



**KTH Computer Science  
and Communication**

# **HSST 2015**

## **Learning-Based Testing for Procedural and Reactive Systems**

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# 0. Overview of the Course

## Part 1: Introduction to Learning-based Testing

1. Requirements Based Black-box Testing
2. Learning Based Testing Paradigm (LBT)
3. Two Frameworks for Study

based on: K. Meinke, F. Niu and M. Sindhua: *Learning-Based Software Testing: a Tutorial*, in: Proc. ISoLA 2011

# Overview

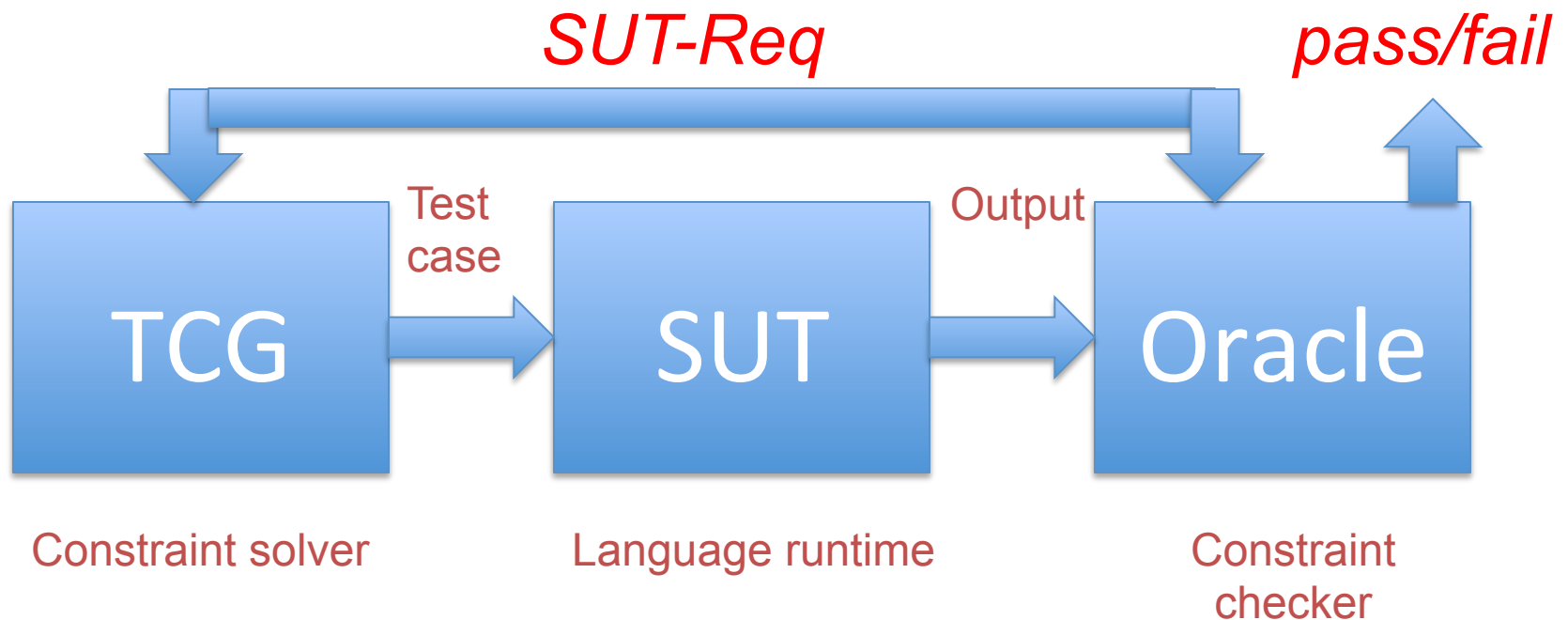
Part 2: LBT for reactive systems: theory

