

Declarative Disambiguation of Deep Priority Conflicts

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Python Expression Syntax

```
star_expr: '*' expr
expr: xor_expr ('|' xor_expr)*
xor_expr: and_expr ('^' and_expr)*
and_expr: shift_expr ('&' shift_expr)*
shift_expr: arith_expr (('<<' | '>>') arith_expr)*
arith_expr: term (('+' | '-') term)*
term: factor (('*' | '@' | '/' | '%' | '//') factor)*
factor: ('+' | '-' | '~') factor | power
power: atom_expr ['**' factor]
atom_expr: [AWAIT] atom trailer*
atom: ('(' [yield_expr|testlist_comp] ')') |
      '[' [testlist_comp] ']' |
      '{' [dictorsetmaker] '}' |
      NAME | NUMBER | STRING+ | '...' | 'None' | 'True' | 'False')
```

<https://docs.python.org/3/reference/grammar.html>

Associativity and Precedence in YACC

```
%right '='
%left '+' '-'
%left '*' '/'
```

```
%%
```

```
expr      :      expr '=' expr
          |      expr '+' expr
          |      expr '-' expr
          |      expr '*' expr
          |      expr '/' expr
          |      NAME
          ;
```

Semantics of Disambiguation in YACC

The precedences and associativities are used by Yacc to resolve parsing conflicts; they give rise to disambiguating rules. Formally, the rules work as follows:

1. The precedences and associativities are recorded for those tokens and literals that have them.
2. A precedence and associativity is associated with each grammar rule; it is the precedence and associativity of the last token or literal in the body of the rule. If the `%prec` construction is used, it overrides this default. Some grammar rules may have no precedence and associativity associated with them.
3. When there is a reduce/reduce conflict, or there is a shift/reduce conflict and either the input symbol or the grammar rule has no precedence and associativity, then the two disambiguating rules given at the beginning of the section are used, and the conflicts are reported.
4. If there is a shift/reduce conflict, and both the grammar rule and the input character have precedence and associativity associated with them, then the conflict is resolved in favor of the action (shift or reduce) associated with the higher precedence. If the precedences are the same, then the associativity is used; left associative implies reduce, right associative implies shift, and nonassociating implies error.

<http://dinosaur.compilertools.net/yacc/>

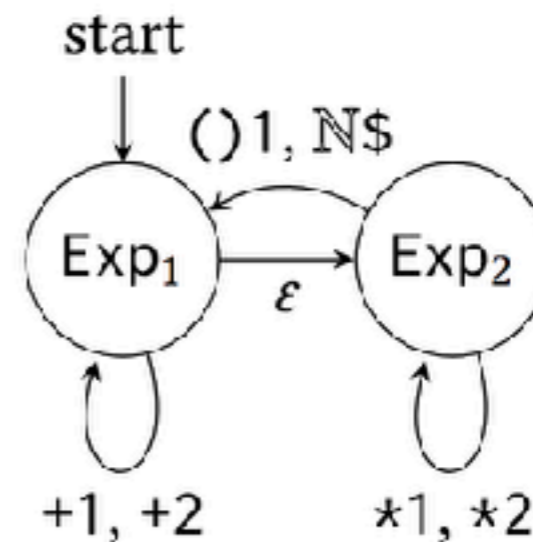
Disambiguation with Tree Automata



(a) Violating pattern



(b) Violating pattern



(c) Automaton

$((+(\square, \square))^* \cdot$
 $(*(\square, \square))^* \cdot$
 $(N() \mid () (\square))^*$

(d) Regular expression

$\text{Exp}_1 \rightarrow + \text{Exp}_1 \text{Exp}_1$
 $\text{Exp}_1 \rightarrow \epsilon \text{Exp}_2$

$\text{Exp}_2 \rightarrow N \epsilon$
 $\text{Exp}_2 \rightarrow * \text{Exp}_2 \text{Exp}_2$
 $\text{Exp}_2 \rightarrow () \text{Exp}_1$

(e) Tree rewrites

What is the *direct* semantics of associativity and priority?

SDF2 Semantics

[Visser 1997]

Declarative Disambiguation in SDF3

context-free syntax

Exp.Add = Exp "+" Exp {left}

Exp.Mul = Exp "*" Exp {left}

Exp.Int = INT

context-free priorities

Exp.Mul > Exp.Add

SDF2 Semantics

$$\frac{A.C_1 = \alpha B \gamma > B.C_2 = \beta \in \text{Pr}(G)}{[A.C_1 = \alpha[C_2]\gamma] \in Q_G}$$

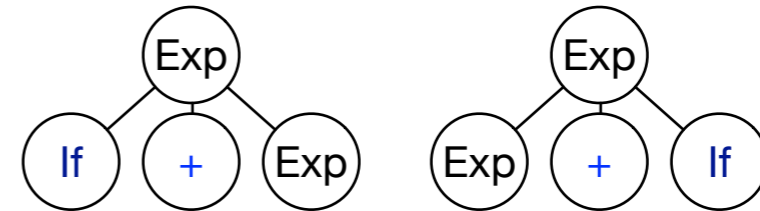
context-free syntax

Exp.Add = Exp "+" Exp

Exp.If = "if" "(" Exp ")" Exp

context-free priorities

Exp.Add > Exp.If



SDF2 Semantics

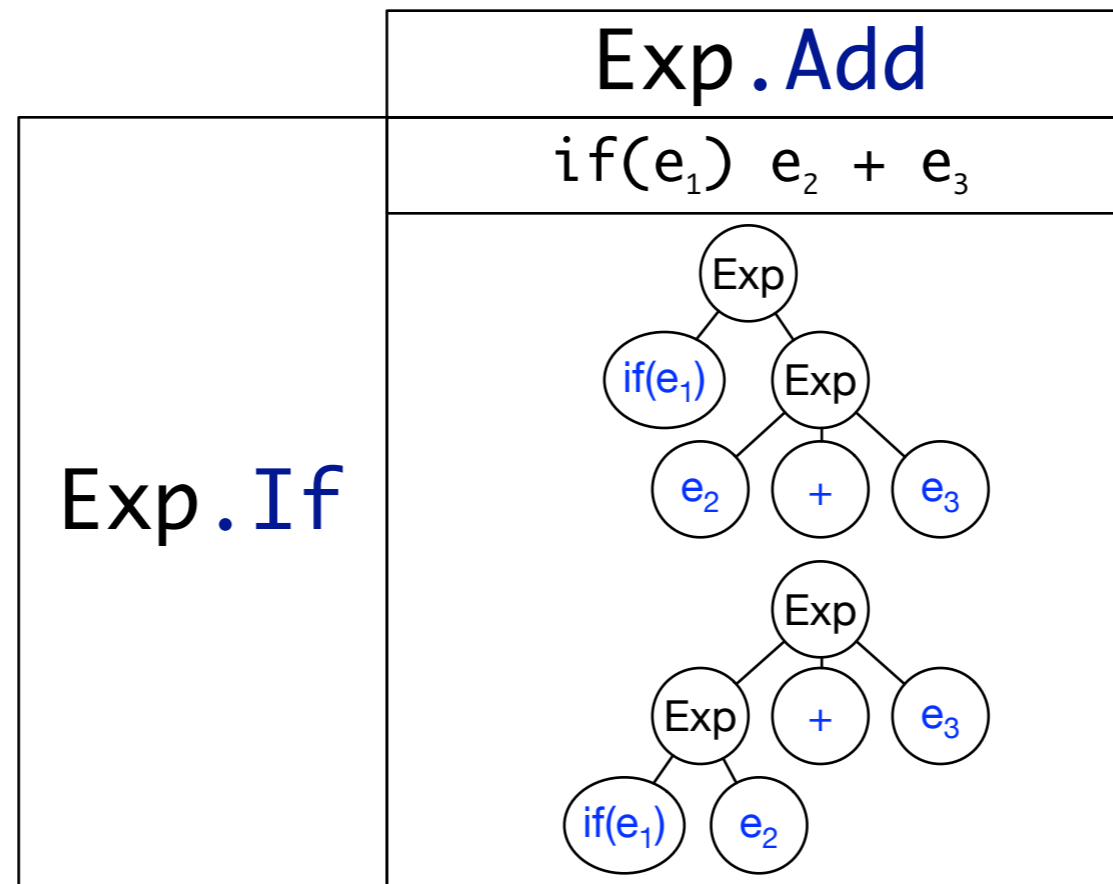
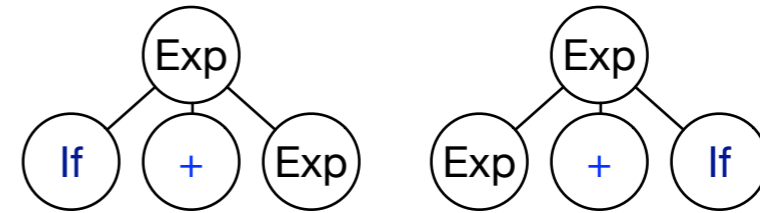
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context-free syntax

Exp.Add = Exp "+" Exp
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context-free priorities

Exp.Add > Exp.If



SDF2 Semantics

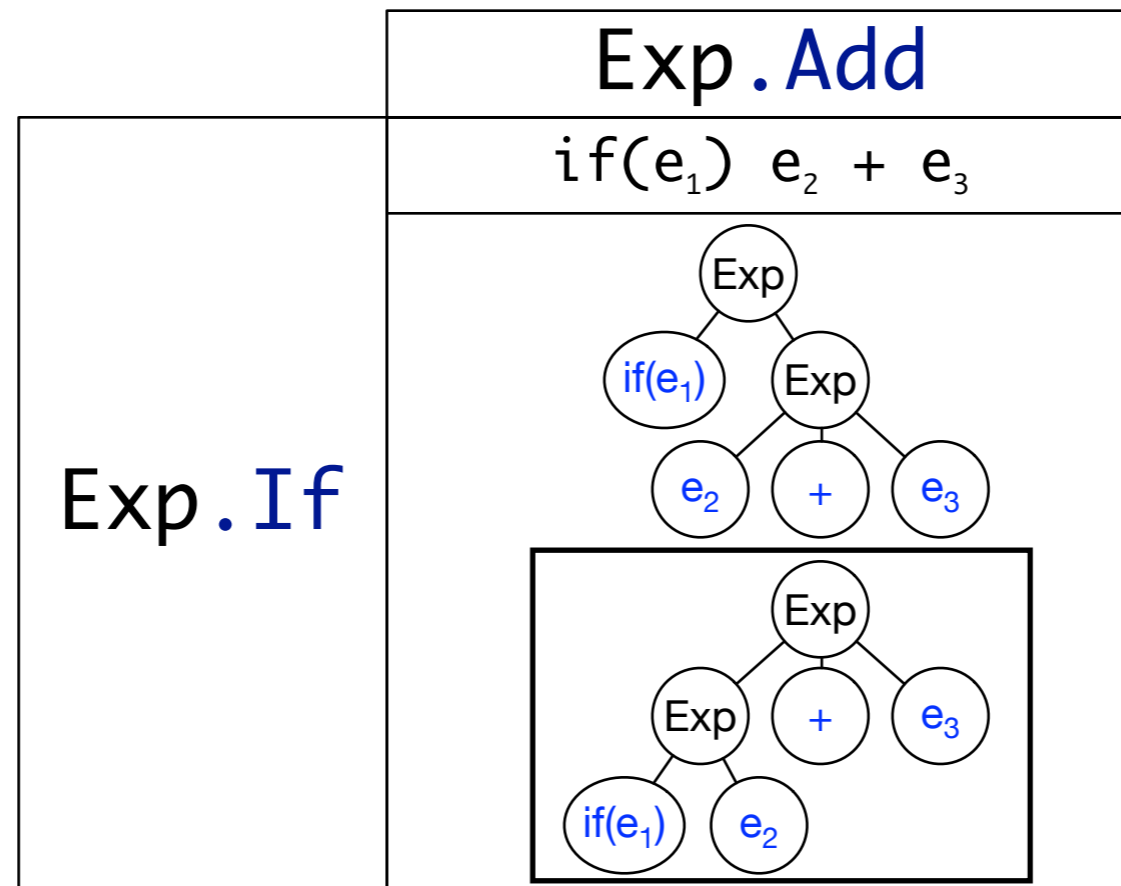
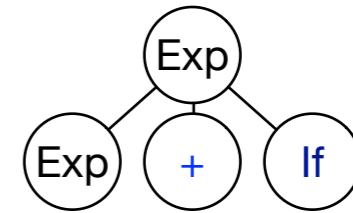
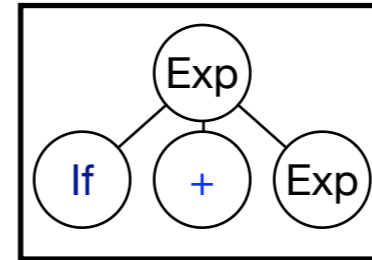
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context-free priorities

