Simplifying the Test-Case Isolating the Causes

### Slicing: Applications

- 1. Test adequacy: for each output variable, all du-paths in its slice must be covered
- Robustness testing: Add pseudo-variables that check dangerous situations, generate the slice and test
- Regression testing: testing if a change influences a particular component (i.e., if the slice of the component interface contains the change)
- Debugging: code review comparing a correct running program with a new faulty version

#### Automated Debugging is about Perfection

#### Perfection

Perfection is achieved not when you have nothing more to add, but when there is nothing more left to take away.

Antoine de Saint-Exupéry

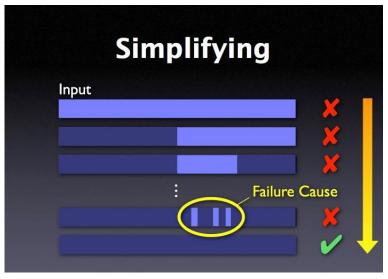
#### **Automated Debugging**

Take out all that has nothing to do with the failure...

#### Debugging: An Example

- ▶ My slides for today (in LATEX) did not compile
- some part of it did work before (older slides)
- divide the new parts into two:
  - 1. remove first half part
  - 2. if the problem is there, repeat until one (new) slide is left
  - 3. if not, put back the second half and and remove the first, repeat
- apply the same technique to the content of the remaining slide

This is called delta debugging: our order of business for today.



(Ack. figures are due to Andreas Zeller.)

# Minimizing Delta Debugging: Basic Idea

Try to find the minimal environment causing the failure by:

- ▶ Divide the circumstances C in n parts  $C_i$ ,
- remove a part  $C_i$  such that  $C \setminus C_i$  causes failure, repeat the algorithm with  $C \setminus C_i$ ,
- ▶ if no such part exists, choose a bigger n < |C| and repeat.

# Minimizing Delta Debugging: Formalization

- ► Circumstances: *C* (input but could be: program, environment, etc.)
- ▶ Test:  $test: 2^C \rightarrow \{\times, \checkmark, ?\}$
- ▶ Starting state:  $C_x \subseteq C$ , such that  $test(C_x) = x$
- ▶ Goal: find a minimal subset  $C'_{\times} \subseteq C_{\times}$  such that  $test(C'_{\times}) = \times$

# Minimizing Delta Debugging: Algorithm

 $ddmin(C_{\times}, 2)$ , where

$$ddmin(C'_{\times}, n) =$$

$$\begin{cases} C_{\times}', & \text{if } \mid C_{\times}' \mid = 1, \\ ddmin(C_{\times}' \setminus C_i, max(n-1,2)) & \text{else if } \exists_{i \leq n} test(C_{\times}' \setminus C_i) = \times \\ ddmin(C_{\times}', max(2n, \mid C_{\times}' \mid)) & \text{else if } n < \mid C_{\times}' \mid \\ C_{\times}' & \text{otherwise} \end{cases}$$

where  $C_i$ 's are partitions of  $C'_{\times}$  of (almost) equal size.

# Application in Random Testing

#### Idea

- feed huge inputs to the system (guaranteed crash on huge input)
- simplify input
- present the simplified result as a test-case

# Application in Random Testing

### **Examples**

- applied to command UNIX tools
- ► FLEX (lexical analyzer): crashed on a test-case of 2121 characters
- ► NROFF (document formatter): crashed on a single control character
- CRTPLOT (plotter output): crashed on single characters 't' or 'f'

### **Improvements**

- caching: save the test outcomes, use the saved data
- ▶ stop early: define a criterion to stop the algorithm, e.g.,
  - 1. no progress
  - 2. reaching a certain granularity
  - 3. upper bound on time
- use structures, e.g., blocks instead of characters
- differences vs. circumstances (compare sane with insane)

### What is a Cause?

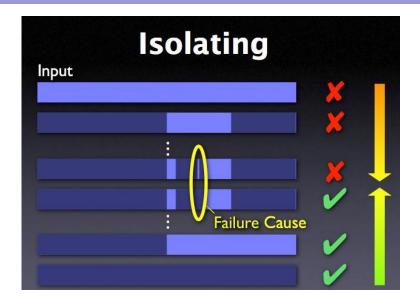
- ► Effect: the failure
- Cause: an event preceding effect,
   without which effect would not have happened

### Isolating the cause

- ► Cause: the minimal difference between the worlds with and without the failure
- ► Challenge: the world without failure: the goal of debugging
- ► Two solutions:
  - 1. manipulate the world by a debugger: turn infected to sane
  - 2. use another test-case in which no fault appears

# Isolating: The Sorting Program Case

- 1. ./sample produces a failure on 5 4 3 666666
- 2. works fine on 5 4 3
- 3. find combinations of
  - 3.1 states of 1 with 2 such that the program passes
  - 3.2 states of 2 with 1 such that the program fails
- 4. the difference between the two leads to a cause



### Delta Debugging: The Algorithm

#### Start from:

- $\triangleright$   $C_{\checkmark} = \emptyset$ : passing circumstances and
- $ightharpoonup C_{\times}$ : failing circumstances
- 1. compute the difference  $\Delta$  between the failing and the passing circ., divide into n parts:  $\Delta_i$ ,
- 2. remove  $\Delta_i$  from the failing circ.; it is the new passing circ., if it passes
- 3. add  $\Delta_i$  to the passing circ.; it is the new failing circ., if it fails
- 4. add  $\Delta_i$  to the passing circ.; it is the new passing circ., if it passes
- 5. remove  $\Delta_i$  from the failing circ.; it is the new failing circ., if it fails
- 6. increase *n* if none of the above holds
- 7. repeat until the difference is a singleton