Part 3: LBT for reactive systems: praxis

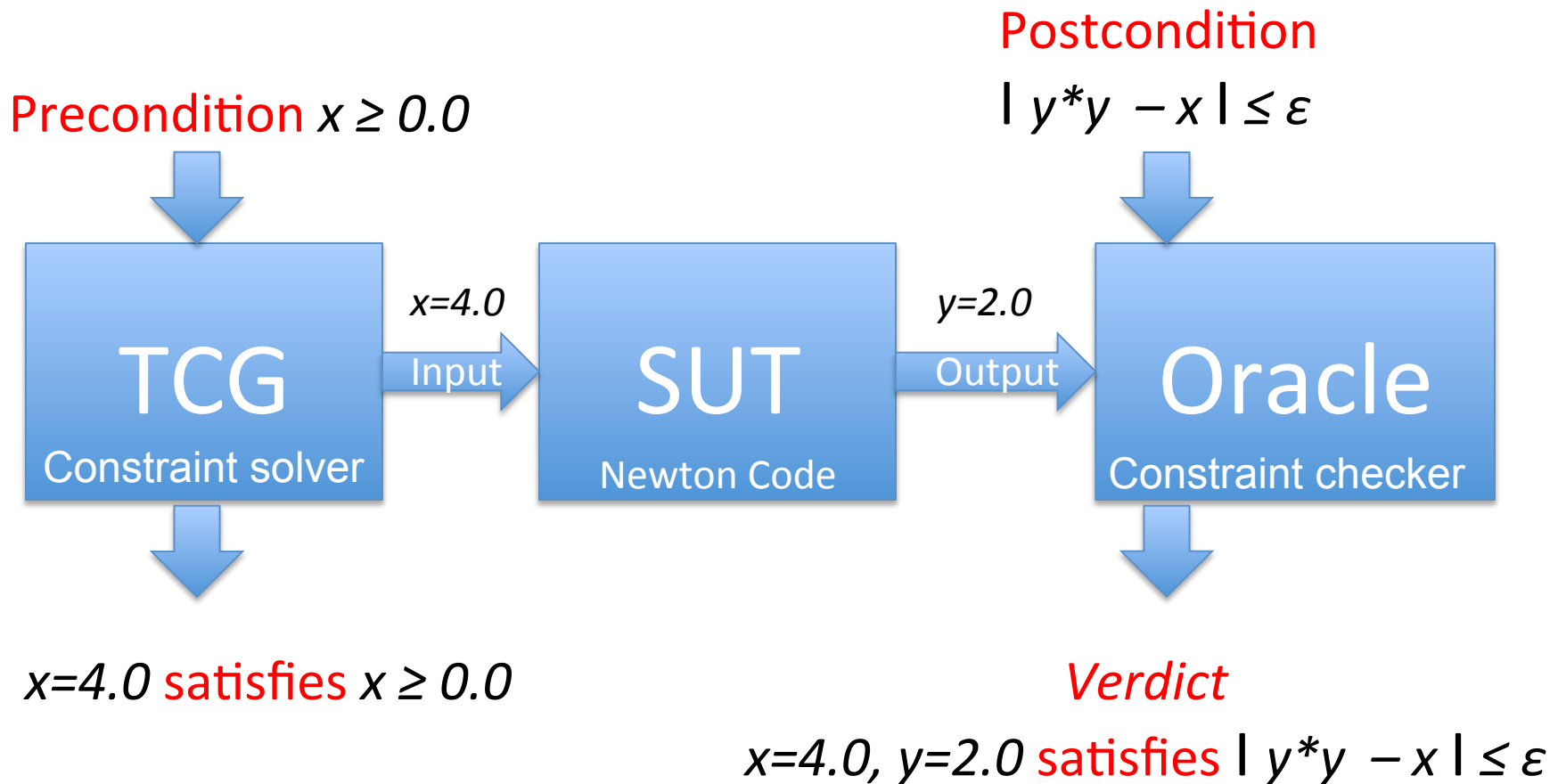
Part 4: LBT for procedural systems

# 1. Requirements Based Black-Box Testing

1. User requirement *SUT-Req*
2. System under Test *SUT*
3. Test verdict *pass/fail Oracle*



