Functional Testing

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http://ceres.hh.se/mediawiki/DIT085

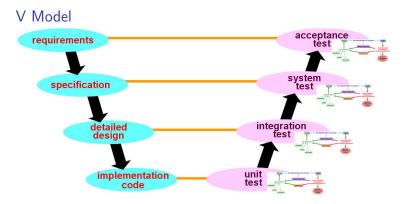
Testing and Verification (DIT085), Chalmers and GU, January 30, 2015



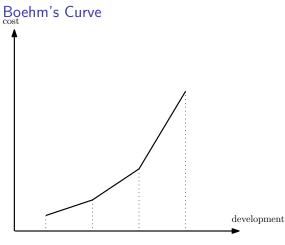
Announcements

- ► Groups: 62 people registered in GUL (fewer sent emails); you need to register in order to get evaluated.
- ► Final Exam: March 17 at 08:30, Closed book
- Supervised instructions: from 13:00 to 16:45
- ► FAQ: http://ceres.hh.se/mediawiki/DIT085_FAQ_2015
- ► Tools: slight changes in the tools for Phase 2; check the course page.

When?



When?



requirement specification design implementation



Outline

Introduction

Equivalence Class Testing

Decision Tables

Classification Trees

Conclusions

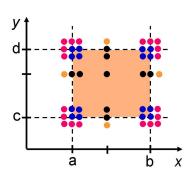
Functional Testing

- functional testing: program is an input from a certain domain to a certain range
- impossible to check all input/output combinations: defining a coverage criterion to choose some some



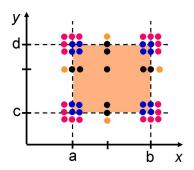
Boundary Value Testing

 boundary value testing: a test case for each combination of extreme (normal, out of bound) values



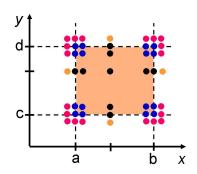
Boundary Value Testing: Pros and Cons

- + straightforward test-case generation
 - no sense of covering the input domain
 - awkward for logical vars.
 - only independent input domains
 - not using white-box information



Boundary Value Testing: Pros and Cons

- + straightforward test-case generation
 - no sense of covering the input domain *
 - awkward for logical vars. *
 - only independent input domains *
 - not using white-box information
- *: Today's order of business.



Outline

Introductio

Equivalence Class Testing

Decision Table

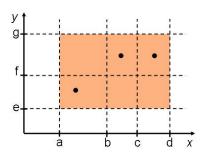
Classification Trees

Conclusions

Conclusions

Weak Normal EC: Idea

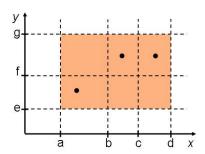
- Define equivalence classes on the domain (range) of input (output) for each variable: (independent input)
- cover equivalence classes for the domain of each variable: single fault assumption
- how many test-cases are needed?
- also called: (equivalence, category) partition method





Little Puzzle

What is the minimal number of tokens that are needed to be put in an $m \times n$ grid such that each row and column contains at leats one token?

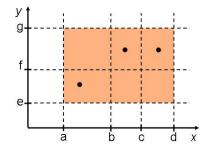


Little Puzzle

What is the minimal number of tokens that are needed to be put in an $m \times n$ grid such that each row and column contains at leats one token?

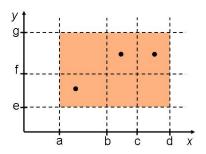
max(m,n):

Put token number i at (max(i, m), max(i, n)).



Weak Normal EC: Idea

- Define equivalence classes on the domain (range) of input (output) for each variable: (independent input)
- cover equivalence classes for the domain of each variable: single fault assumption
- ► how many test-cases are needed? $\max_{x} |S_{x}|$.





Mortgage Example (recap)

Introduction

Spec. Write a program that takes three inputs: gender (boolean), age([18-55]), salary ([0-10000]) and output the total mortgage for one person

Mortgage = salary * factor, where factor is given by the following table.

Category	Male	Female
Young	(18-35 years) 75	(18-30 years) 70
Middle	(36-45 years) 55	(31-40 years) 50
Old	(46-55 years) 30	(41-50 years) 35



Weak Normal EC Testing

Category	Male	Female
Young	(18-35 years) 75	(18-30 years) 70
Middle	(36-45 years) 55	(31-40 years) 50
Old	(46-55 years) 30	(41-50 years) 35

- age: difficult!
- ► salary: [0-10000]
- male: as strange as boundary value!