Exp.Add > Exp.If



SDF2 Semantics

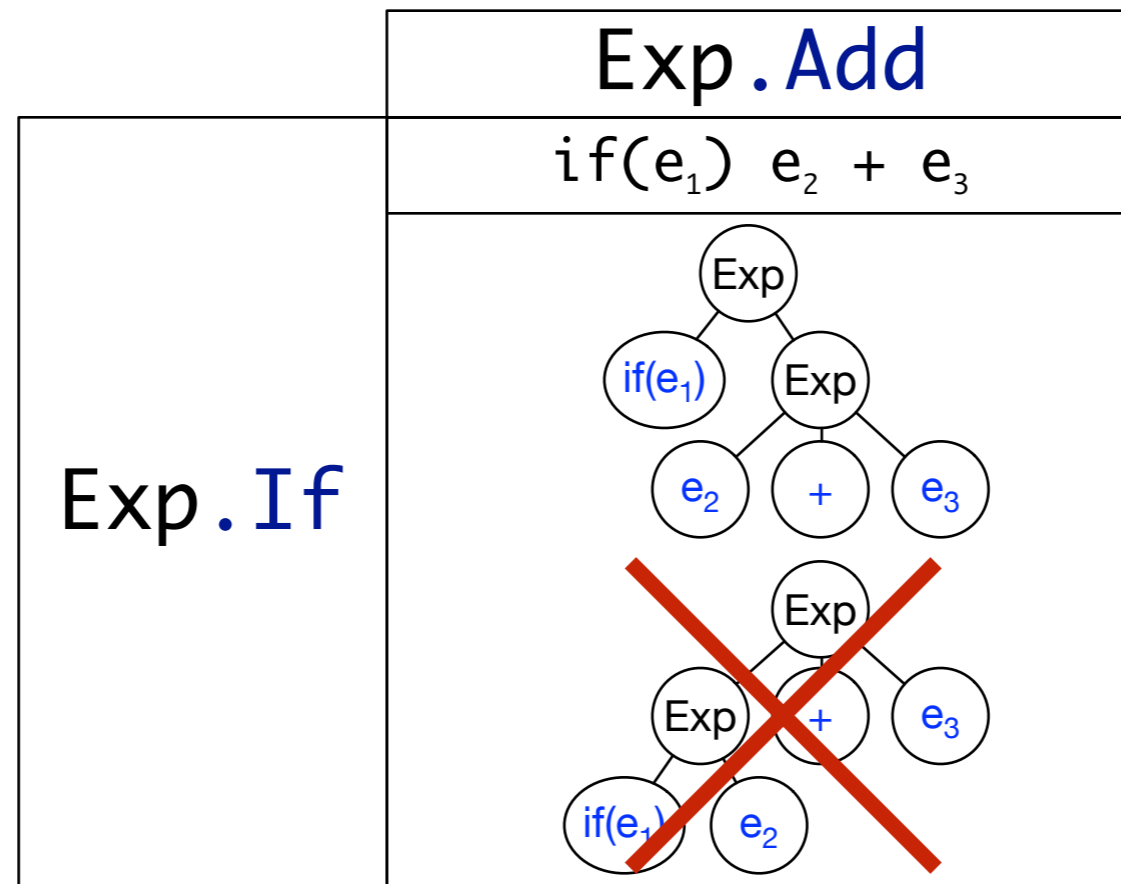
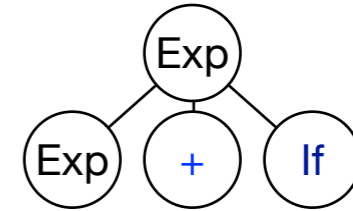
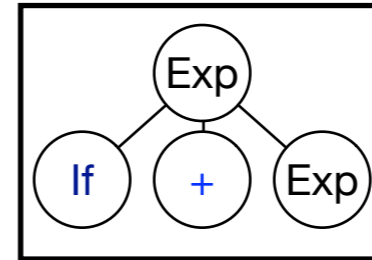
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context-free syntax

Exp.Add = Exp "+" Exp
 Exp.If = "if" "(" Exp ")" Exp

context-free priorities

Exp.Add > Exp.If



context-free syntax

Exp.Min = "-" Exp
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Exp.Lt = Exp "<" Exp
Exp.Add = Exp "+" Exp
Exp.Seq = Exp ";" Exp ";"
Exp.Fac = Exp "!"
Exp = "(" Exp ")"
Exp.Int = INT

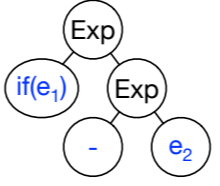
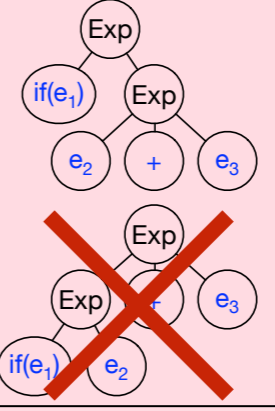
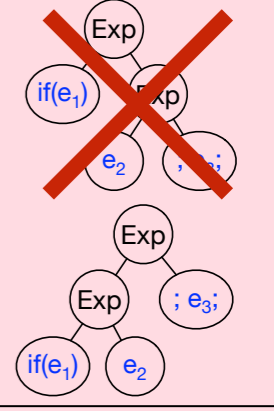
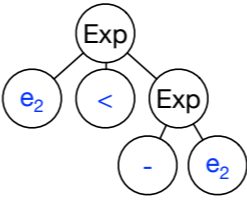
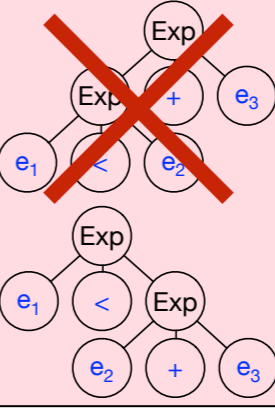
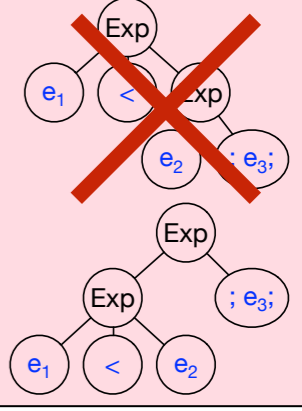
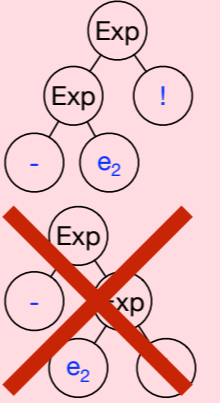
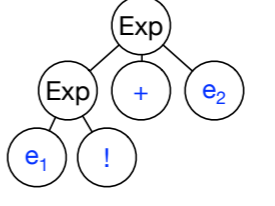
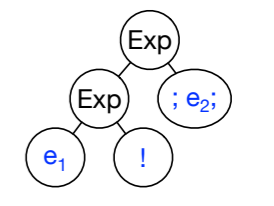
context-free syntax

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 Exp.Add = Exp "+" Exp {left}
 Exp.Seq = Exp ";" Exp ";"
 Exp.Fac = Exp "!"
 Exp = "(" Exp ")" {bracket}
 Exp.Int = INT

context-free priorities

Exp.Min > Exp.Lt > Exp.Add >
 Exp.If > Exp.Seq > Exp.Fac

Exp.Add > Exp.If
 Exp.If > Exp.Seq
 Exp.Add > Exp.Lt
 Exp.Lt > Exp.Seq
 Exp.Min > Exp.Fac

	Exp.Min	Exp.Add	Exp.Seq
Exp.If	$if(e_1) - e_2$ 	$if(e_1) e_2 + e_3$ 	$if(e_1) e_2; e_3;$ 
Exp.Lt	$e_1 < - e_2$ 	$e_1 < e_2 + e_3$ 	$e_1 < e_2; e_3;$ 
Exp.Fac	$- e_1!$ 	$e_1! + e_2$ 	$e_1!; e_2;$ 

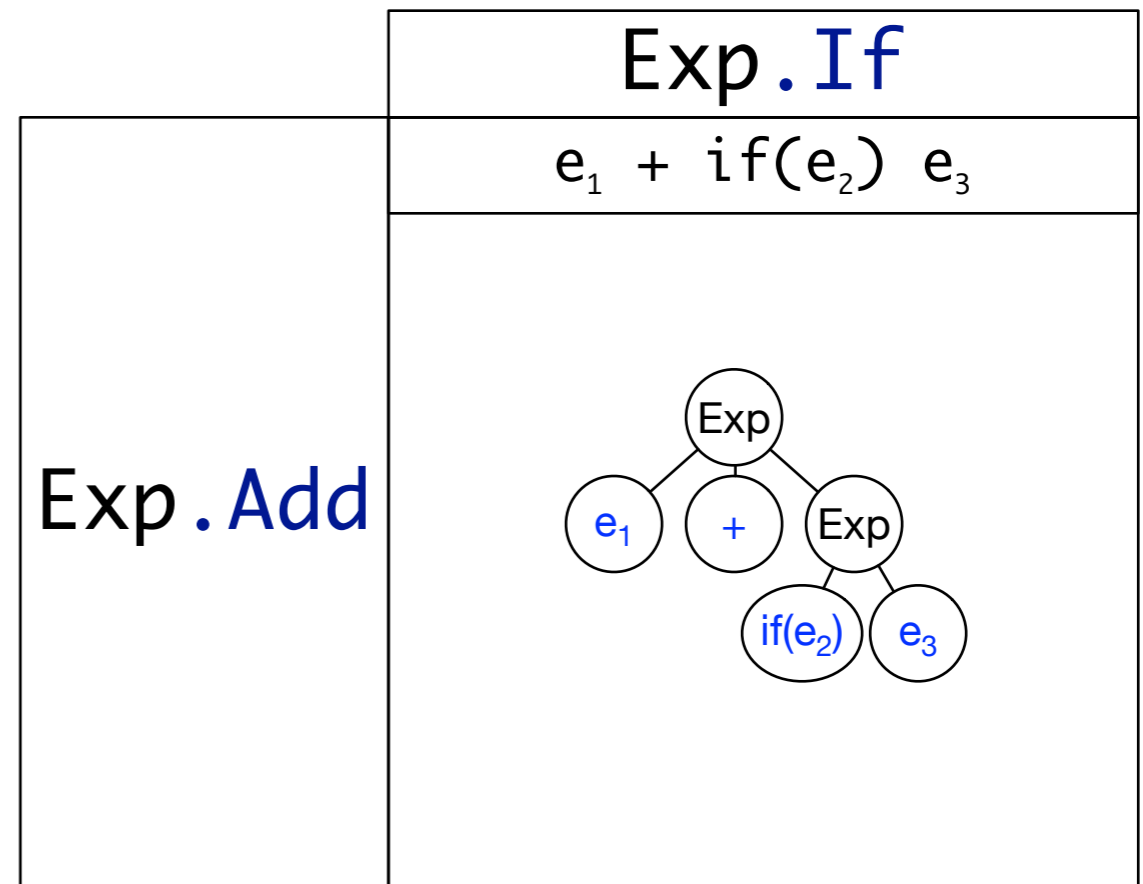
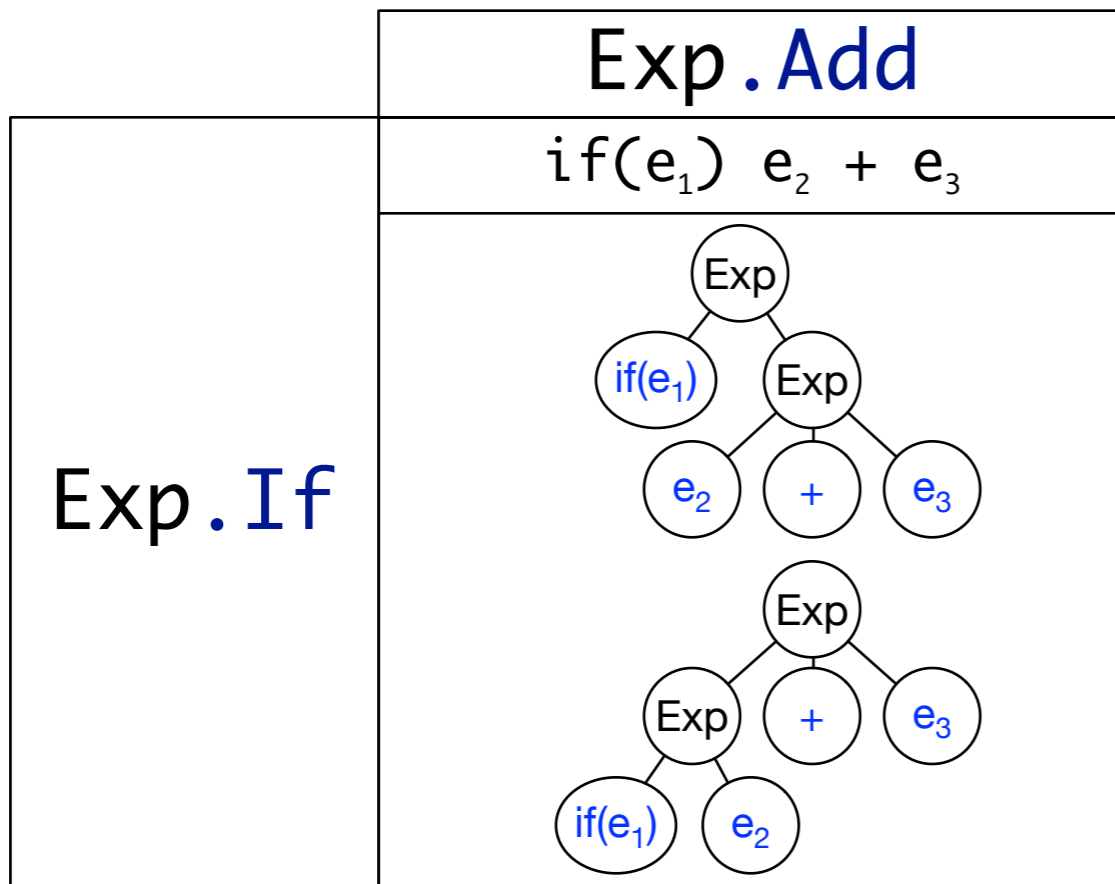
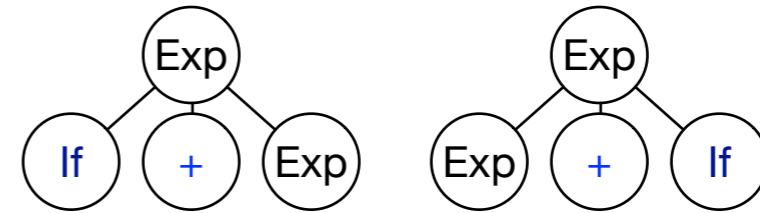
SDF2 Semantics is Unsafe