# 1.1. Procedural Code Example: *Newton's Square Root Algorithm*



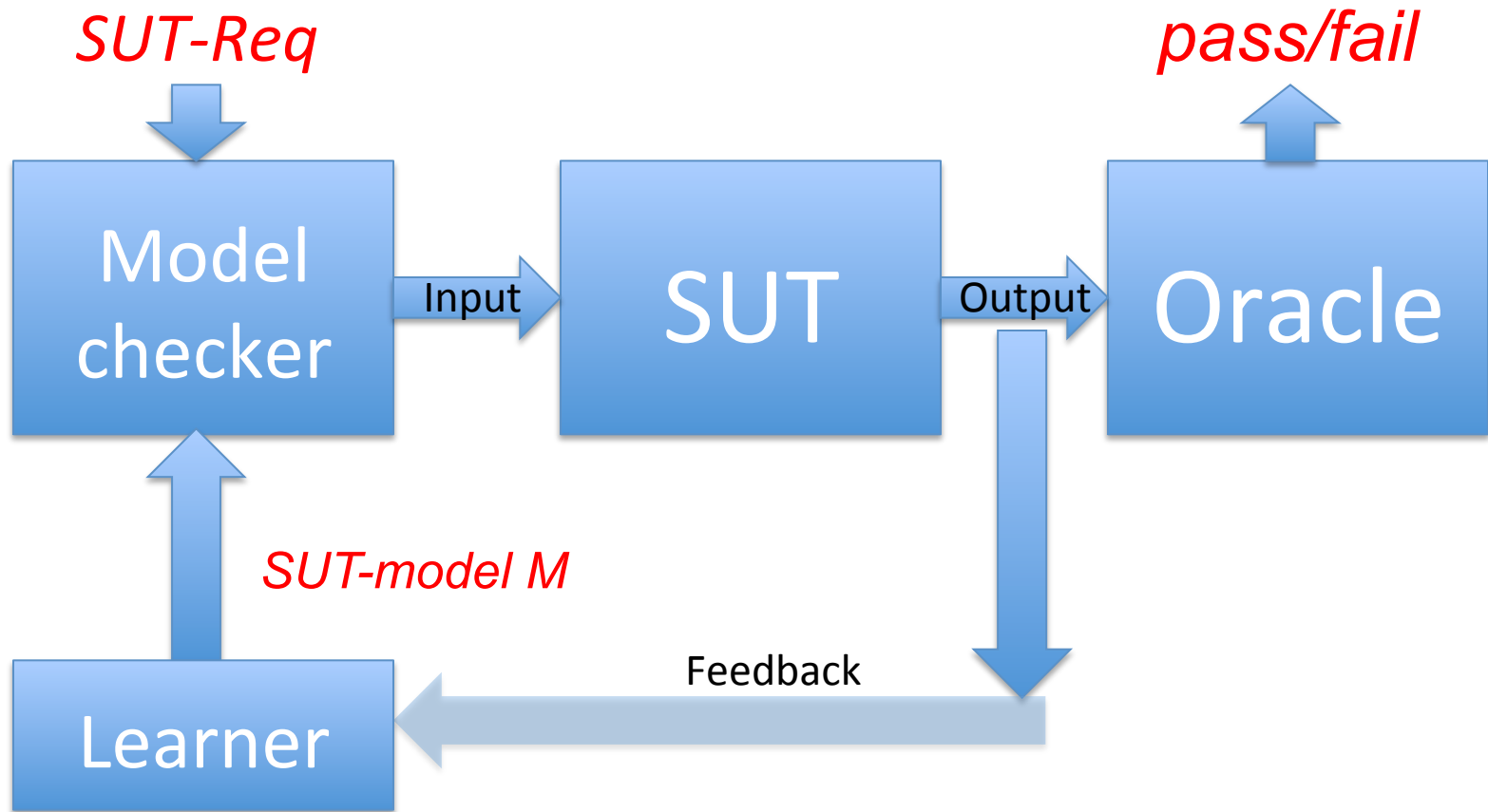
## 1.2. Key Problem: Feedback

**Problem:** How to modify this architecture to..

1. Improve next test case using previous test outcomes
2. Execute a large number of good quality tests?
3. Obtain good coverage?
4. Find bugs quickly?