Weak Normal EC Testing

Category	Male	Female
Young	(18-35 years) 75	(18-30 years) 70
Middle	(36-45 years) 55	(31-40 years) 50
Old	(46-55 years) 30	(41-50 years) 35

- ▶ age: difficult! [18-30], [31-35], [36-40], [41,45], [46-50], [51-55]
- salary: [0-10000]
- male: as strange as boundary value! true, false



Weak Normal EC Testing

Introduction

if (male) then return

```
((18 \le age < 35)?(75 * salary) : (31 \le age < 40)?(55 * salary) : (30 * salary))
```

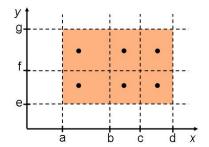
else return $((18 \le age < 30)?(75 * salary) : (31 \le age < 40)?(50 * salary) : (35 * salary))$

	((8- \/-	()).(8- \).())	()))
Gender	Age	Salary	Output	Correct Out.	Pass/Fail
male	20	1000	75*1000	75*1000	Р
female	32	1000	50*1000	50*1000	Р
male	38	1000	55*1000	50*1000	Р
female	42	1000	35*1000	35*1000	Р
male	48	1000	30*1000	30*1000	Р
female	52	1000	35*5000	too latel	F

Conclusions

Strong Normal EC Testing

- cover the all combinations of equivalence classes for the domain of all variables: multiple fault assumption
- ▶ number of test-cases? $\prod_{x} |S_{x}|$



Strong Normal EC Testing

Male	Female
(18-35 years) 75	(18-30 years) 70
(36-45 years) 55	(31-40 years) 50
(46-55 years) 30	(41-50 years) 35
	(18-35 years) 75 (36-45 years) 55

- ▶ age: [18-30], [31-35], [36-40], [41,45], [46-50], [51-55]
- salary: [0-10000]
- male: true, false



if (male) then return

```
((18 \le age < 35)?(75 * salary) : (31 \le age < 40)?(55 * salary) : (30 * salary))
```

else return $((18 \le age < 30)?(75 * salary) : (31 \le age < 40)?(50 * salary) : (35 * salary))$

Gender	Age	Salary	Output	Correct Out.	Pass/Fail
female	20	1000	75*1000	70*1000	F
female	32	1000	50*1000	50*1000	Р
female	38	1000	50*1000	50*1000	Р
female	42	1000	35*1000	35*1000	Р
female	48	1000	35*1000	35*1000	Р
female	52	1000	35*5000	too late!	F

Strong Normal EC Testing

Introduction

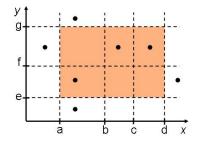
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((18 \le age < 35)?(75 * salary) : (31 \le age < 40)?(55 * salary) : (30 * salary))
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else return $((18 \le age < 30)?(75 * salary) : (31 \le age < 40)?(50 * salary) : (35 * salary))$

Gender	Age	Salary	Output	Correct Out.	Pass/Fail
male	20	1000	75*1000	75*1000	Р
male	32	1000	50*1000	75*1000	F
male	38	1000	55*1000	50*1000	Р
male	42	1000	30*1000	55*1000	F
male	48	1000	30*1000	30*1000	Р
male	52	1000	30*1000	30*1000	Р

- includes weak normal; adds out of range test-cases for each variable
- ► number of test-cases? $(\max_x | S_x |) + 2 * n$



Weak Robust EC Testing

if (male) then return

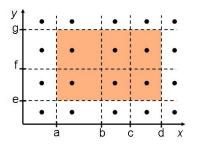
```
((18 \le age < 35)?(75 * salary) : (31 \le age < 40)?(55 * salary) : (30 * salary))

else return ((18 \le age < 30)?(75 * salary) : (31 \le age < 40)?(50 * salary) : (35 * salary))
```

	((8- \/-	()) . (-8- () ())	()))
Gender	Age	Salary	Output	Correct Out.	Pass/Fail
male	17	1000	30*1000	too young!	F
female	56	1000	35*1000	too late	F
male	36	-1	55*-1	0	F
female	36	10001	50*10001	50*10000	F

Strong Robust EC

- Same as strong normal but also checks for all out of range combinations
- ▶ number of test-cases? $\prod_{x} (|S_x| + 2)$



Strong Robust EC

if (male) then return

```
((18 \le age < 35)?(75 * salary) : (31 \le age < 40)?(55 * salary) : (30 * salary))

else return ((18 \le age < 30)?(75 * salary) : (31 \le age < 40)?(50 * salary) : (35 * salary))
```

Mostly similar faults to Weak Robust EC:

Gender	Age	Salary	Output	Correct Out.	Pass/Fail
male	17	1000	30*1000	too young!	F
female	56	1000	35*1000	too late	F
female	17	1000	35*1000	too young!	F
male	56	1000	30*1000	too late	F
male	36	-1	55*-1	0	F
female	36	10001	50*10001	50*10000	F

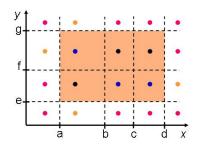
. . .