[Afroozeh et al. 2013]

$$\frac{A.C_1 = \alpha B \gamma > B.C_2 = \beta \in \text{Pr}(G)}{[A.C_1 = \alpha[C_2]\gamma] \in Q_G}$$

Exp.If = "if" "(" Exp ")" Exp
 Exp.Add = Exp "+" Exp

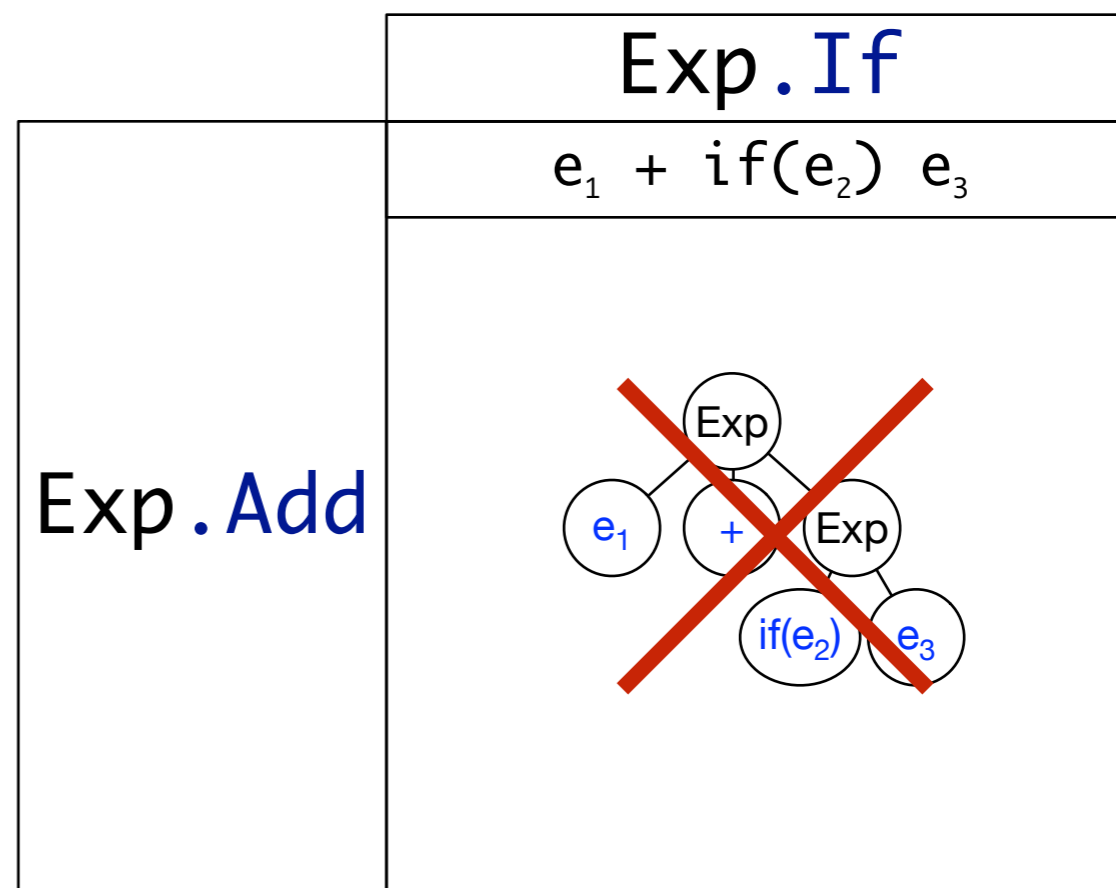
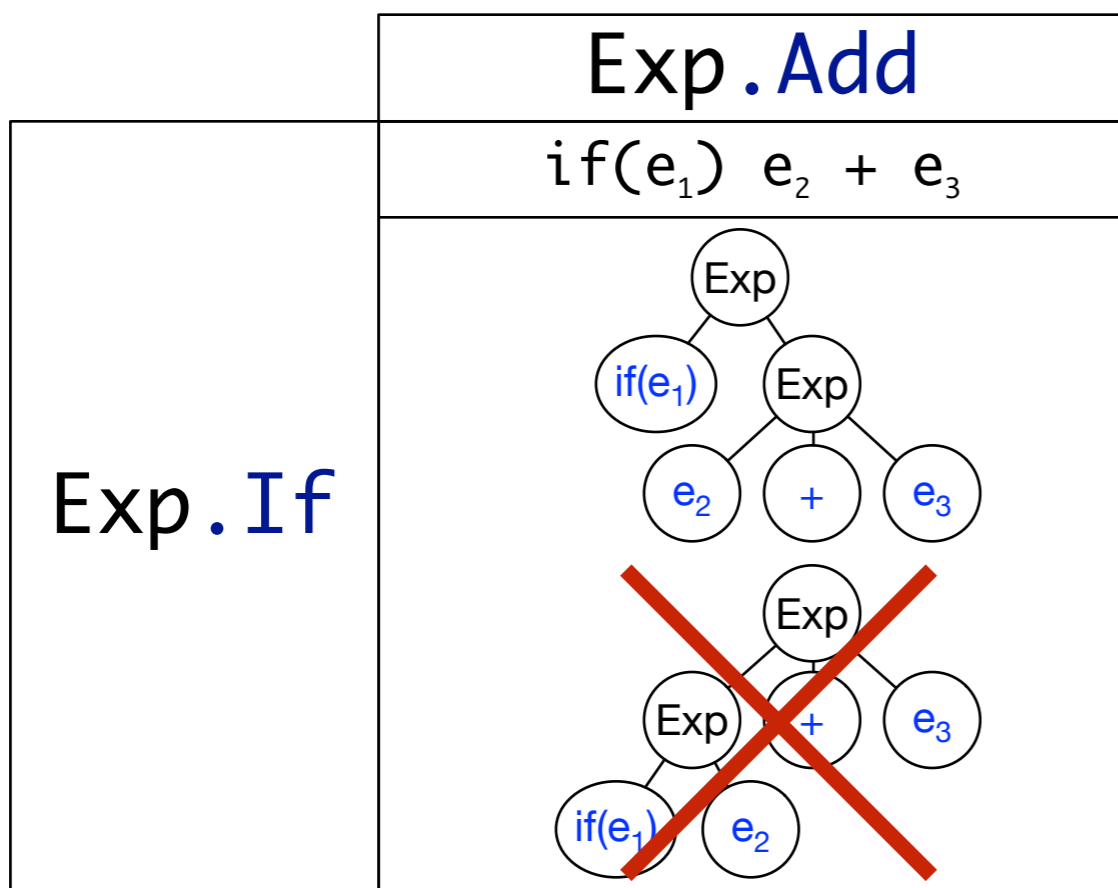
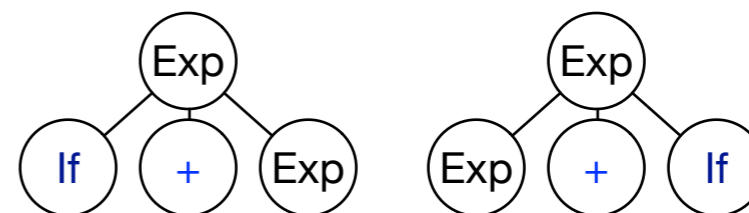
Exp.Add > Exp.If



$$\frac{A.C_1 = \alpha B \gamma > B.C_2 = \beta \in \text{Pr}(G)}{[A.C_1 = \alpha[C_2]\gamma] \in Q_G}$$

Exp.If = "if" "(" Exp ")" Exp
 Exp.Add = Exp "+" Exp

Exp.Add > Exp.If



context-free syntax

Exp.Min = "-" Exp
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 Exp.Lt = Exp "<" Exp {right}
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context-free priorities

Exp.Min > Exp.Lt > Exp.Add >
 Exp.If > Exp.Seq > Exp.Fac

Exp.Add > Exp.If
 Exp.If > Exp.Seq
 Exp.Add > Exp.Lt
 Exp.Lt > Exp.Seq
 Exp.Min > Exp.Fac
 Exp.Add > Exp.Fac
 Exp.Seq > Exp.Fac

	Exp.Min	Exp.Add	Exp.Seq
Exp.If	$if(e_1) - e_2$ 	$if(e_1) e_2 + e_3$ 	$if(e_1) e_2; e_3;$
Exp.Lt	$e_1 < - e_2$ 	$e_1 < e_2 + e_3$ 	$e_1 < e_2; e_3;$
Exp.Fac	$- e_1!$ 	$e_1! + e_2$ 	$e_1!; e_2;$

Disambiguation Safety

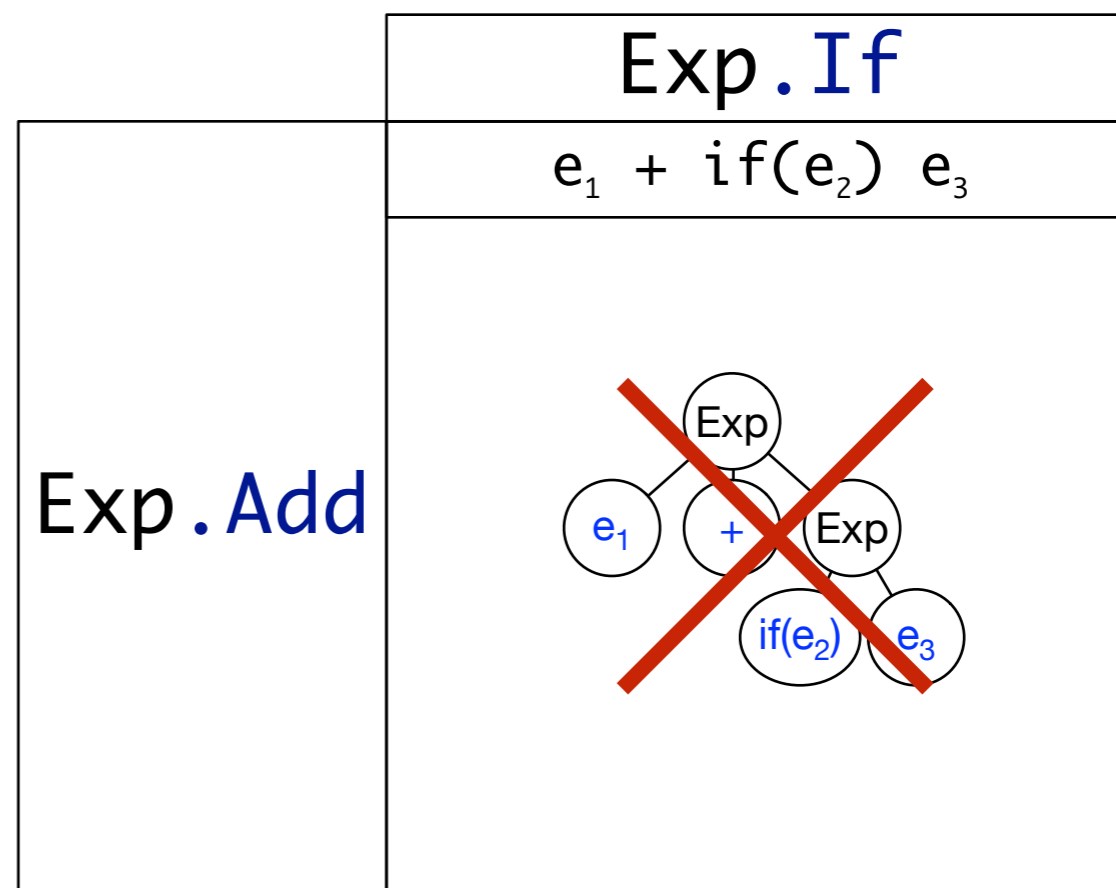
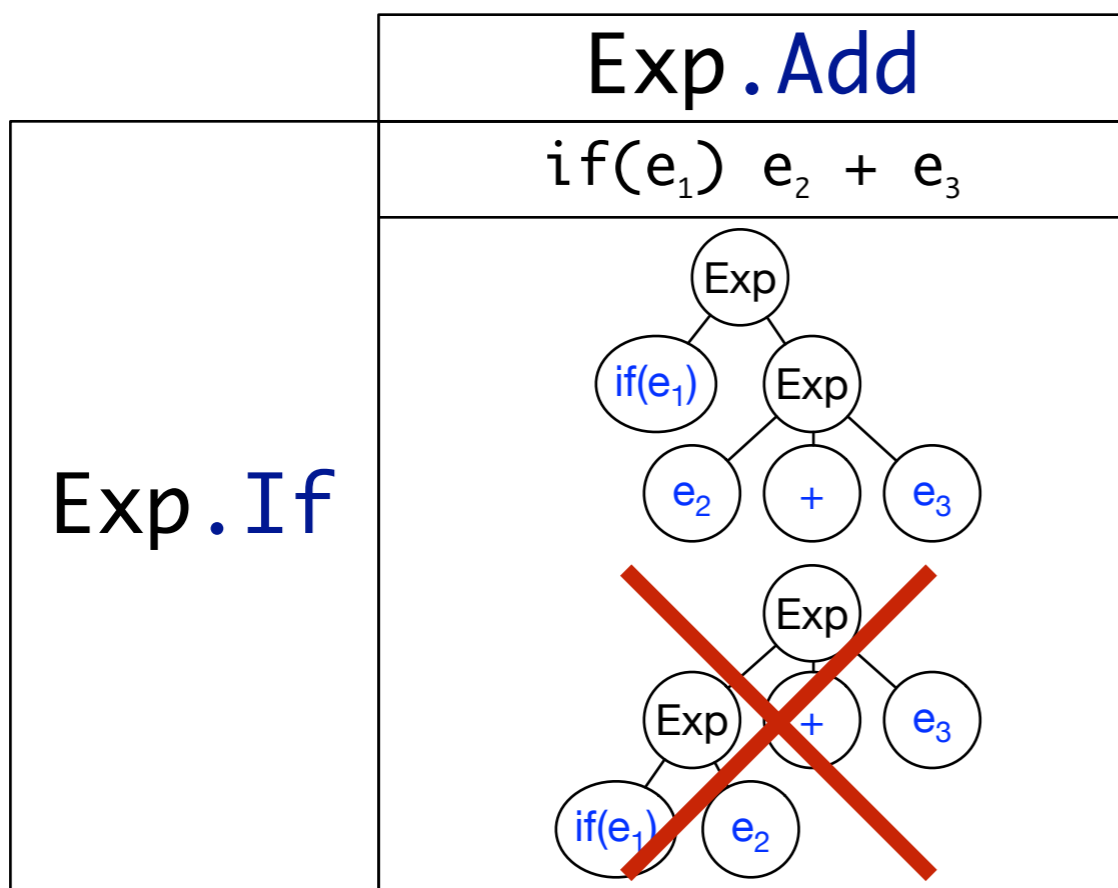
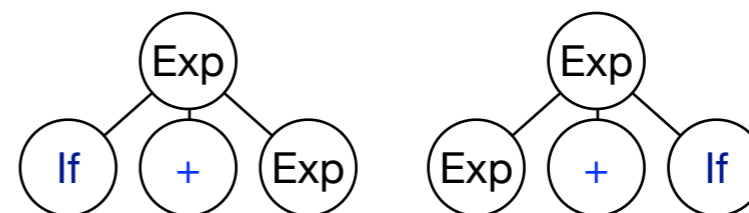
Disambiguation should not reject
unambiguous sentences