# 2. Learning-Based Testing (LBT)

Meinke 2004, Proc. ISSTA-04



“*aka.* Model based testing without a model”

## 2.1. Basic Idea ...

LBT is a **search heuristic** that:

1. Partially and incrementally learns an SUT model
2. Uses generalisation (*inductive inference*) to predict unseen bugs!
3. Uses best prediction as next test case
4. Iteratively refines model according to each test outcome

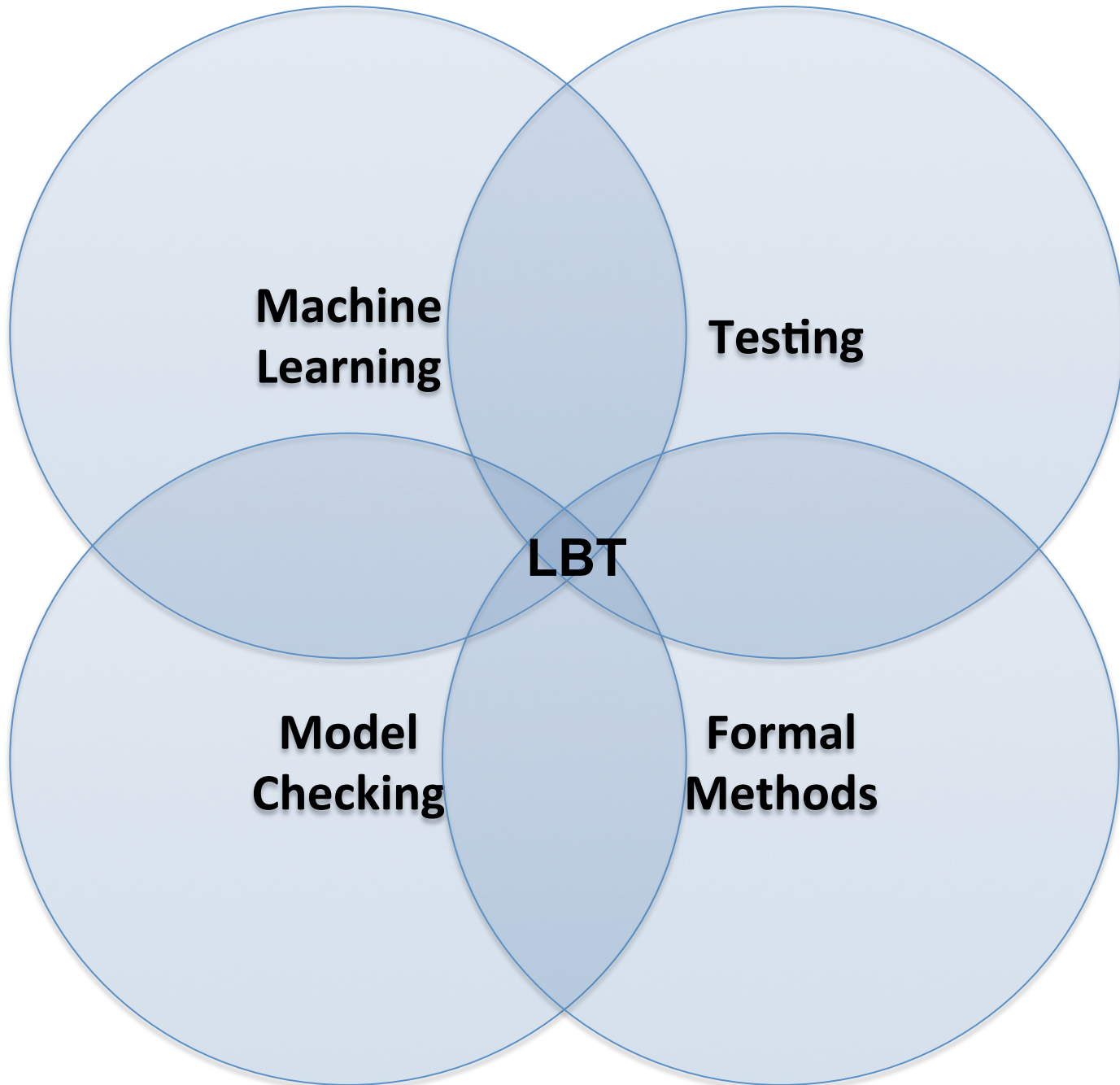


## 2.2. Abstract LBT Algorithm

1. Start from *null hypothesis*  $M_0$
2. For each  $k \geq 0$  do
  1. Model check  $M_k$  against *SUT-Req*
  2. Choose “**best counterexample**”  $i_{k+1}$  from step 2.1
  3. Execute  $i_{k+1}$  on SUT to produce  $o_{k+1}$
  4. if  $(i_{k+1}, o_{k+1})$  satisfies *!SUT-Req* label  $i_{k+1}$  as a bug
  5. Use  $(i_{k+1}, o_{k+1})$  to refine  $M_k$  to  $M_{k+1}$
  6. If *finished* break.

When Step 2.2 fails we fall back on:

- **Active learning queries**
- **Equivalence checking queries**



## 2.3. Technical Difficulties

General problem is to find **combinations** of  
*models, requirements languages and solvers* ( $M, L, S$ )  
so that ...

1. models  $M$  are:

- expressive,
- compact,
- partial and/or local (an abstraction method)
- easy to construct and learn
- behaviour is captured by  $L$

2.  $M$  and  $L$  are **feasible** to model check with  $S$

3. Supervised learning of  $M$  admits a notion of **convergence**

## 2.4. Convergence and Test Case Choice

- How **reliable** are counterexamples  $c_1, \dots, c_n$  ?
- Question of **false negatives**
- Some (parts of) SUTs more easily learned than others
- Measure **local convergence** around model points
- Convergence is a **proxy for model reliability** ...  
*“Counterexamples from locally well-converged regions are more reliable”*