A Brief Comparison

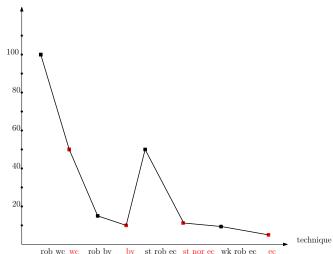


 $A \rightarrow B$: Test-cases of A (faults detected by A) is a subset of those of B.

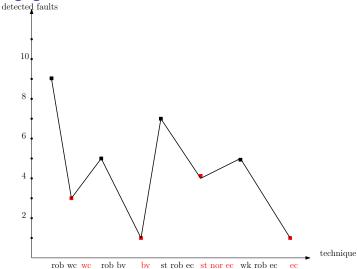


Mortgage Case: #Test-Cases

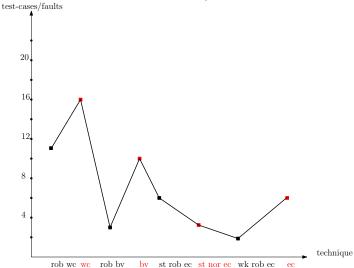
test-cases/faults



Mortgage Case: Detected Fault

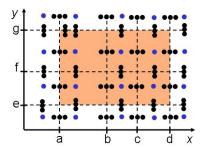


Mortgage Case: #Test-Cases/Fault



Idea

- ► Considering the boundaries of each partition relevant
- Example: Robust worst case testing of of partitions



Strong Robust EC + Robust BV

Gender	Age	Salary	Output	Correct Out.	Pass/Fail
male	17	-1	30*-1	too young!	F 1
male	17	1000	30*1000	too young!	F 1
male	17	10001	30*10001	too young!	F 1
male	56'	-1	30*-1	too late	F 2
male	56	1000	30*1000	too late	F 2
male	56	10001	30*10001	too late	F 2
female	17	-1	30*-1	too young!	F 3
female	17	1000	30*1000	too young!	F 3
female	17	10001	30*10001	too young!	F 3
female	56	-1	30*-1	too late	F 4
female	56	1000	30*1000	too late	F 4
female	56	10001	30*10001	too late	F 4



Gender	Age	Salary	Output	Correct Out.	Pass/Fail
female	18	1000	75*1000	70*1000	F 5
female	19	1000	75*1000	70*1000	F 5
female	20	1000	75*1000	70*1000	F 5
female	29	1000	75*1000	70*1000	F 5
female	30	1000	35*1000	70*1000	F 6
female	31	1000	50*1000	50*1000	Р
female	32	1000	50*1000	50*1000	Р
female	34	1000	50*1000	50*1000	Р
female	35	1000	50*1000	50*1000	Р
female	36	1000	50*1000	50*1000	Р
female	38	1000	50*1000	50*1000	Р
female	39	1000	50*1000	50*1000	Р
female	40	1000	35*1000	50*1000	F 7

Gender	Age	Salary	Output	Correct Out.	Pass/Fail
female	41	1000	35*1000	35*1000	Р
female	42	1000	35*1000	35*1000	Р
female	44	1000	35*1000	35*1000	Р
female	45	1000	35*1000	35*1000	Р
female	46	1000	35*1000	35*1000	Р
female	49	1000	35*1000	35*1000	Р
female	50	1000	35*1000	35*1000	Р
female	51	1000	35*1000	too late!	F 7
female	52	1000	35*1000	too late!	F 7
female	53	1000	35*1000	too late!	F 7
female	54	1000	35*1000	too late!	F 7
female	55	1000	35*1000	too late!	F 7