Safe Semantics

$$\frac{A.C_1 = \alpha B \gamma > B.C_2 = \beta \in \text{Pr}(G)}{[A.C_1 = \alpha[C_2]\gamma] \in Q_G}$$

Exp.If = "if" "(" Exp ")" Exp
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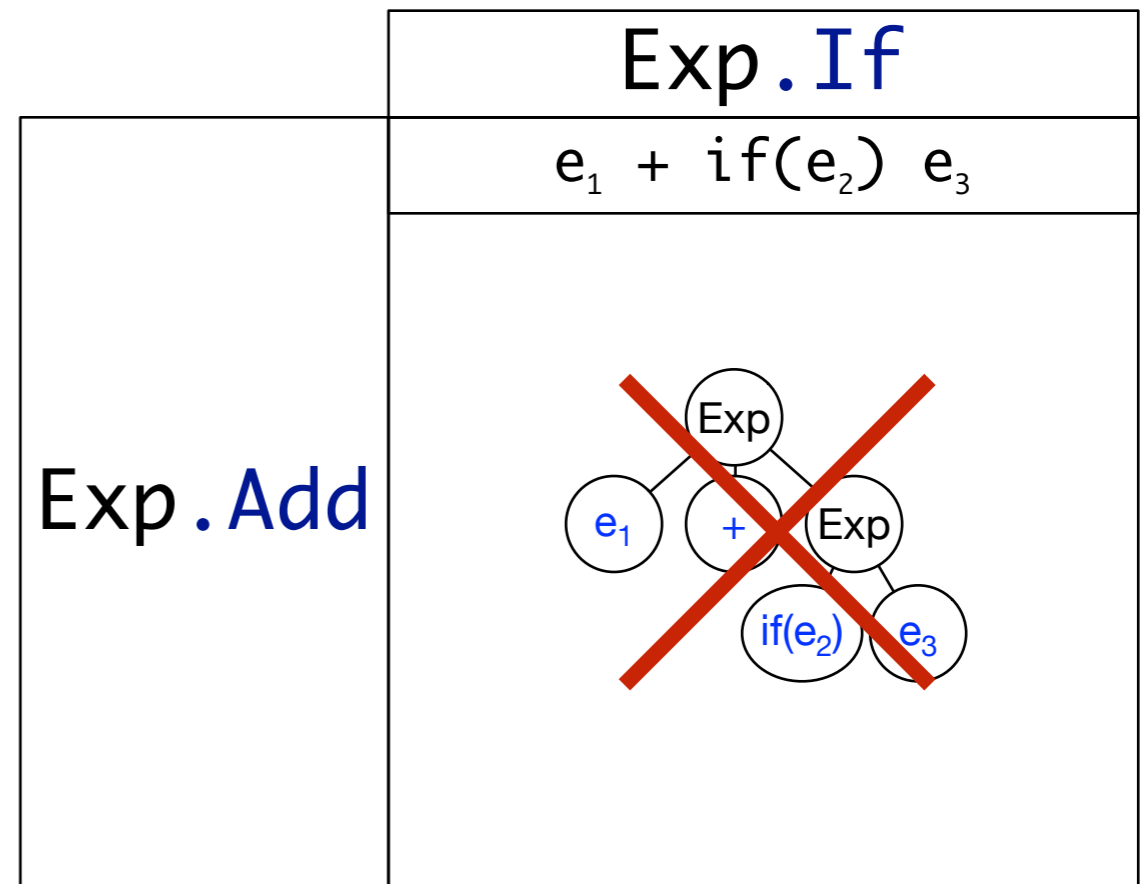
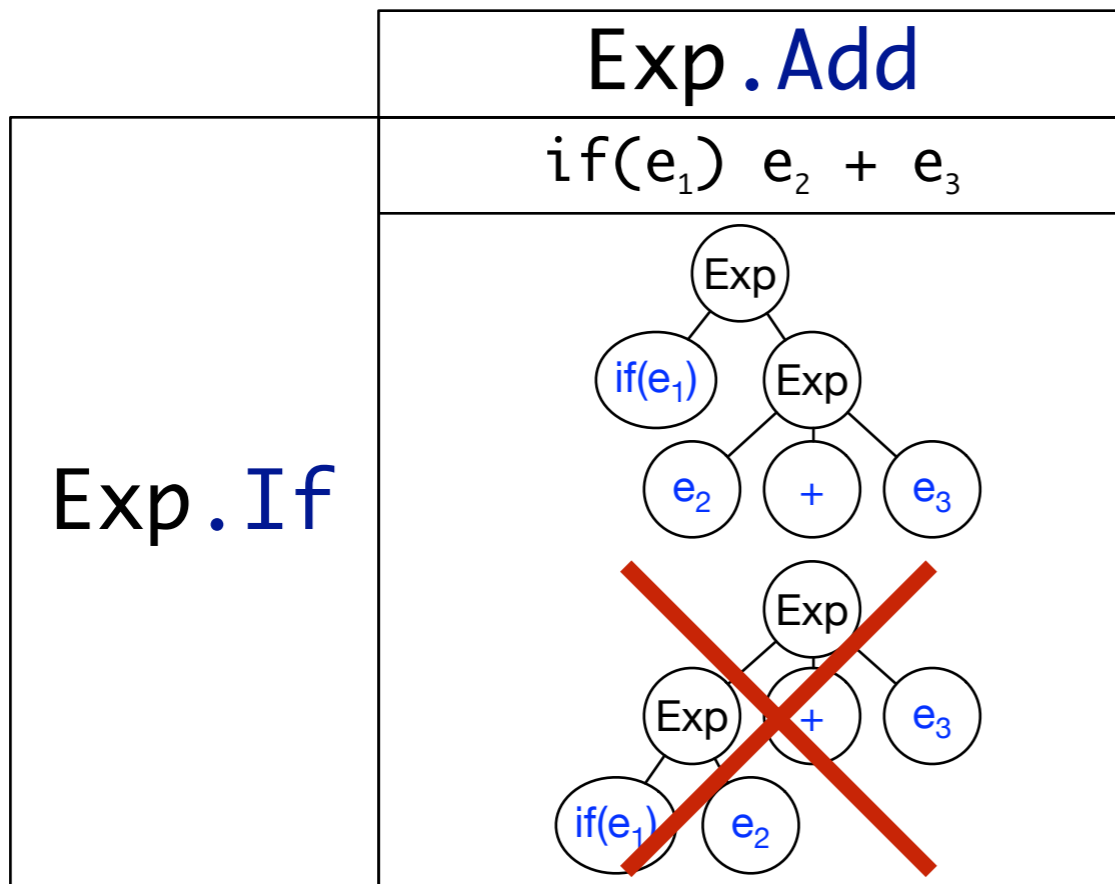
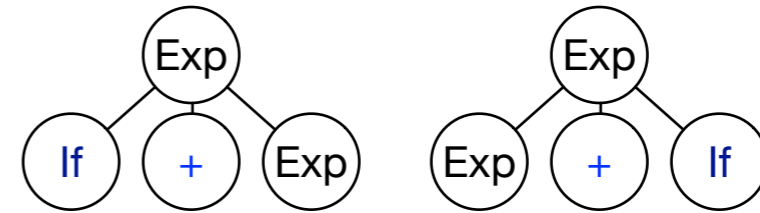
Exp.Add > Exp.If



$$\frac{A.C_1 = \alpha B \gamma > B.C_2 = \beta \in \text{Pr}(G)}{[A.C_1 = \alpha[C_2]\gamma] \in Q_G}$$