## 2.5. Convergence and Coverage

- Convergence is also **proxy for coverage**
- If no counterexamples (  $n = 0$  )
  - choose point from least converged region (**breadth first search**)
- **Question:** *Do formal models of approximation and convergence always exist?*
- **Answer:** sometimes, but important exceptions also exist.

# 3. Two Frameworks for Study: Procedural Numerical Code

Generally **data-oriented testing**

1. Requirements Language – pre and postconditions  
– first-order logic of real-closed fields
2. Models  
– non-gridded  $n$ -dimensional piecewise polynomials
3. Model checker  
– Hoon-Collins CAD algorithm, (Mathematica)
4. Learning algorithm  
–  $n$ -dimensional polynomial interpolation

# *Framework 2: Reactive Systems*

Generally *control-oriented testing*

1. Requirements language = propositional linear temporal logic (PLTL)
2. Model = FSM, Moore machine
3. Model checker = BDD/SAT-based checkers
4. Learning = regular inference algorithms

# Why not Neural Networks?

Neural and deep neural networks have notable recent success ... but several problems here ...

1. NN are implicit continuous models unsuited to symbolic model checking
2. NN learning paradigm based on iterative training (*weight optimisation*) on big data

Testing does not fit this paradigm

Single test case can take 1-10 minutes!

3. NN models are statistical in character



# 5. Conclusions

- A promising approach ...
- Flexible general heuristic,
  - many models and requirement languages seem possible
- Many SUT types might be testable
  - procedural, reactive, real-time, hybrid etc.

## Open Questions

- Benchmarking?
- Scalability? abstraction, dimension reduction?
- Bottlenecks? model checking, learning, SUT?