Age	Salary	Output	Correct Out.	Pass/Fail
18	1000	75*1000	75*1000	Р
19	1000	75*1000	75*1000	Р
20	1000	75*1000	75*1000	Р
29	1000	75*1000	75*1000	Р
30	1000	75*1000	75*1000	Р
31	1000	55*1000	75*1000	F 8
32	1000	55*1000	75*1000	F 8
34	1000	55*1000	75*1000	F 8
35	1000	55*1000	75*1000	F 9
36	1000	55*1000	55*1000	Р
38	1000	55*1000	55*1000	Р
39	1000	55*1000	55*1000	Р
40	1000	55*1000	20*1000	F 10
	18 19 20 29 30 31 32 34 35 36 38 39	18 1000 19 1000 20 1000 29 1000 30 1000 31 1000 32 1000 34 1000 35 1000 36 1000 38 1000 39 1000	18 1000 75*1000 19 1000 75*1000 20 1000 75*1000 29 1000 75*1000 30 1000 75*1000 31 1000 55*1000 32 1000 55*1000 34 1000 55*1000 35 1000 55*1000 36 1000 55*1000 38 1000 55*1000 39 1000 55*1000	18 1000 75*1000 75*1000 19 1000 75*1000 75*1000 20 1000 75*1000 75*1000 29 1000 75*1000 75*1000 30 1000 75*1000 75*1000 31 1000 55*1000 75*1000 32 1000 55*1000 75*1000 34 1000 55*1000 75*1000 35 1000 55*1000 75*1000 36 1000 55*1000 55*1000 38 1000 55*1000 55*1000 39 1000 55*1000 55*1000



Gender	Age	Salary	Output	Correct Out.	Pass/Fail
male	41	1000	30*1000	30*1000	Р
male	42	1000	30*1000	30*1000	Р
male	44	1000	30*1000	30*1000	Р
male	45	1000	30*1000	30*1000	Р
male	46	1000	30*1000	30*1000	Р
male	49	1000	30*1000	30*1000	Р
male	50	1000	30*1000	30*1000	Р
male	51	1000	30*1000	30*1000	Р
male	52	1000	30*1000	30*1000	Р
male	53	1000	30*1000	30*1000	Р
male	54	1000	30*1000	30*1000	Р
male	55	1000	30*1000	30*1000	Р



Strong Robust EC + Robust BV (Cont'd)

Gender	Age	Salary	Output	Correct Out.	Pass/Fail
female	17	-1	35*-1	0	F 11
female	18	-1	75*-1	0	F 11

Strong Robust EC + Robust BV (Cont'd)

Gender	Age	Salary	Output	Correct Out.	Pass/Fail
female	17	10001	35*10001	too young!	F 11
female	18	10001	75*10001	75*10000	F 12

. . .

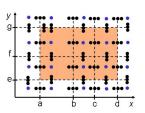
Strong Robust EC + Robust BV (Cont'd)

Gender	Age	Salary	Output	Correct Out.	Pass/Fail
male	17	-1	30*-1	0	F 12
male	18	-1	70*-1	0	F 12

. . .

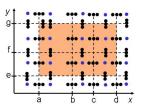
Gender	Age	Salary	Output	Correct Out.	Pass/Fail
male	17	10001	30*10001	too young!	F 12
male	18	10001	70*10001	75*10000	F 12

. . .



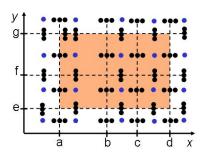
Problems

- >100 test-cases for the mortgage example
- ► too many for any real-life program e.g., 5 vars., each 5 partitions:
 - \sim 8 million test-cases
 - 1 sec. for each test-case:
 - 3 months testing!



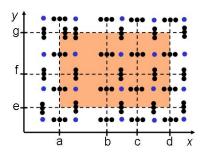
Problems

- ▶ Problems:
 - No constraints on the equivalence classes
 - 2. Dependencies among different variables not taken into account
 - No choice among relevant classes (e.g., apply worst-case testing on some and boundary values on others)
- Solutions: Decision tables, classification trees



Problems

- ▶ Problems:
 - No constraints on the equivalence classes
 - Dependencies among different variables not taken into account
 - No choice among relevant classes (e.g., apply worst-case testing on some and boundary values on others)
- Solutions: Attend the coming lecture!



Introduction

- Pairwise testing: for each two variables and each two partitions of their valuations, there is at least one test case
- ► T-wise testing: for each T variables and each T partitions of their valuations, there is at least one test case

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Classification Trees

Conclusions

ldea

- ► Goal: Summarize the logic of the program (à la Karnaugh maps)
- ► Find a few conditions on input determining the output behavior need not be independent relaxing the independence assumption in all previous techniques
- Determine the output actions for each combination of condition evaluations
- also called: cause-effect graph testing, or tableau testing



► Stub:

- condition part the most dominating conditions first multi-valued conditions and special cases last
- action part exceptions preferably combined actions as new rows

Stub	Entry							
c1	F	Т	Т					
c2	-	F	Т					
c3	-	-	F					
a1	X	-	-					
a2	-	X	-					
a1;a2	-	-	Χ					

- Entry
 - columns are called rules
 - condition part: true, false, (possibly other values) or don't care
 - action part