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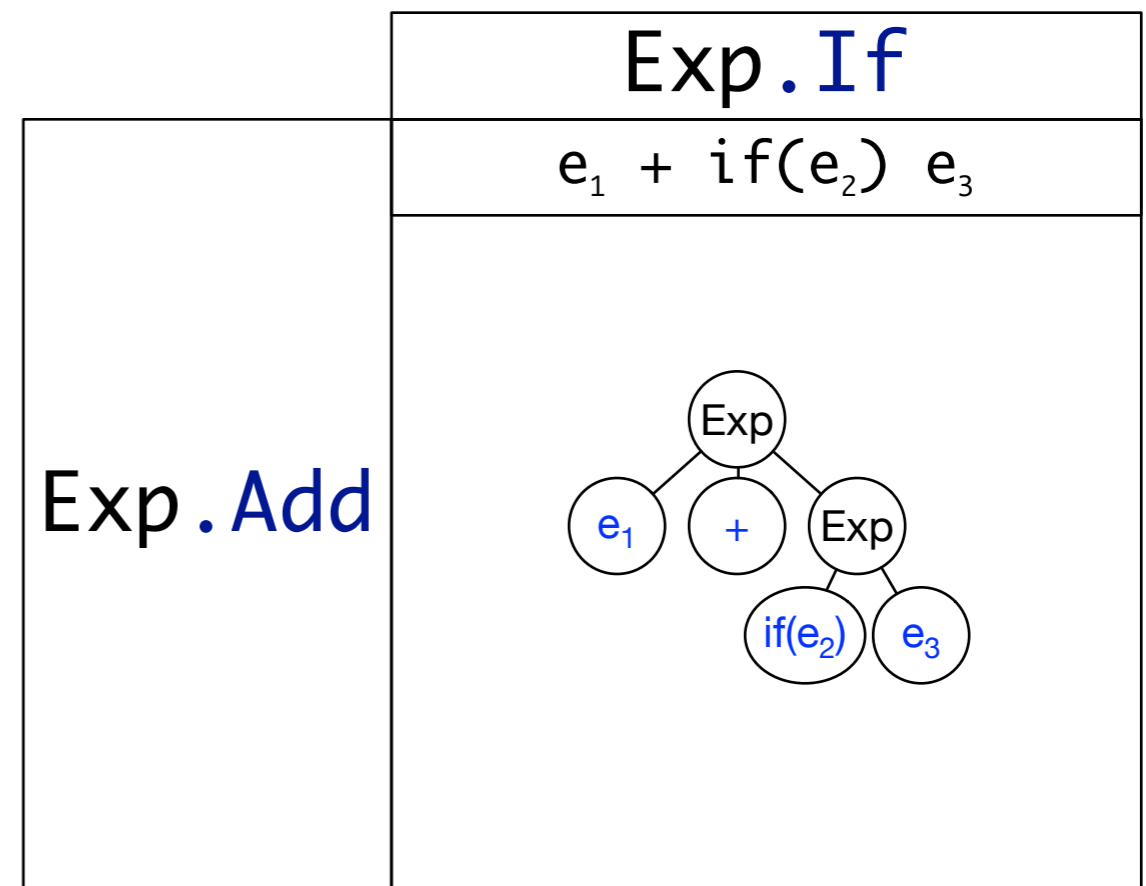
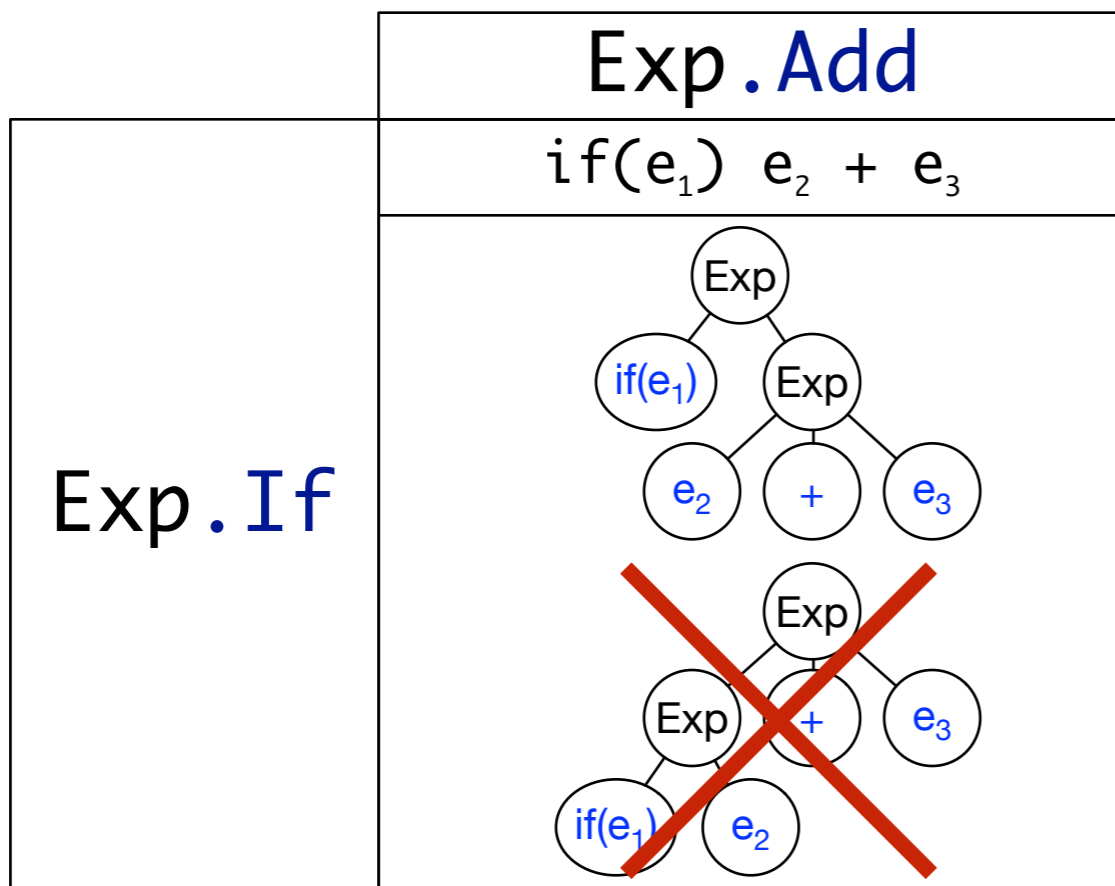
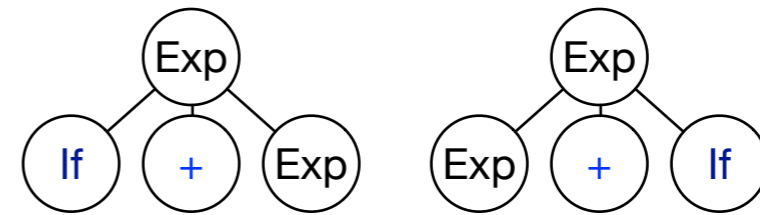


$$\frac{A.C_1 = \alpha B \gamma > B.C_2 = \beta \in \text{Pr}(G)}{[A.C_1 = \alpha [C_2] \gamma] \in Q_G}$$

$$\frac{A.C_1 = A \gamma > A.C_2 = \alpha A \in \text{Pr}(G)}{[A.C_1 = [C_2] \gamma] \in Q'_G}$$

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Exp.Add > Exp.If



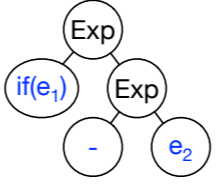
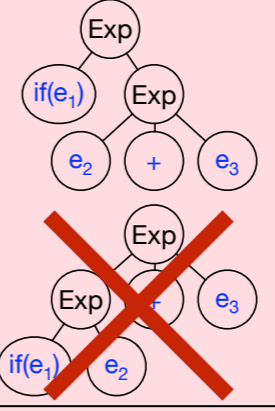
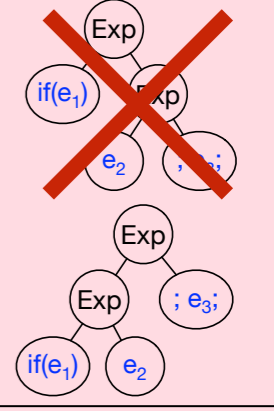
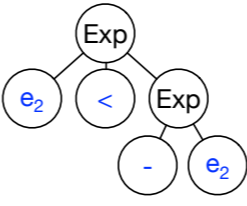
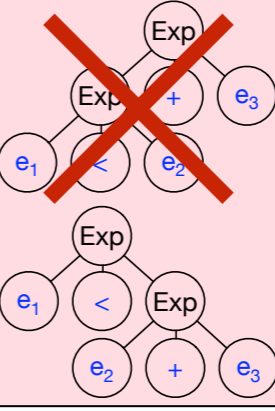
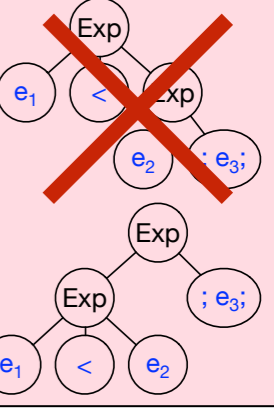
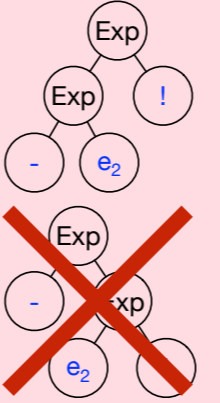
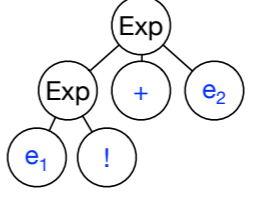
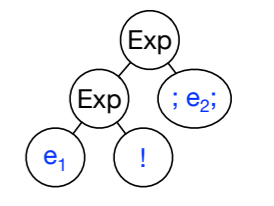
context-free syntax

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 Exp.Lt = Exp "<" Exp {right}
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 Exp.Seq = Exp ";" Exp ";"
 Exp.Fac = Exp "!"
 Exp = "(" Exp ")" {bracket}
 Exp.Int = INT

context-free priorities

Exp.Min > Exp.Lt > Exp.Add >
 Exp.If > Exp.Seq > Exp.Fac

Exp.Add > Exp.If
 Exp.If > Exp.Seq
 Exp.Add > Exp.Lt
 Exp.Lt > Exp.Seq
 Exp.Min > Exp.Fac
 Exp.Add > Exp.Fac
 Exp.Seq > Exp.Fac

	Exp.Min	Exp.Add	Exp.Seq
Exp.If	$if(e_1) - e_2$ 	$if(e_1) e_2 + e_3$ 	$if(e_1) e_2; e_3;$ 
Exp.Lt	$e_1 < - e_2$ 	$e_1 < e_2 + e_3$ 	$e_1 < e_2; e_3;$ 
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context-free priorities

Exp.Min > Exp.Lt > Exp.Add >
 Exp.If > Exp.Seq > Exp.Fac

Exp.Add > Exp.If
 Exp.If > Exp.Seq
 Exp.Add > Exp.Lt
 Exp.Lt > Exp.Seq
 Exp.Min > Exp.Fac
 Exp.Add > Exp.Fac
 Exp.Seq > Exp.Fac

	Exp.If	Exp.Lt	Exp.Fac
Exp.Min	- if(e ₁) e ₂	- e ₂ < e ₃	- e ₁ !
Exp.Add	e ₁ + if(e ₂) e ₃	e ₁ + e ₂ < e ₃	e ₁ + e ₂ !
Exp.Seq	if(e ₁) e ₂ ; e ₃ ;	e ₁ ; e ₂ ; < e ₃	e ₁ ; e ₂ !;

Deep Conflicts

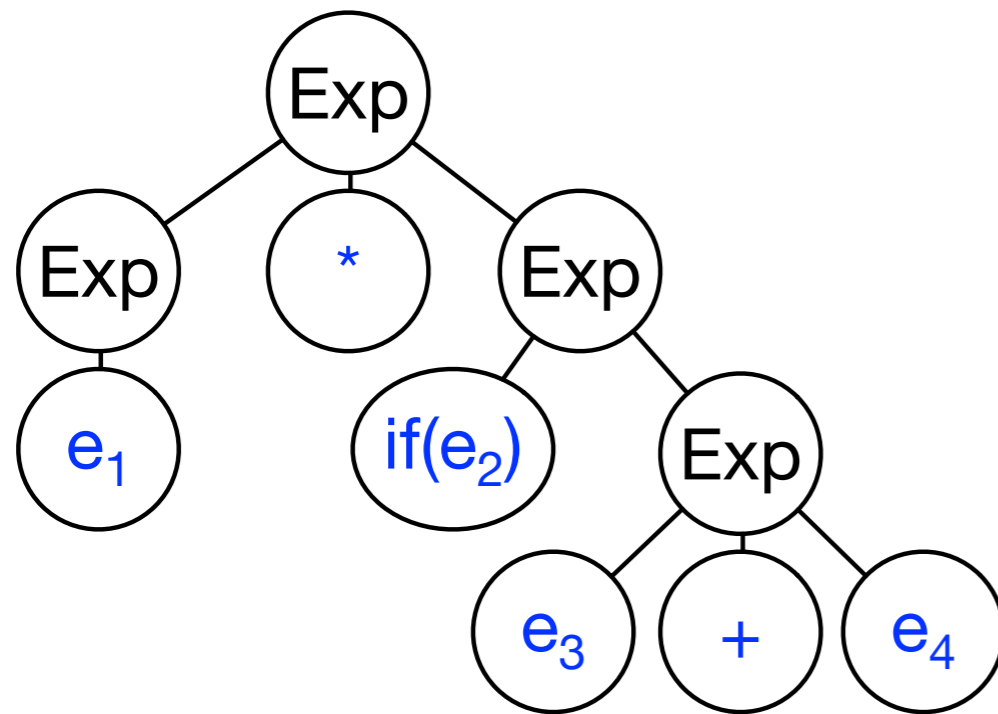
context-free syntax

Exp.If = "if" "(" Exp ")" Exp
Exp.Add = Exp "+" Exp {left}
Exp.Mul = Exp "*" Exp {left}
Exp.Int = INT