## Delta Debugging: Algorithm

 $dd(C_{\checkmark}, C_{\times}, 2)$ , where  $ddmin(C_{\checkmark}', C_{\times}', n)$  is defined recursively as:

$$\begin{cases} (C'_{\checkmark},C'_{\times}) & \text{if } \mid \Delta \mid = 1, \\ dd(C'_{\times} \setminus \Delta_i,C'_{\times},2) & \text{else if } \exists_{i \leq n} test(C'_{\times} \setminus \Delta_i) = \checkmark \\ dd(C'_{\checkmark},C'_{\checkmark} \cup \Delta_i,2) & \text{else if } \exists_{i \leq n} test(C'_{\checkmark} \cup \Delta_i) = \times \\ dd(C'_{\checkmark} \cup \Delta_i,C'_{\times}, max(n-1,2)) & \text{else if } \exists_{i \leq n} test(C'_{\checkmark} \cup \Delta_i) = \checkmark \\ dd(C'_{\checkmark},C'_{\times} \setminus \Delta_i, max(n-1,2)) & \text{else if } \exists_{i \leq n} test(C'_{\times} \setminus \Delta_i) = \times \\ dd(C'_{\checkmark},C'_{\times}, min(2n,|\Delta|)) & \text{else if } n < |\Delta| \\ (C'_{\checkmark},C'_{\times}) & \text{otherwise} \end{cases}$$

where  $\Delta = C'_{\times} \setminus C'_{\checkmark}$  and  $\Delta_i$ 's are n partitions of  $\Delta$  of (almost) equal size.

Debugging

# Delta Debugging: Applied to Test-Case Simplification

#### Start from:

- $C_{\checkmark} = \emptyset$ : the empty test-case
- $ightharpoonup C_{\times}$ : the test-case leading to failure
- ▶ Much more efficient than minimizing delta debugging

# Delta Debugging: Applied to Regression Testing

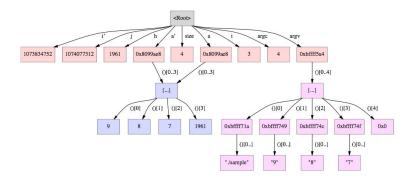
#### Start from:

- Goal: find out what went wrong in the new development (the old version worked well)
- $ightharpoonup C_{\checkmark} = \emptyset$ : basis is the old program, no changes needed
- ► C<sub>×</sub>: difference between the old and the new i.e., changes needed to obtain the new program from the old one

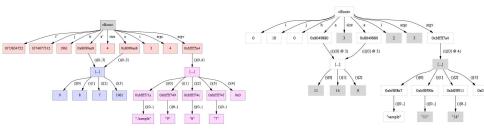
### Isolating the Cause: Idea

- ► Capture the state of the program
- Compare the states of a passes and a failed run
- ightharpoonup The smallest difference  $\Delta$  is the variable causing the problem
- ▶ Find out what influences this variable

### Program State: Memory Graphs



# Comparing the Differences



Implementable as debugger commands,
e.g., set variable size = 2.

### Isolating the Cause: Implementation

- ► Compute the common subgraph of the passing and failing memory graphs. Let the difference be  $C_{\times}$ .
- ▶ Implement  $C_{\times}$  as debugger commands.
- ▶ Apply delta-debugging to  $C_{\checkmark} = \emptyset$  and  $C_{×}$ 
  - 1. Apply differences to the memory graphs and test.
  - 2. At each step of *dd* if the changed state is not a valid state (program does not run), return ?, if it is a valid state, return the result of the test,
- The result Δ leads to a cause.

### Isolating the Cause: Sorting Case

Run the algorithm before calling shell\_sort with the state of ./sample 7 8 9 as passing and ./sample 11 14 as failing.

If 0 at the state: test fails  $\times$ , passes  $\checkmark$  otherwise.

- 1.  $C_{\times} = \{ a[], i, size, argc, argv[] \}, C_{\checkmark} = \emptyset.$
- 2. new failing state: a[], argv[1]  $\times$
- new passing state: argv[1] √
- new passing state: a[0] √
- 5. new passing state: a[0] and a[1] ✓
- 6.  $\Delta = \{ a[2] \}$

### Isolating the Cause: Illustrated Case

 $\blacksquare$  =  $\delta$  is applied,  $\square$  =  $\delta$  is *not* applied

#	a'[0] a[0] a'[1] a[1] a'[2] a[2] argc argv[1] argv[2] argv[3] i size											0	utput	Test
1												7	8 9	~
2												0	11	×
3												0	11 14	×
4												7	11 14	?
5												0	9 14	×
6												7	9 14	?
7												0	8 9	×
8												0	8 9	×
_														

Result

## Isolating the Chain of Causes

- Apply delta-debugging at the start, determine the minimal passing and running state
- Choose a common point (e.g., a function call) in the middle
- Apply delta-debugging on the states of the minimal passing and failing run
- ► Repeat the algorithm with the rest of the program and the new passing and failing states

# Finding the Culprits

- ▶ The previous algorithm gives different  $\Delta$ 's (causes at different points)
- Track the change of causes
- ► A smelling point: *a* ceases to be a cause and *b* becomes a cause

# **Automated Debugging**

- A natural mechanization of simple debugging principles
- Provides (partial) solutions to
  - 1. testing,
  - 2. simplifying the test-cases,
  - 3. isolating the causes and
  - 4. isolating the cause-effect chain.

## Notes on the Reading Material

- ▶ Covered: Chapters 5, 13 (apart from 13.6) and 14
- ► Chapters 1 and 12 provide background information
- Andreas Zeller's slides are also a very good source (see web page)
- Igor command-line tool can be downloaded from www.askigor.org (unfortunately, the debugging web-service is closed by now)