Stub	Entry								
c1	F	Т	Т						
c2	-	F	Т						
c3	-	-	F						
a1	Х	-	-						
a2	-	Х	-						
a1;a2	-	_	Χ						

- Completeness check for independent variables
 - each don't care counts for two rules
 - there must be $2^{|\{c_i\}|}$ rules (for n_i -valued conditions: $\prod_i n_i$)

c1	F	Т	Т
c2	-	F	Т
c3	-	-	F
a1	Х	_	-
a2	-	X	-
a1;a2	-	-	Χ



- Completeness check for independent variables
 - each don't care counts for two rules
 - there must be $2^{|\{c_i\}|}$ rules (for n_i -valued conditions: $\prod_i n_i$)

c1	F	T	Т	Т
c2	-	F	Т	Т
c3	-	-	F	Т
a1	X	_	-	_
a2	_	X	-	-
a1;a2	_	_	Χ	-
error	-	-	-	Χ



Cor	nditions/Actions									
c7:	0≤salary≤10000?	n	у	у	у	у	у	у	у	у
c1:	male?	-	_	_	у	у	у	n	n	n
c2:	too young? [,18]	-	у	_	_	_	-	-	_	-
c3:	young? m:[18,,35], f:[18,,30]	-	_	_	у	_	-	у	_	-
c4:	mid? m:[36,,45], f:[31,,40]	_	_	-	_	у	-	-	у	-
c5:	old? m:[46,,55], f:[40,,50]	-	_	-	_	_	у	-	-	у
c6:	too old? m:[56,], f:[51,]	-	_	у	_	_	-	-	-	-
a1:	wrong inputs	Х	Χ	Χ	_	_	_	_	_	-
a2:	75*salary	-	_	_	Χ	_	-	_	_	-
a3:	70*salary	-	_	-	_	_	-	Х	-	-
a4:	55*salary	-	_	-	_	Χ	-	_	-	-
a5:	50*salary	-	_	_	_	_	-	_	Χ	-
a6:	35*salary	-	_	_	_	_	_	_	_	X
a7:	30*salary	-	_	_	_	_	Х	_	-	-
'					4.0	N 4 5	1 6 4	= 1 4	= 1	

Introduction

Decision Table for Testing

Introduction

variables: Physical or Logical	Р	Р	Р	Р	Р	L	L	L	L	L
Independent?	У	у	у	У	n	у	у	У	у	n
Single fault assum.?	У	у	n	n	-	у	у	n	n	-
Exception handling?	У	n	у	n	-	у	n	у	n	_
BV		X								
Robust	Χ									
WC				Х						
Robust WC			X							
EC							Χ			
Strong (Normal) EC									Χ	
(Weak) Robust EC						Χ				
Strong Robust EC								Χ		
Decision Table					Х					X



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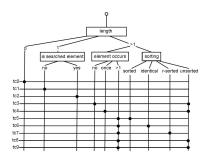
Conclusions

Conclusions

Basic Steps

Classification tree:

- Determine the aspects of specification influencing the logic
- Establish a hierarchy between aspects (the more global conditions first)
- Partition the input domain for each aspect cover the whole domain of the "parent" node

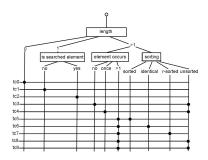




Basic Steps

Combination table:

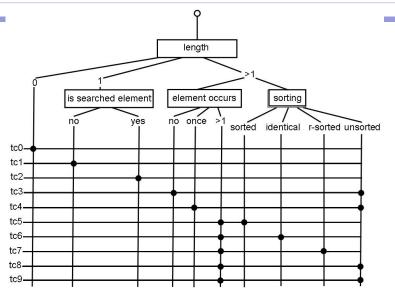
 Define a test-case for each relevant combination of inputs



Introduction

Informal Spec

Consider the function count(list: List(EI), eI: EI): int, which takes a list of elements (with an order defined on them), and an element and output the number of occurrences of the element in the list.



Mortgage Example

Classes

- 1. Salary: -1, [0..10000], >10000,
- 2. Gender: Male, Female,
- 3. Age: Too young, Young, Middle, Old, Too old (dependent on gender)

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Functional Testing

- Equivalence testing forms the basis:
 - Strong variants are often practically infeasible
 - ▶ Robust techniques are very effective for PL's with weak typing
- Decision tables and classification trees, help us in:
 - 1. summarizing the logic
 - identifying and documenting the effective methods and test-cases.

One Sentence to Take Home

No perfect functional testing technique exists:

classification tree (or DT)

augmented with coverage information (to iteratively add test cases) should provide an effective mix.