context-free priorities

Exp.Mul > Exp.Add > Exp.If

$e_1 * \text{if}(e_2) e_3 + e_4$



$e_1 * [\text{if}(e_2) e_3 + e_4]$

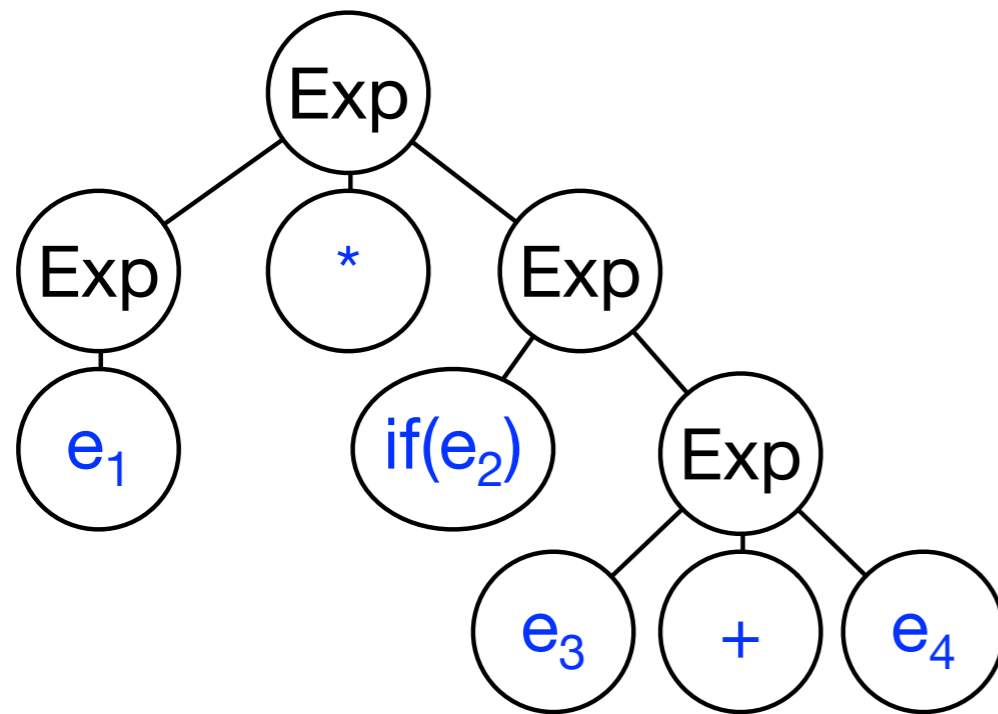
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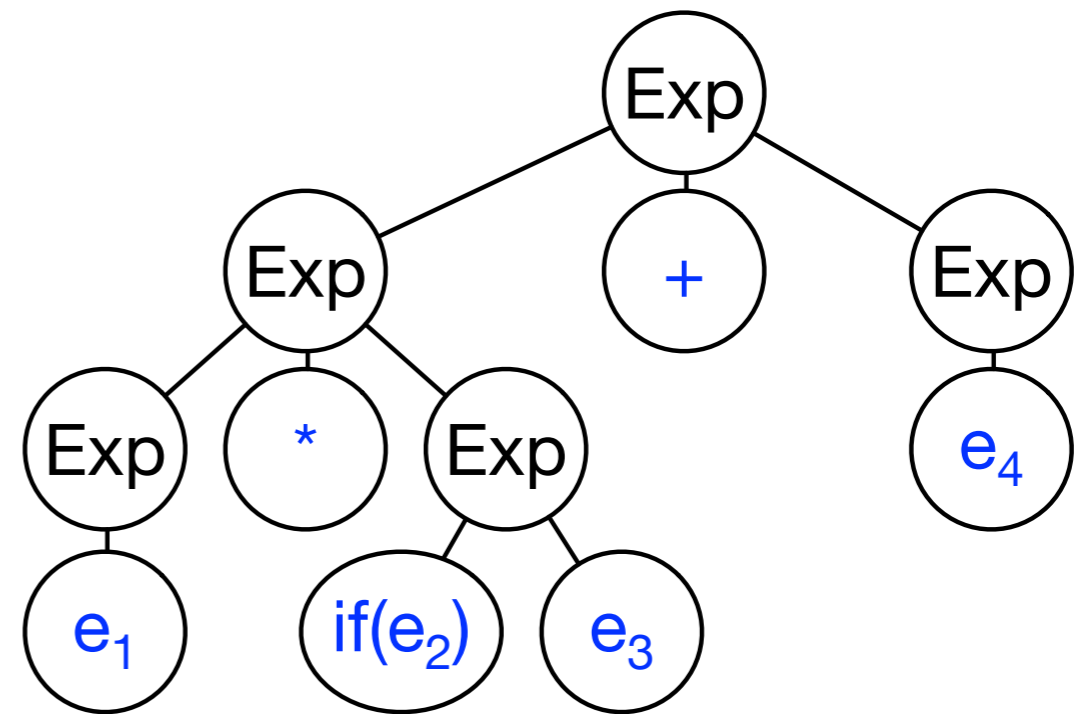
context-free priorities

Exp.Mul > Exp.Add > Exp.If

$e_1 * \text{if}(e_2) e_3 + e_4$



$e_1 * [\text{if}(e_2) e_3 + e_4]$



$[e_1 * \text{if}(e_2) e_3] + e_4$

context-free syntax

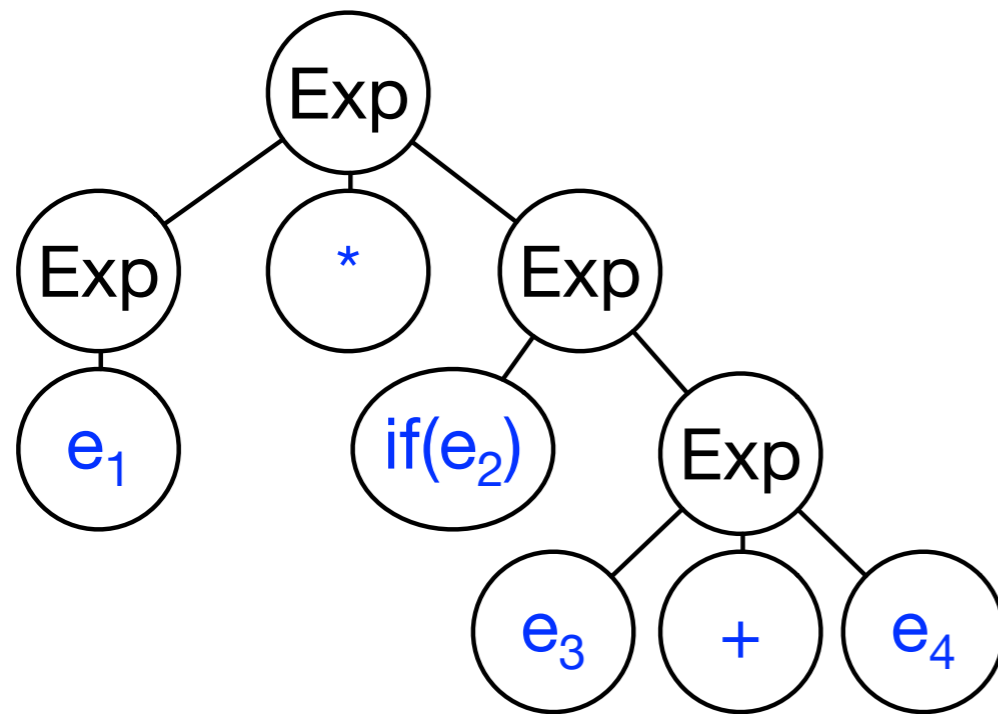
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context-free priorities

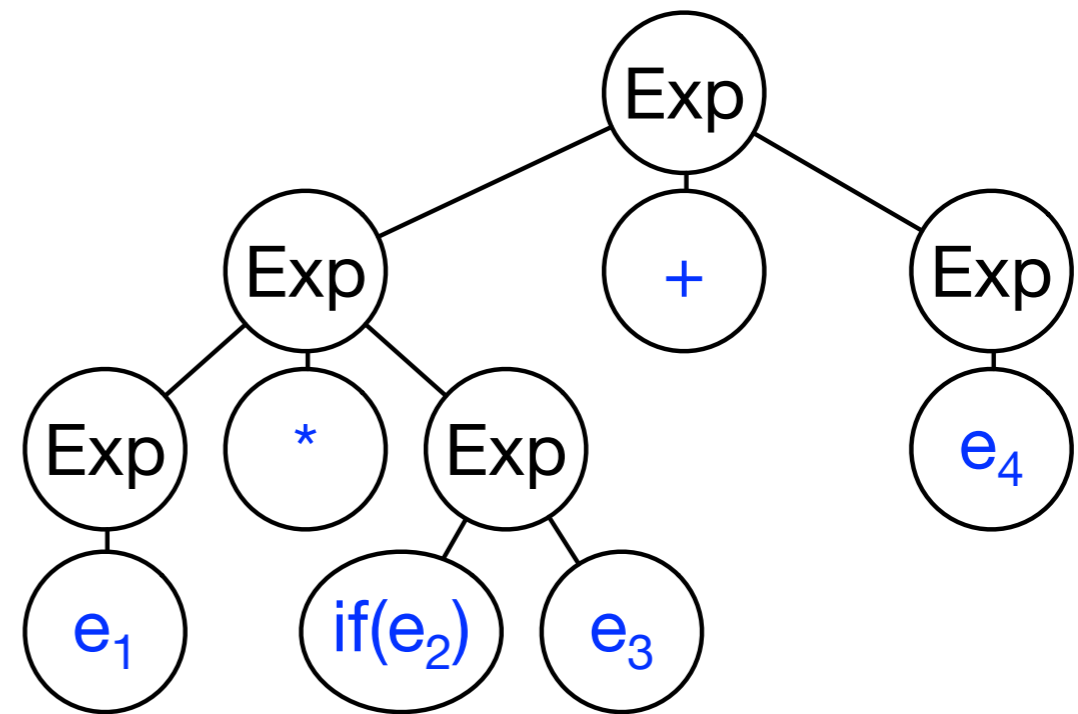
Exp.Mul > Exp.Add > Exp.If

$$e_1 * \text{if}(e_2) e_3 + e_4$$

Deep Priority Conflict!



$$e_1 * [if(e_2) e_3 + e_4]$$

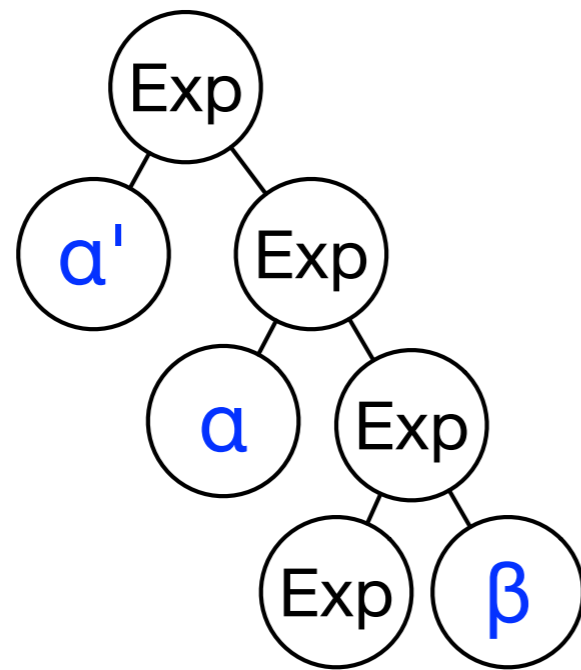


$$[e_1 * if(e_2) e_3] + e_4$$

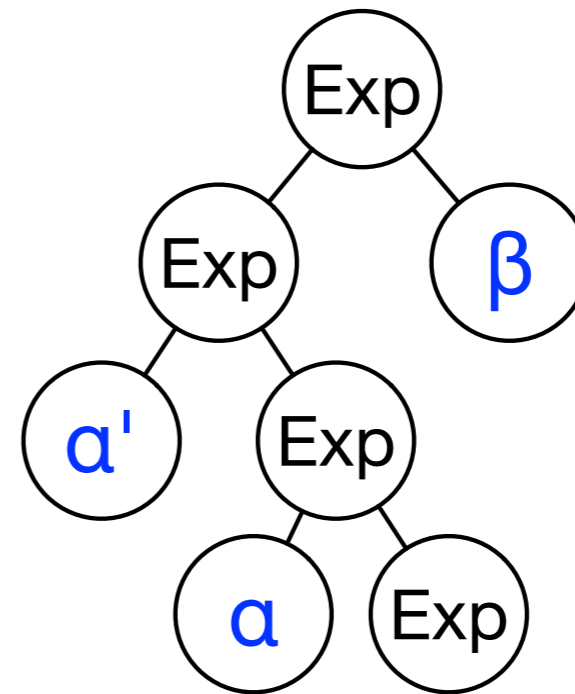
Operator-style Deep Conflict

Exp = α Exp
Exp = Exp β
Exp = α' Exp
 $\alpha' > \beta > \alpha$

α' α Exp β



α' α [Exp β]



[α' α Exp] β

context-free syntax

Exp.If = "if" "(" Exp ")" Exp
 Exp.Add = Exp "+" Exp {left}
 Exp.Mul = Exp "*" Exp {left}
 Exp.Int = INT

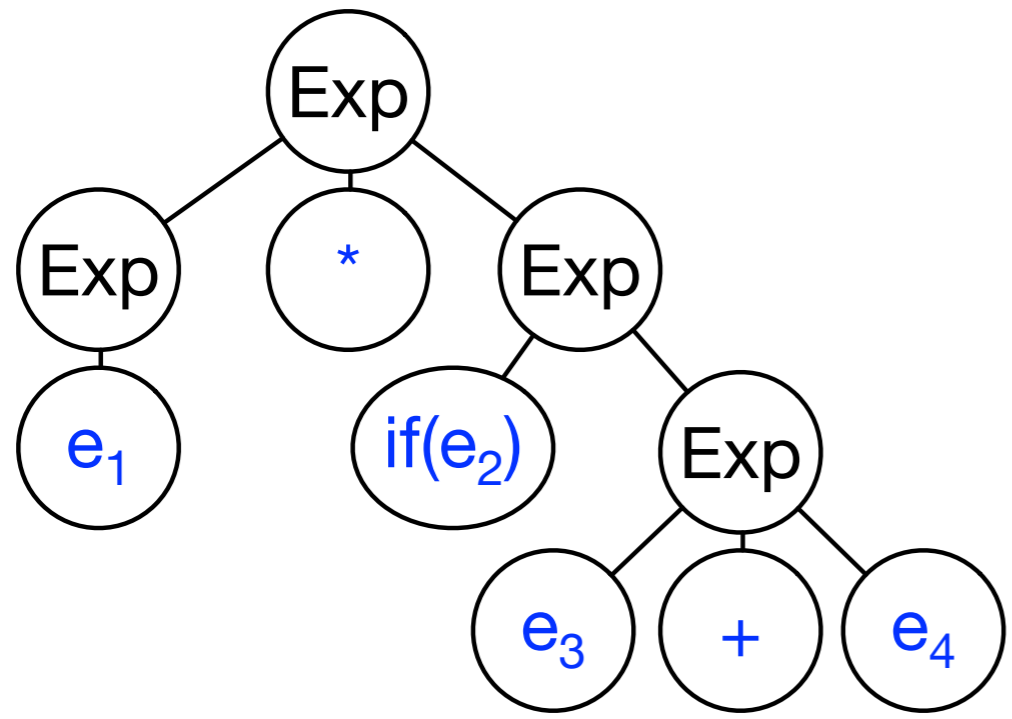
context-free priorities

Exp.Mul > Exp.Add > Exp.If

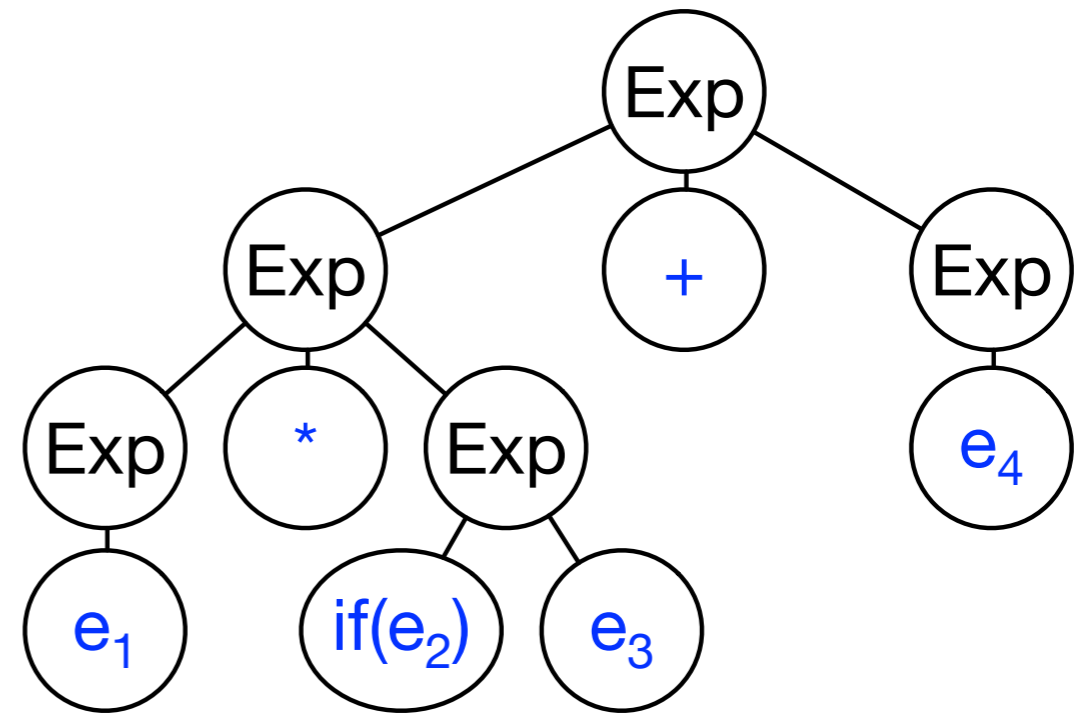
$$\frac{A.C_2 > A.C_1 \in \text{Pr}(G) \quad \alpha \stackrel{*}{\neq}_G A\beta}{[A.C_2 = [A.C_1 = \alpha A]y] \in Q_G^{rm}}$$

$$e_1 * \text{if}(e_2) e_3 + e_4$$

Deep Priority Conflict!



$$e_1 * [if(e_2) e_3 + e_4]$$



$$[e_1 * if(e_2) e_3] + e_4$$

context-free syntax

Exp.If = "if" "(" Exp ")" Exp
 Exp.Add = Exp "+" Exp {left}
 Exp.Mul = Exp "*" Exp {left}
 Exp.Int = INT

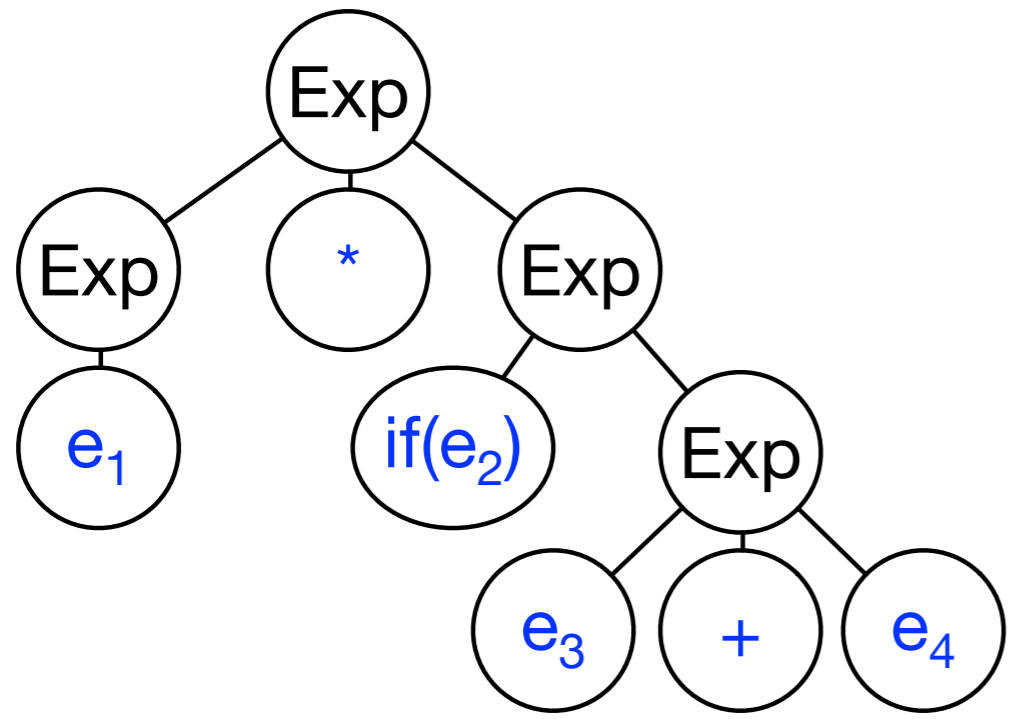
context-free priorities

Exp.Mul > Exp.Add > Exp.If

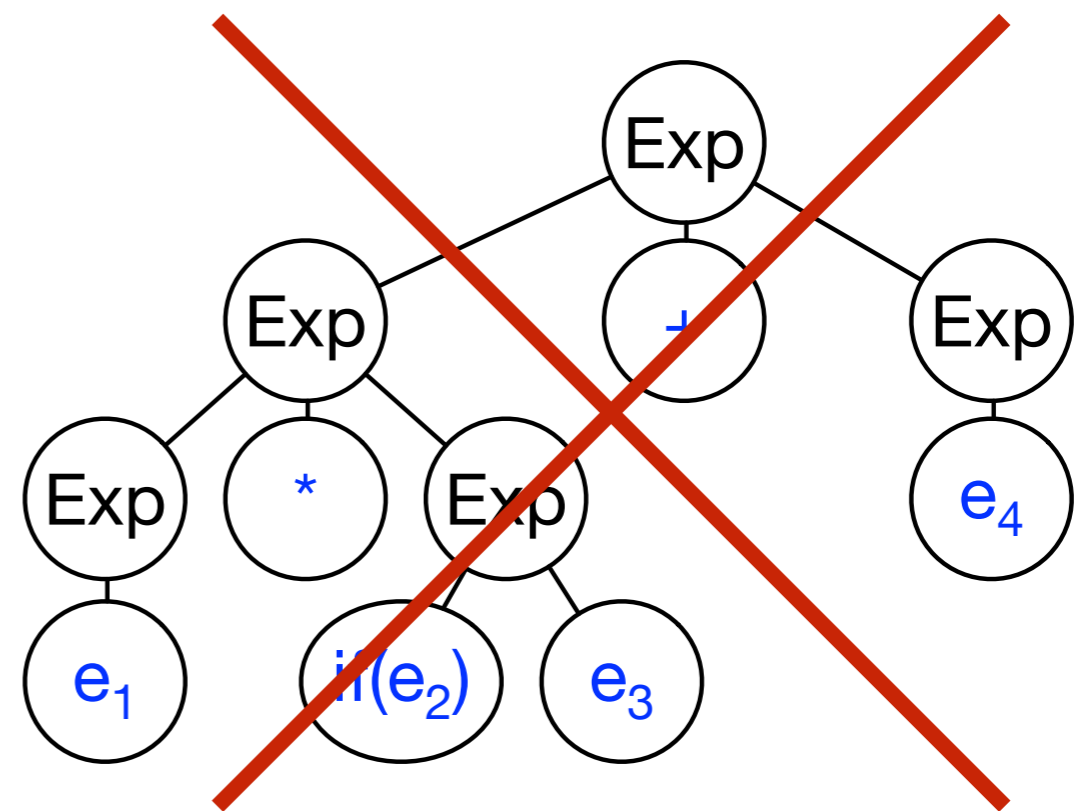
$$\frac{A.C_2 > A.C_1 \in \text{Pr}(G) \quad \alpha \stackrel{*}{\neq}_G A\beta}{[A.C_2 = [A.C_1 = \alpha A]y] \in Q_G^{rm}}$$

$$e_1 * \text{if}(e_2) e_3 + e_4$$

Deep Priority Conflict!



$$e_1 * [if(e_2) e_3 + e_4]$$



$$[e_1 * if(e_2) e_3] + e_4$$

Contextual Grammars

context-free syntax

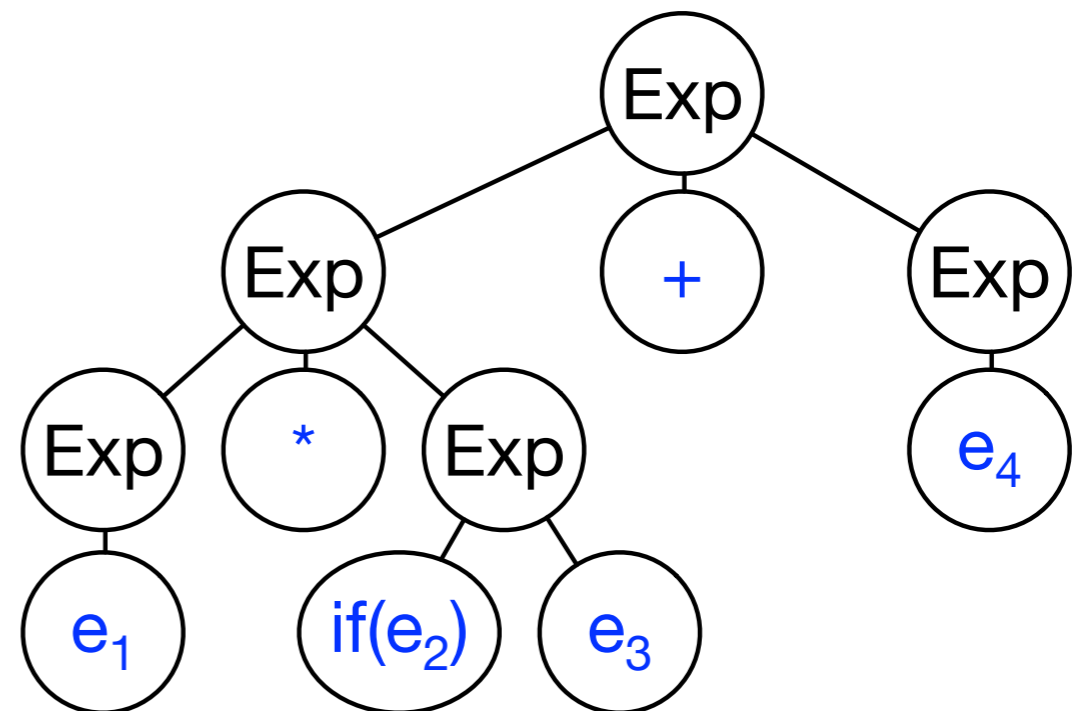
Exp.If = "if" "(" Exp ")" Exp
Exp.Add = Exp "+" Exp {left}
Exp.Mul = Exp "*" Exp {left}
Exp.Int = INT

context-free priorities

Exp.Mul > Exp.Add > Exp.If

$e_1 * \text{if}(e_2) e_3 + e_4$

Deep Priority Conflict!



$[e_1 * \text{if}(e_2) e_3] + e_4$

context-free syntax

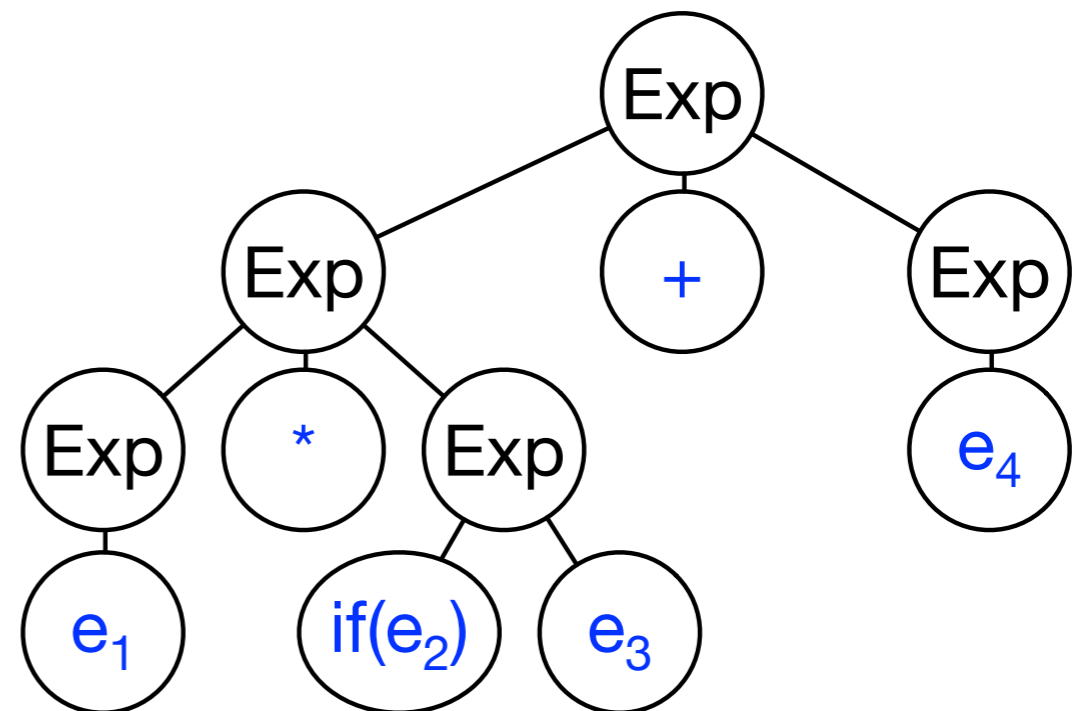
Exp.If = "if" "(" Exp ")" Exp
Exp.Add = Exp_{if} "+" Exp {left}
Exp.Mul = Exp "*" Exp {left}
Exp.Int = INT

context-free priorities

Exp.Mul > Exp.Add > Exp.If

$$e_1 * \text{if}(e_2) e_3 + e_4$$

Deep Priority Conflict!



$$[e_1 * \text{if}(e_2) e_3] + e_4$$

context-free syntax

Exp.If = "if" "(" Exp ")" Exp
Exp.Add = Exp_{if} "+" Exp {left}
Exp.Mul = Exp "*" Exp {left}
Exp.Int = INT

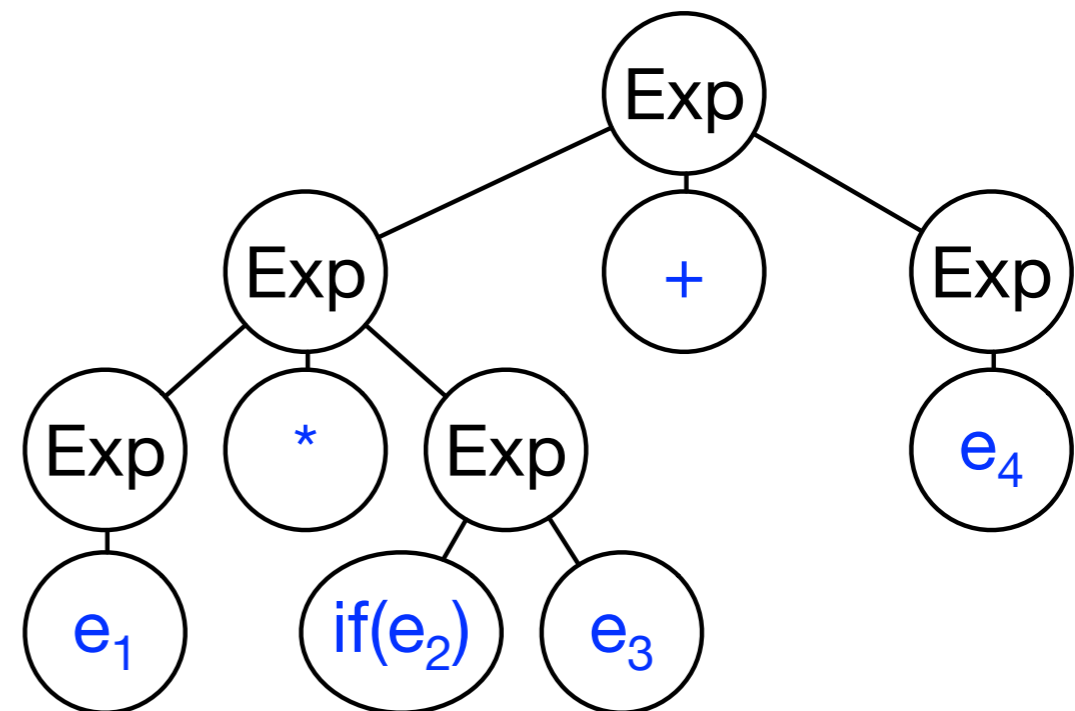
Exp_{if}.Add = Exp_{if} "+" Exp_{if} {left}
Exp_{if}.Mul = Exp "*" Exp_{if} {left}
Exp_{if}.Int = INT

context-free priorities

Exp.Mul > Exp.Add > Exp.If

$e_1 * \text{if}(e_2) e_3 + e_4$

Deep Priority Conflict!



$[e_1 * \text{if}(e_2) e_3] + e_4$

context-free syntax

Exp.If = "if" "(" Exp ")" Exp
 Exp.Add = Exp_{if} "+" Exp {left}
 Exp.Mul = Exp_{if} "*" Exp {left}
 Exp.Int = INT

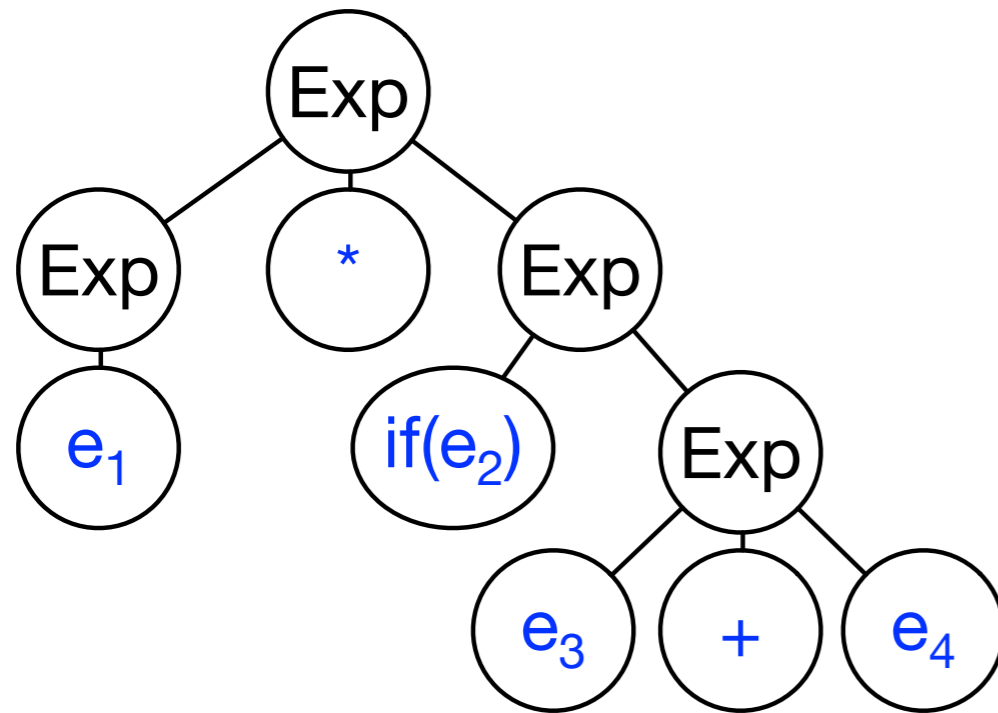
Exp_{if}.Add = Exp_{if} "+" Exp_{if} {left}
 Exp_{if}.Mul = Exp_{if} "*" Exp_{if} {left}
 Exp_{if}.Int = INT

context-free priorities

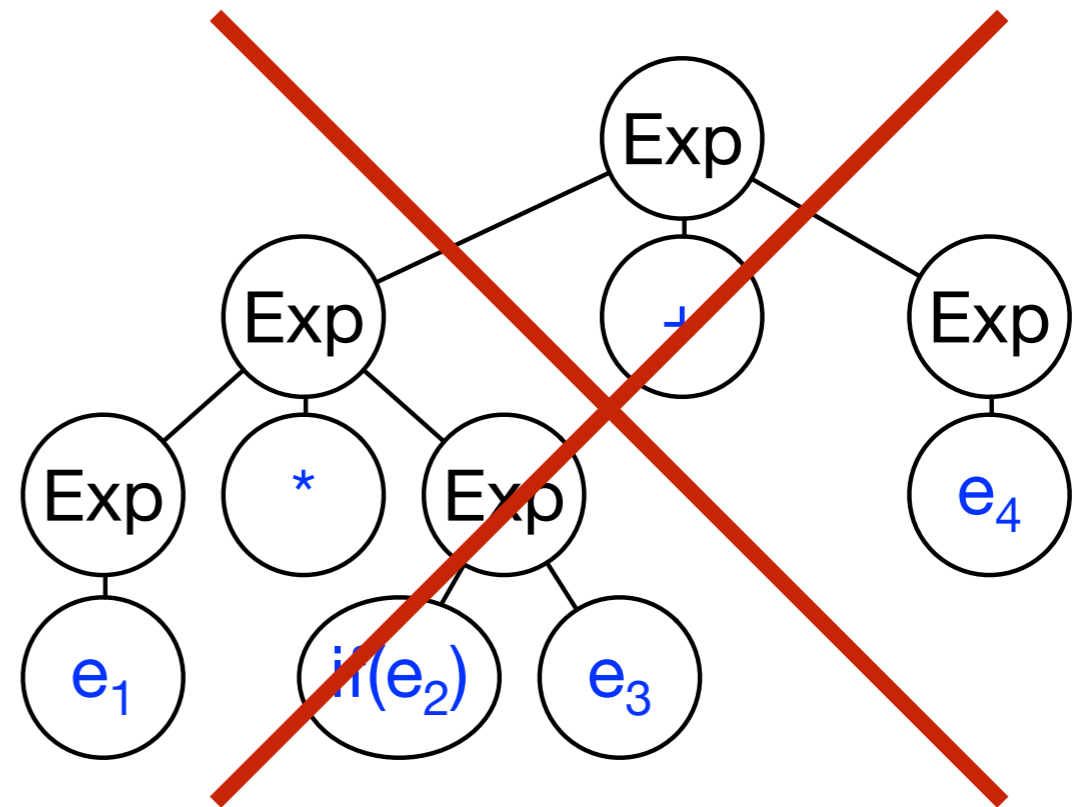
Exp.Mul > Exp.Add > Exp.If

$$e_1 * \text{if}(e_2) e_3 + e_4$$

Deep Priority Conflict!



$$e_1 * [if(e_2) e_3 + e_4]$$



$$[e_1 * if(e_2) e_3] + e_4$$

Spoofax Integration

```

1 module disamb-demo
2
3 imports Common
4
5 context-free start-symbols Exp
6
7 context-free syntax
8
9 Exp.Int      = INT
10 Exp.Var     = ID
11 Exp.Add     = <<Exp> + <Exp>> {left}
12 Exp.If      = <if(<Exp>) <Exp>>
13 Exp.IfElse  = <if(<Exp>) <Exp> else <Exp>>
14 Exp        = <(<Exp>)> {bracket}
15
16 Exp.Match   = <match <Exp> with <Pat+>> {longest-match}
17 Pat.Clause  = [[ID] -> [Exp]]
18
19 //context-free priorities
20 //
21 // Exp.Add > Exp.IfElse > Exp.If > Exp.Match
22
23

```

```

1 a + if(1) 2 + 3

```

```

1 amb(
2   [ Add(
3     Add(Var("a"), If(Int("1"), Int("2")))
4     , Int("3")
5   )
6   , Add(
7     Var("a")
8     , If(Int("1"), Add(Int("2"), Int("3")))
9   )
10 ]
11 )

```

```

1 if(1) if(2) 3 else 4

```

```

1 amb(
2   [ IfElse(
3     Int("1")
4     , If(Int("2"), Int("3"))
5     , Int("4")
6   )
7   , If(
8     Int("1")
9     , IfElse(Int("2"), Int("3"), Int("4"))
10  )
11 ]
12 )

```

Writable

Insert

6 : 6

⋮

```

1 module disamb-demo
2
3 imports Common
4
5 context-free start-symbols Exp
6
7 context-free syntax
8
9 Exp.Int      = INT
10 Exp.Var     = ID
11 Exp.Add     = <<Exp> + <Exp>> {left}
12 Exp.If     = <if(<Exp>) <Exp>>
13 Exp.IfElse = <if(<Exp>) <Exp> else <Exp>>
14 Exp       = <(<Exp>)> {bracket}
15
16 Exp.Match = <match <Exp> with <Pat+>> {longest-match}
17 Pat.Clause = [[ID] -> [Exp]]
18
19 context-free priorities
20
21 Exp.Add > Exp.IfElse > Exp.If > Exp.Match
22
23

```

```

1 if(1 + 2)
2   if(3 + 4 + 5)
3     6 + 7
4   else
5     8 + 9

```

```

1 If(
2   Add(Int("1"), Int("2"))
3 , IfElse(
4   Add(Add(Int("3"), Int("4")), Int("5"))
5   , Add(Int("6"), Int("7"))
6   , Add(Int("8"), Int("9"))
7 )
8 )

```

```

1 match x with
2   z -> 1 + match 5 with
3     a -> a + x
4     y -> 3 + 4

```

```

1 Match(
2   Var("x")
3 , [ Clause(
4   "z"
5   , Add(
6   Int("1")
7   , Match(
8   Int("5")
9   , [ Clause("a", Add(Var("a"), Var("x"))
10  , Clause("y", Add(Int("3"), Int("4"))
11  ]
12  )
13  )
14  )
15 ]

```

Writable

Insert

23 : 2

Status

- Safe and complete semantics for disambiguation with priority and associativity in SDF3 complete for operator-style ambiguities [revision pending]
- Implementation 1: disambiguation of deep conflicts by transformation to contextual grammar [revision pending]
- Implementation 2: data-dependent extension of SGLR; only requires context annotations in original grammar productions [[Programming](#) 2018]
- Available in SDF3+SGLR in current Spoofax LWB
- Applied in grammars for OCaml, Java, ...
- Study: deep conflicts in the wild (they exist) [SLE 2017]